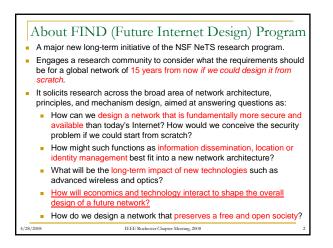
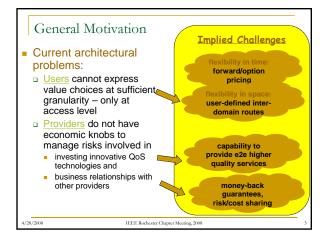
Design and Benefit Analysis of Edge-to-Edge Bailout Forward Contracts for Single-Domain Internet Services

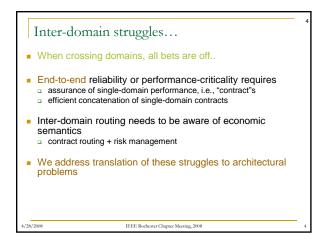
> Aparna Gupta Lally School of Management and Technology Rensselaer Polytechnic Institute Trov, NY

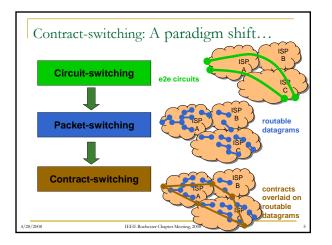
Collaboration with K.Kar, W.Liu (RPI), H.T.Karaoglu, M.Yuksel (UNR)

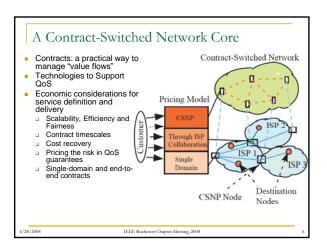
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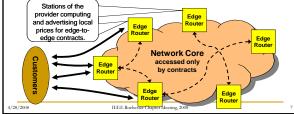


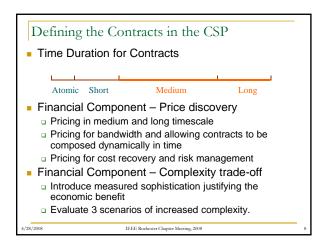






- Utilize overlay contract links between edge nodes (peering points) at domain boundaries
- To indicate wider range of service choices.
- Contracts are the building block
- Contracts include performance, financial and time duration specification









- Contracts at each edge are point-to-anywhere spot contracts
- Flat (linear) pricing scheme
- Demand profile N(p,q) Number or fraction of customers who purchase q-th unit of product at p. We choose a demand profile:

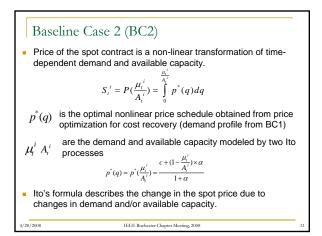
$$N(p,q) = 1 - p - q$$

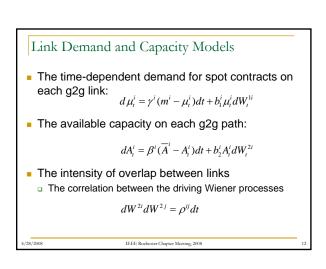
The linear spot price for point-to-anywhere at node i is:

$$B_t^i = p^* \frac{M_t^i}{A^i}$$

M is the aggregate flow through node i and A is the available capacity at node I
p* is the optimal marginal price obtained from price optimization for cost recovery for the above demand profile

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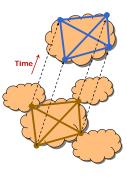




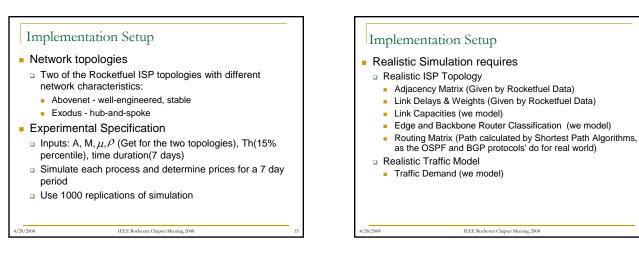


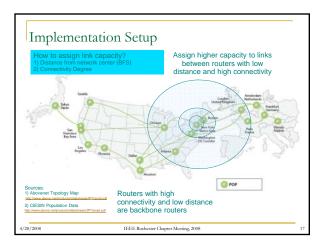
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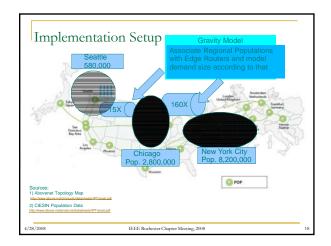
- <u>Bail-out Forwards Contracts on</u> advertisable spot contracts
 - between peering/edge points i and j of an ISP
 - flexibility of advertising different forward prices for edge-to-edge (g2g) intra-domain paths
 - forwards contracts with provision for <u>Bail-out</u> conditioned on network congestion
 - spot and forwards concatenated to create long-term contracts
 - use to realize revenue stability and guaranteed network utilization
 - tool for demand prediction and network upgrades

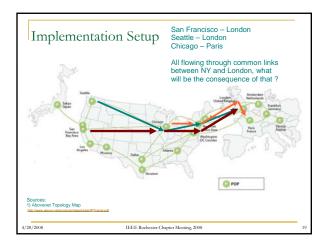


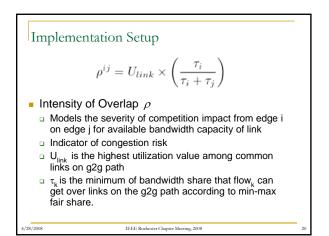
Pricing of Bailout Forward Contract (BFC) • Based on option pricing derivation, the price of the bailout forward satisfies: $\frac{\partial f^{i}}{\partial t} + \frac{1}{2}p^{2}(\frac{\mu_{i}^{l}}{A_{i}^{l}})(b_{i}^{l})^{2}(\frac{\mu_{i}^{l}}{A_{i}^{l}})^{2} + (b_{i}^{l})^{2}(A_{i}^{l})^{2})\frac{\partial^{2}f^{i}}{\partial S^{2}} + \frac{\partial f^{i}}{\partial S_{i}^{l}}rS_{i}^{i} - rf^{i} = 0$ • With the end condition: $f(S_{T}^{i}, T) = (S_{T}^{i} - F)I_{\{A_{T}^{l} > Th^{i}\}}$ • The solution is obtained as: $F = \frac{1}{P(A_{T}^{i} > Th^{i})}E[S_{T}^{i}I_{\{A_{T} > Th^{i}\}}]$ T is the time of delivery of service in future, F is the forward price, and I is the indicator function for no bailout defined in terms of a threshold level, Th.

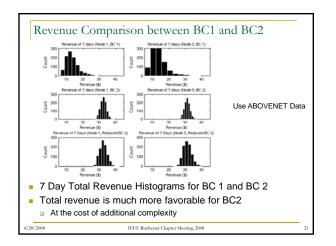


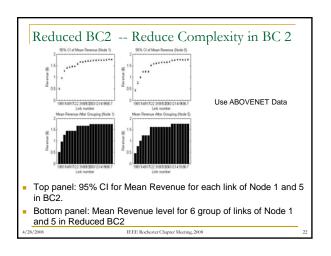


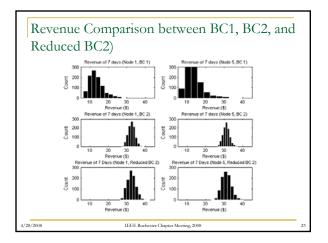


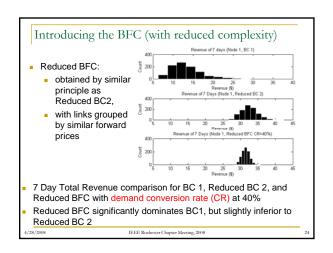


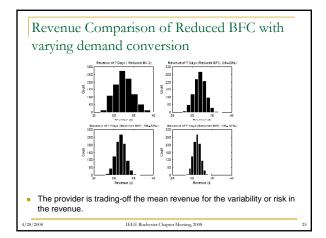


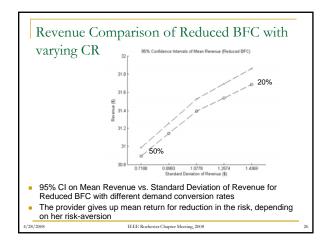


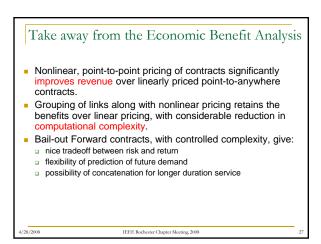


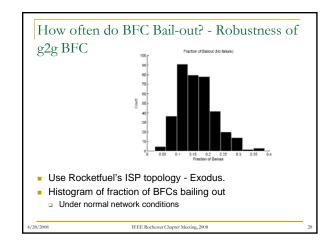


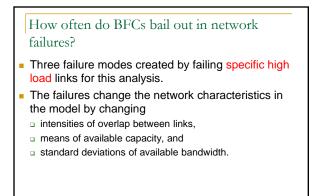




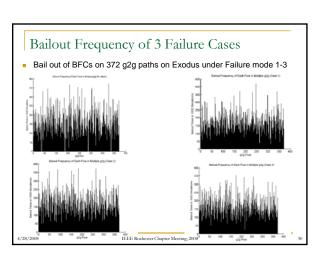








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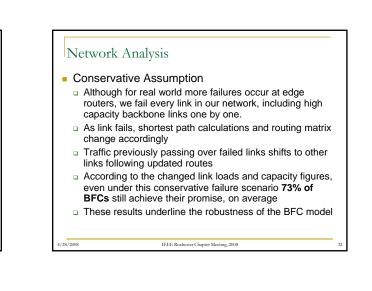


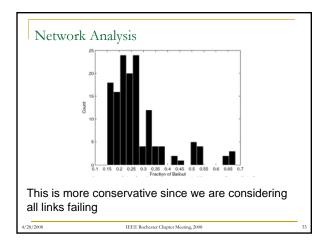
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Case	Expected Total Revenue	Mean Bailout Fraction
artificial No Bailout or Failure Case	95.7464	0
Base Case Bailout Scenario	80.43655	0.16403
Bailouts in Failure Mode 1	78.98833	0.16505355
Bailouts in Failure Mode 2	81.34074	0.163980954
Bailouts in Failure Mode 3	80.98213	0.16676308

- bailing out in the failure modes
- There is a small reduction in revenue in the failure modes IEEE Rochester Chapter Meeting, 2008

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Summary

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- Nonlinear, point-to-point pricing of contracts significantly improves revenue over linearly priced point-to-anywhere contracts.
- Grouping of links along with nonlinear pricing retains the benefits over linear pricing, with considerable reduction in computational complexity.
- Bail-out Forward contracts, with controlled complexity, give:
- nice tradeoff between risk and return flexibility of prediction of future demand possibility of concatenation for longer duration service
- Experimentations shows that the g2g BFC mechanism is robust to link failures, both in terms of the bailing out behavior and revenue lost.

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