

## Biography of Fangxing (Fran) Li

- B.S. (1994) and M.S. (1997) degrees from Southeast University (China)
- Ph.D. (2001) degree from Virginia Tech
- Senior Engineer, 02/2001 ~ 03/2005, ABB Consulting, Raleigh, NC
- Principal Engineer, 04/2005 ~ 08/2005, ABB Consulting, Raleigh, NC
- Assistant Professor, 08/2005 ~ present, The University of Tennessee, Knoxville, TN
- Registered Professional Engineer in North Carolina (NC)
- IEEE Senior Member, 2005
- UT Eta Kappa Nu Outstanding Teacher Award, 2006



Power Engineering Laboratory

1

**IEEE PES**  
Transmission and Distribution  
CONFERENCE and EXPOSITION  
McCormick Place  
**CHICAGO**

Powering Toward the Future

chicago  
April 21-24, **2008**

## Reactive Power Planning:

- (1) A Review
- (2) VSCOPF with TSV Approach

**Authors: Wenjuan Zhang, Fangxing (Fran) Li, and Leon M. Tolbert**

**Presenter: Fran Li, Ph.D., P.E.**

**Assistant Professor**

**Dept. of Electrical Engineering and Computer Science**



THE UNIVERSITY of TENNESSEE

2

## Outlines

- Introduction to Reactive Power Planning
- Review of RPP: Objectives, Constraints, and Algorithms
- Voltage Stability Constrained OPF approach with Two Sets of Variables
- Conclusions



## Introduction



## Motivation

- Reactive power, or Var, is a critical need for power system operation, and has received greater attention by utilities and researchers since the Great Northeastern Blackout in August 2003.
- The development in Var compensators like SVC and STATCOM makes it more attractive to site Var at appropriate locations with appropriate amount.
- Review of RPP: objectives, constraints, and algorithms
- Present a RPP approach considering voltage stability with two sets of variables



## Review of RPP: Objectives, Constraints, and Algorithms



## Objective functions

- **Minimize Var cost**
  - $C1 \cdot Q_c$  (no fixed cost)
  - $(C0 + C1 \cdot Q_c) \cdot x$  (with fixed cost  $C0$ )
- **Minimize Var cost and real power losses**
- **Minimize Var cost and generator fuel cost**
- **Minimum deviation from a specified point**
  - $\sum (V_i^{max} - V_i)$
- **Voltage stability related objectives**
- **Multi-objective (MO)**



Power Engineering Laboratory

7

## Constraints

- **Optimal Power Flow (OPF)**
  - **Minimize**  $f(u, x)$
  - **Subject to**  $g(u, x) = 0$
  - $h(u, x) \geq 0$
- **Security Constrained OPF (SCOPF)**
  - Considers security constraints
- **Voltage stability constrained OPF**
  - Considers voltage stability constraints



Power Engineering Laboratory

8

## Solution Algorithms

- **Conventional Approaches**
  - *Linear programming*
  - *Nonlinear programming*
  - *Mixed integer nonlinear programming*
- **Intelligent Searches**
  - *Simulated annealing*
  - *Evolutionary Algorithms*
  - *Tabu Search*
- **Fuzzy set theory**
  - *To address uncertainties in constraints as well as objective functions*

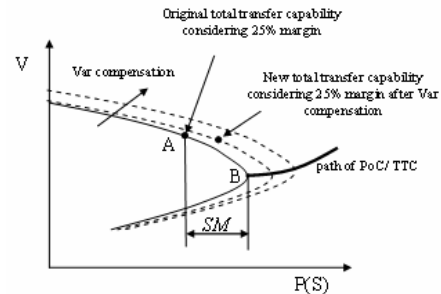


Voltage stability constrained  
RPP with two sets of variables



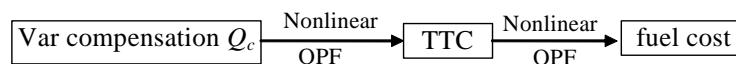
## Var compensation and stability margin

- **Var compensation increases total transfer capability**



- **Var, TTC and cost**

- We may apply an enumerative approach to site Var



Power Engineering Laboratory

11

## A generic approach of two sets of variables

$$\text{Min: } C(x_o, \rho) \longrightarrow \sum f_1(P_{Goi}) + \sum f_2(Q_{ci}) \times y_i$$

Subject to:

$$F(x_o, \rho, TTC_o) = 0$$

$$F(x_*, \rho, TTC_*) = 0$$

$$(TTC_* - TTC_o) / TTC_* = SM$$

$$SM \geq SM_{spec}$$

$$x_{o,min} \leq x_o \leq x_{o,max}$$

$$x_{*,min} \leq x_* \leq x_{*,max}$$

$$\rho_{min} \leq \rho \leq \rho_{max}$$



Power Engineering Laboratory

12

Constraints applicable to both of the normal operating point and PoC

$$\sum y_i = k \quad (\text{Number of Var compensator installations})$$

$$P_{Goi} - P_{Loi} - P(V_i, \theta_i) = 0 \quad (\text{Real power balance})$$

$$P_{G* i} - P_{L* i} - P(V_i, \theta_i) = 0$$

$$Q_{Goi} + Q_c - Q_{Loi} - Q(V_i, \theta_i) = 0 \quad (\text{Reactive power balance})$$

$$Q_{G* i} + Q_c - Q_{L* i} - Q(V_i, \theta_i) = 0$$

$$P_{Gi}^{\min} \leq P_{Goi} \leq P_{Gi}^{\max} \quad (\text{Generation real power limits})$$

$$P_{Gi}^{\min} \leq P_{G* i} \leq P_{Gi}^{\max}$$

$$Q_{Gi}^{\min} \leq Q_{Goi} \leq Q_{Gi}^{\max} \quad (\text{Generation reactive power limits})$$

$$Q_{Gi}^{\min} \leq Q_{G* i} \leq Q_{Gi}^{\max}$$

$$V_i^{\min} \leq V_{oi} \leq V_i^{\max} \quad (\text{Voltage limits})$$

$$V_i^{\min} \leq V_{* i} \leq V_i^{\max}$$

$$|LF_{li}| \leq LF^{\max} \quad (\text{Line flow thermal limits})$$

$$|LF_{li}| \leq LF^{\max}$$

$$SM = \frac{\sum_{i \in S_s} S_{si} - \sum_{i \in S_{li}} S_{li}}{\sum_{i \in S_{li}} S_{li}} \quad (\text{The line MVA TTC security margin})$$

$$SM \geq SM_{\text{spec}} \quad (\text{Security margin limits})$$

$$Q_{ci}^{\min} \leq Q_{ci} \leq Q_{ci}^{\max} \quad (\text{Compensation limits})$$

13

## Constraints are only applicable to PoC

$$P_{L* i} \geq P_{L* i}^0 \quad (i \in \text{Sink}) \quad (\text{real load in load center increases})$$

$$Q_{L* i} \geq Q_{L* i}^0 \quad (i \in \text{Sink}) \quad (\text{reactive load in load center increases})$$

$$P_{G* i} \geq P_{G* i}^0 \quad (i \in \text{Source}) \quad (\text{real power generation in generation center increases})$$

$$P_{G* i} = P_{G* i}^0 + \frac{\left( \sum_{i \in \text{Source}} P_{G* i} - \sum_{i \in \text{Source}} P_{G* i}^0 \right) \times (P_{Gi}^{\max} - P_{G* i}^0)}{\sum_{i \in \text{Source}} (P_{Gi}^{\max} - P_{G* i}^0)} \quad (\text{pattern of generation increase})$$

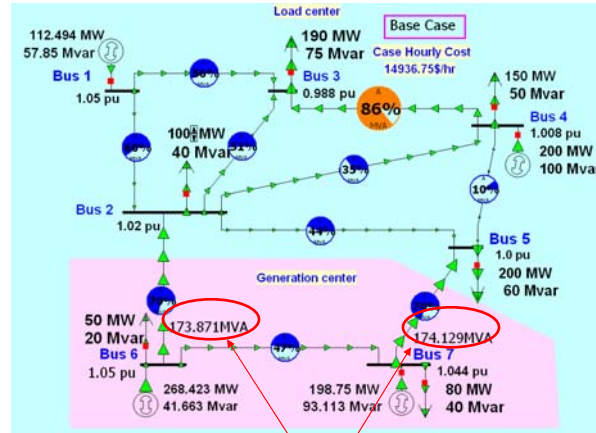
$$P_{L* i} = P_{L* i}^0 + \frac{\left( \sum_{i \in \text{Sink}} P_{L* i} - \sum_{i \in \text{Sink}} P_{L* i}^0 \right) \times P_{L* i}^0}{\sum_{i \in \text{Sink}} P_{L* i}^0} \quad (\text{pattern of load increase})$$

$$P_{L* i} / P_{L* i}^0 = Q_{L* i} / Q_{L* i}^0 \quad (\text{maintaining constant power factor when load increases})$$

14

Power Engineering Laboratory

## Seven-Bus System Example: Base Case



Binding Tie-line flow = 348 MVA

Power Engineering Laboratory

15

## Results from VSCOPF model with the proposed TSV approach

Objective							
Fuel cost (\$/hr)	Var cost (\$/hr)			Total cost (\$/hr)			
15168.98	24.46			15193.44			
Variables output							
Bus	1	2	3	4	5	6	7
$Q_c$ (MVar)			14.54				
$y$ (binary)			1				
$P_{Go}$ (MW)	85			200		300	196
$Q_{Go}$ (MVar)	81			100		52	55
$P_{Lo}$ (MW)		100	190	150	200	50	80
$Q_{Lo}$ (MVar)		40	75	50	60	20	40
$V_e$ (V)	1.05	1.01	0.99	1.00	0.97	1.04	1.01
$TTC_e$ (MVA)	369.54						
$P_{G*}$ (MW)	70			200		300	300
$Q_{G*}$ (MVar)	63			100		98	100
$P_{L*}$ (MW)		113	215	170	226	50	80
$Q_{L*}$ (MVar)		47	87	60	73	20	40
$V_*$ (V)	1.02	1.00	0.95	0.97	0.97	1.05	1.03
$TTC_*$ (MVA)	492.73						

Power Engineering Laboratory

16



## Comparison of three models

Table IV. Results comparison of three models: Enumeration, TSV Model I, and TSV Model II.

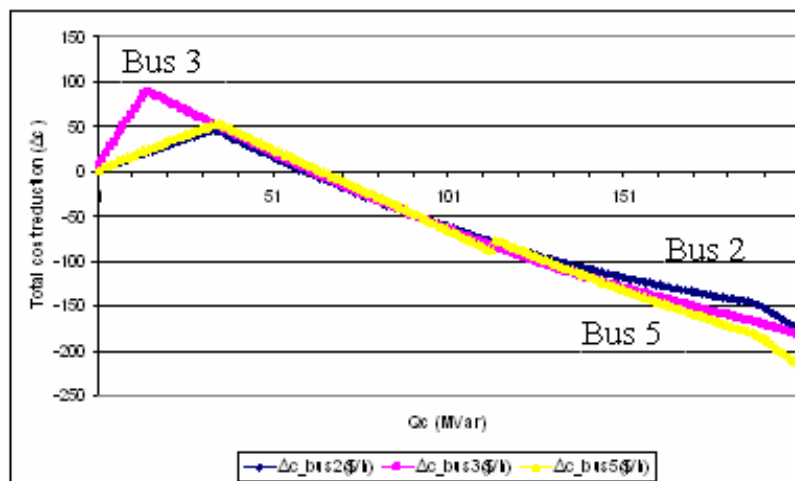
	Enumeration approach	TSV model to minimize Var cost only (TSV Model I)	TSV model to minimize fuel cost + Var cost (TSV Model II)
Running time (s)	81	0.156	0.328
Fuel cost (\$/hr)	15169.13	15515.86	15168.98
Var cost (\$/hr)	25.21	0.00	24.46
Total cost (\$/hr)	15194.34	15515.86	15193.44
Var location	Bus 3	None	Bus 3
Var size (MVar)	15	0.00	14.54
$TTC_o$ (MVA)	369.46	304.39	369.54
$TTC_*$ (MVA)	492.61	464.28	492.73
SM	25%	34%	25%



Power Engineering Laboratory

17

## Results from enumeration approach



Power Engineering Laboratory

18

## Conclusions



## Conclusions

- A review of RPP is provided.
- The results from the enumeration approach and the improved TSV model are very close. This validates the TSV model.
- The economic efficiency of Var compensation may not grow as the Var compensation amount grows.
  - It may be an economical loss if the Var size is beyond a certain range.
- The results show that the new objective function in the improved TSV model (to minimize Var cost and fuel cost) may lead to significantly different results from and is a great improvement over the model to minimize Var cost only.



## Questions and Answers?



**Power Engineering Laboratory**

21