
Bandwidth Extension Techniques for CMOS Amplifiers

David J. Allstot, Sudip Shekhar, and Jeffrey S. Walling

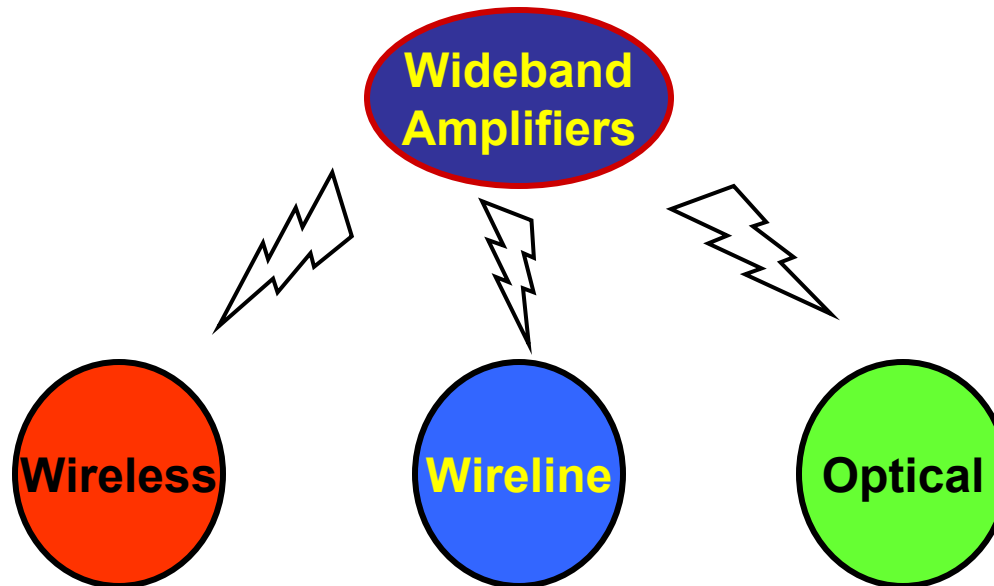
**Dept. of Electrical Engineering
University of Washington
Seattle, WA 98195-2500**

Outline

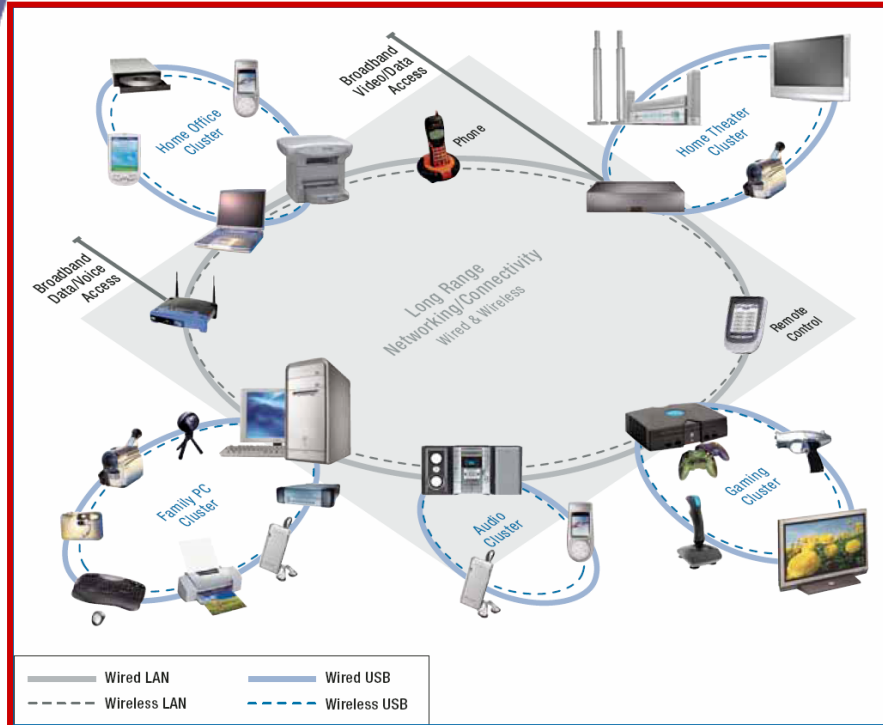
- **Motivations: Performance and Low Power**
(bandwidth $\propto g_m \propto [I]^{1/2}$, settling time, rise time)
- **Bridged-Shunt Peaking**
- **Bridged-Shunt-Series Peaking**
- **Asymmetric T-coil Peaking**
- **Wideband Amplifiers**
- **Results**
- **Conclusions**

Motivation

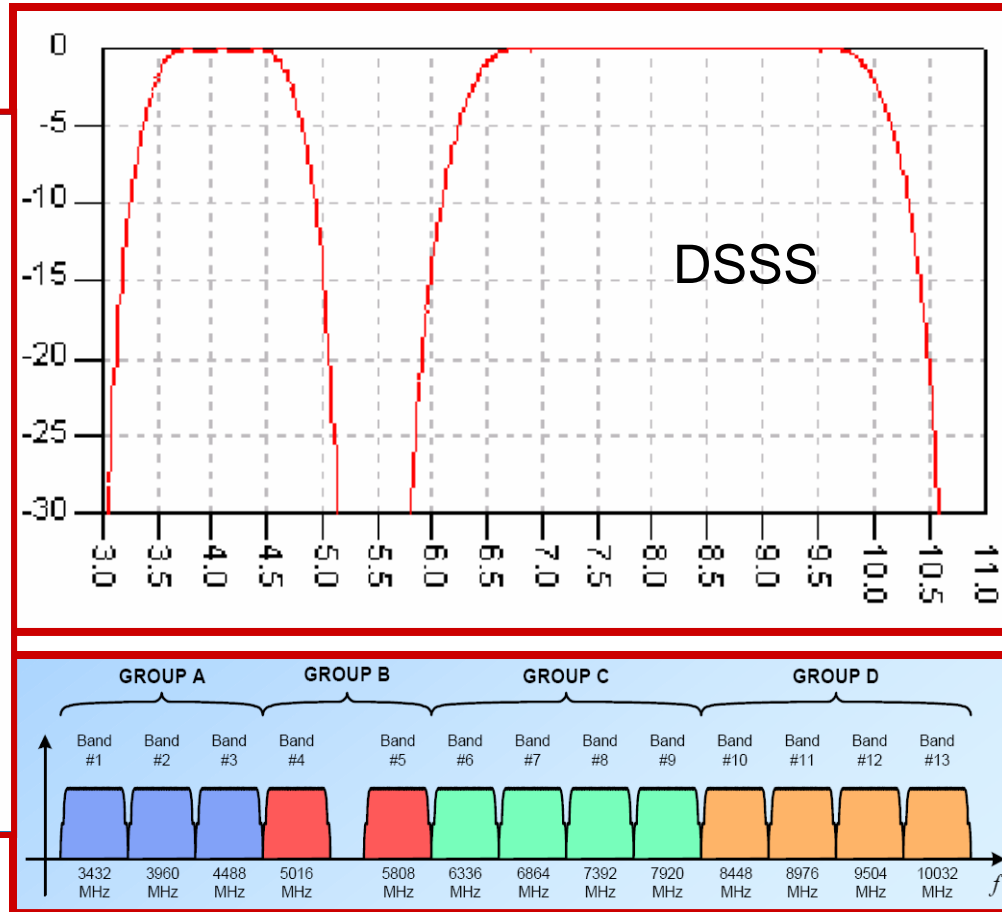
- **Broad Band Amplifiers**
- **Ultra Wideband (UWB) Receivers**
- **Transimpedance Amplifiers (TIAs)**
- **Pre-drivers and Mux/Demux**



UWB Standards

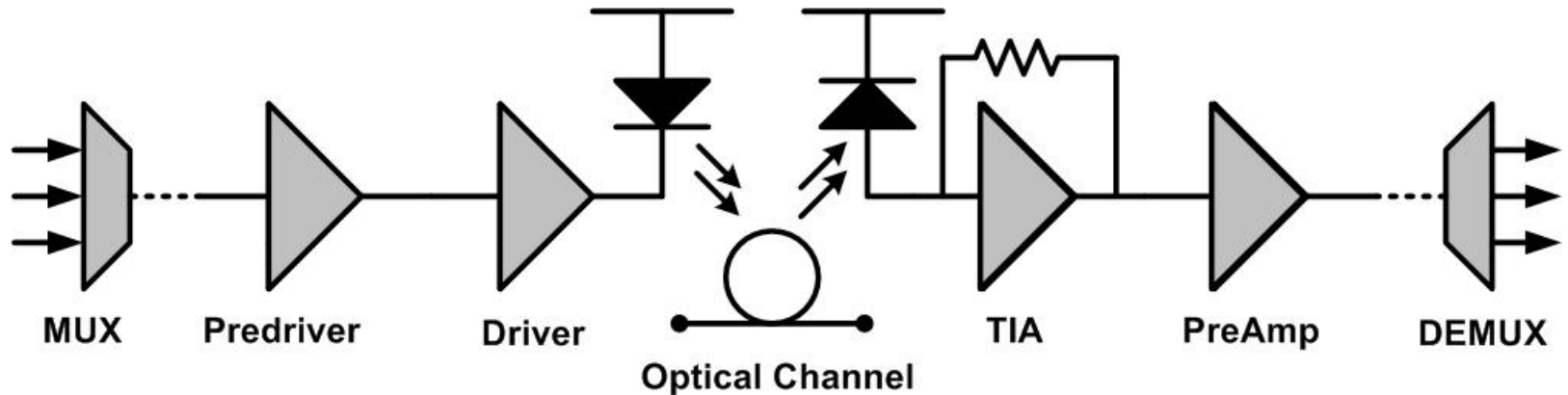


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MBOA (Multi-band OFDM Access) is supported by most of industry.
Direct Sequence Spread Spectrum (DSSS) is primarily supported by Motorola/Freescale.

Optical Communications



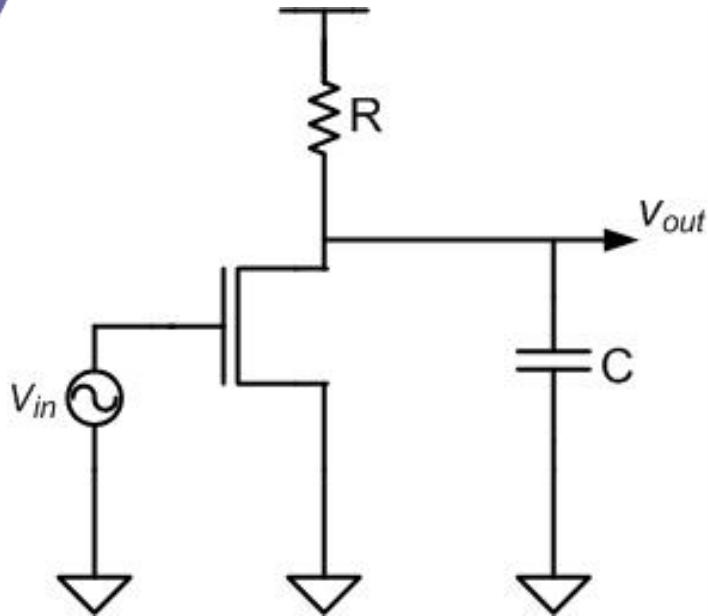
Large Bandwidth Needed ($\sim 40\text{Gb/s}$)

S. Galal and B. Razavi, "40Gb/s amplifier and ESD protection circuit in 0.18um CMOS technology," *IEEE J. Solid-State Circuits*, vol. 39, pp. 2389-2396, Dec. 2004.

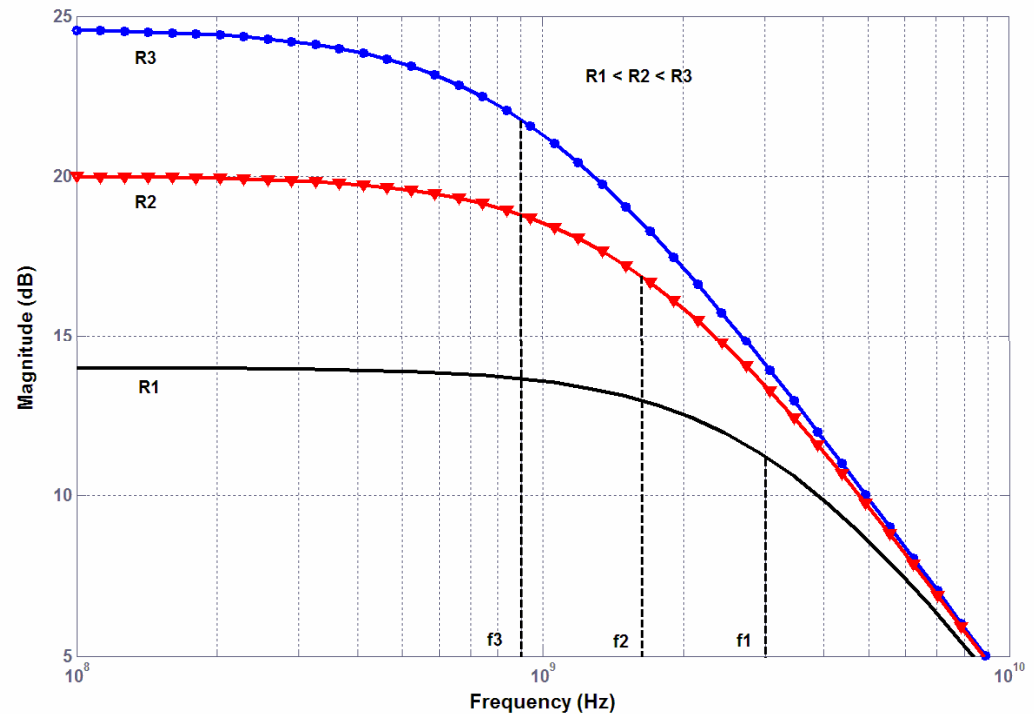
H. Wheeler, "Wide-band amplifiers for television," *Proc. of the I.R.E.*, pp. 429-438, July 1939.

F. A. Muller, "High-frequency compensation of RC amplifiers," *Proc. of the I.R.E.*, pp. 1271-1276, Aug. 1954.

Common-Source Reference Amplifier



$$A_v = \frac{V_{out}}{V_{in}} = \frac{g_m R}{1 + sRC}$$

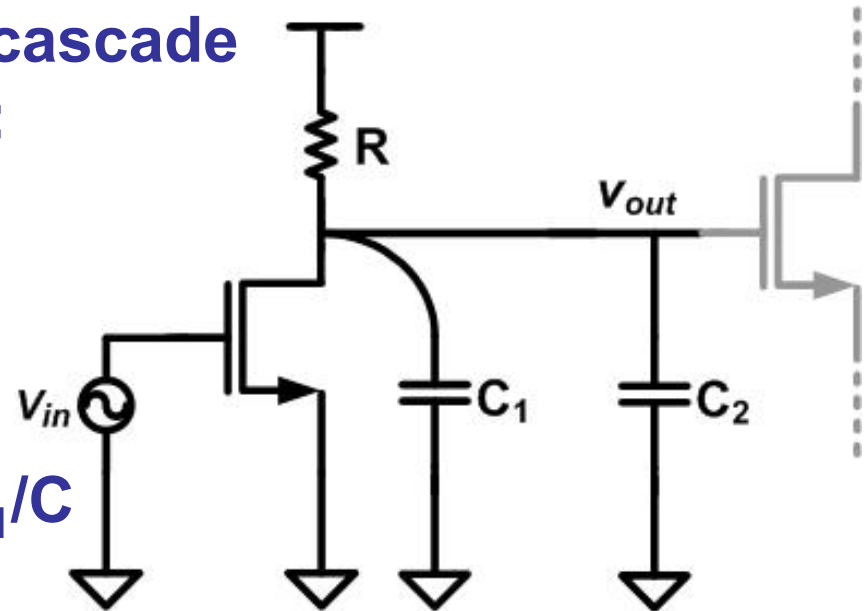


Gain-BW Tradeoff

- Desire BW extension for a given gain
- Power Dissipation Fixed for Comparison

Multi-Stage Amplifier Parasitics

- CS amplifier in multi-stage cascade
- Transistor W/L depends on:
 - Gain
 - Voltage Swing
 - Supply Current
 - Noise Figure
- Define: $k_C = C_1 / (C_1 + C_2) = C_1 / C$
 → design constraint



→ Desire BW extension for a given k_C

Peaking Techniques

Modify Conventional Peaking Techniques:

- Obtain larger BW extension ratio (BWER), smaller settling time
- Include (and exploit) parasitic effects
- Retain simplicity and generality
- Comprehensive design for different k_C values
 - Important Result: Use different techniques for different k_C values

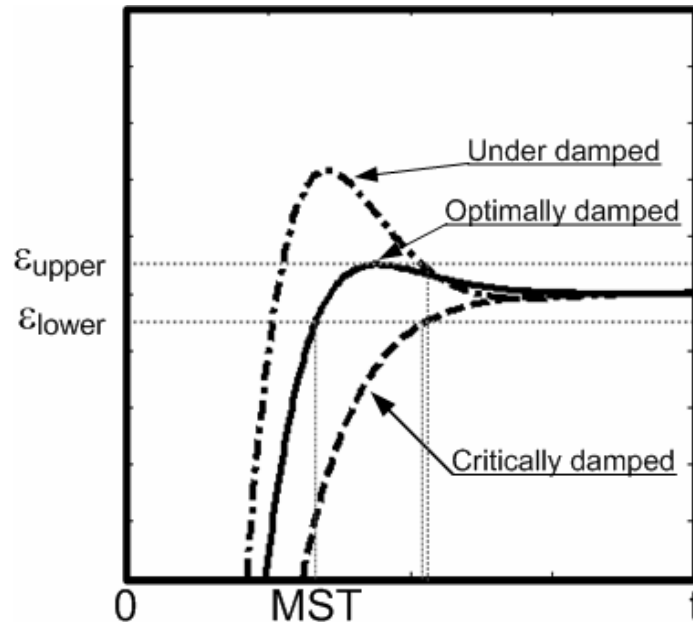
Bandwidth extension approaches:

- Resonance, capacitor splitting, magnetic coupling

Terminology

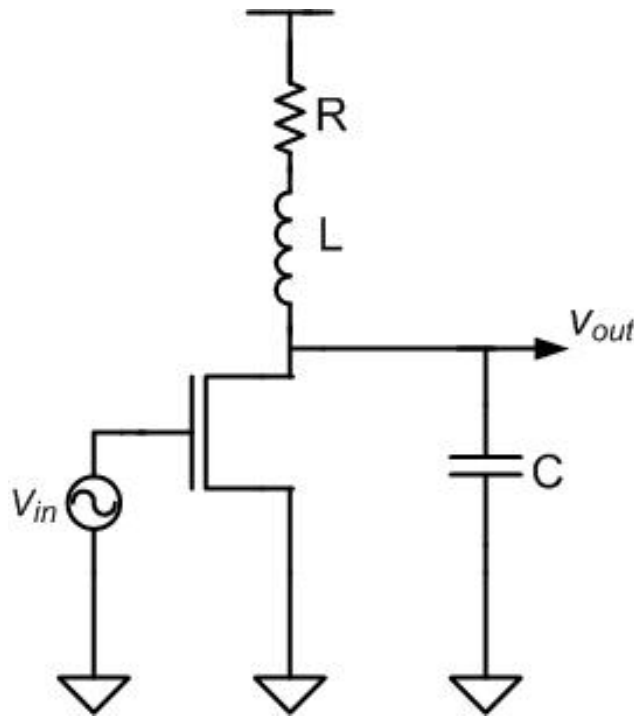
- BW extension ratio (BWER) = $f_{3dB, peak} / f_{3dB, ref}$
- Settling Time (1%) reduction ratio (STRR) = $\tau_{s, ref} / \tau_{s, peak}$
- Rise Time (10-90%) reduction ratio (RTRR) = $\tau_{r, ref} / \tau_{r, peak}$

**BWER, STRR & RTRR hard to maximize simultaneously.
Optimize for desired application.**



MST = Minimum settling Time

Conventional Shunt Peaking

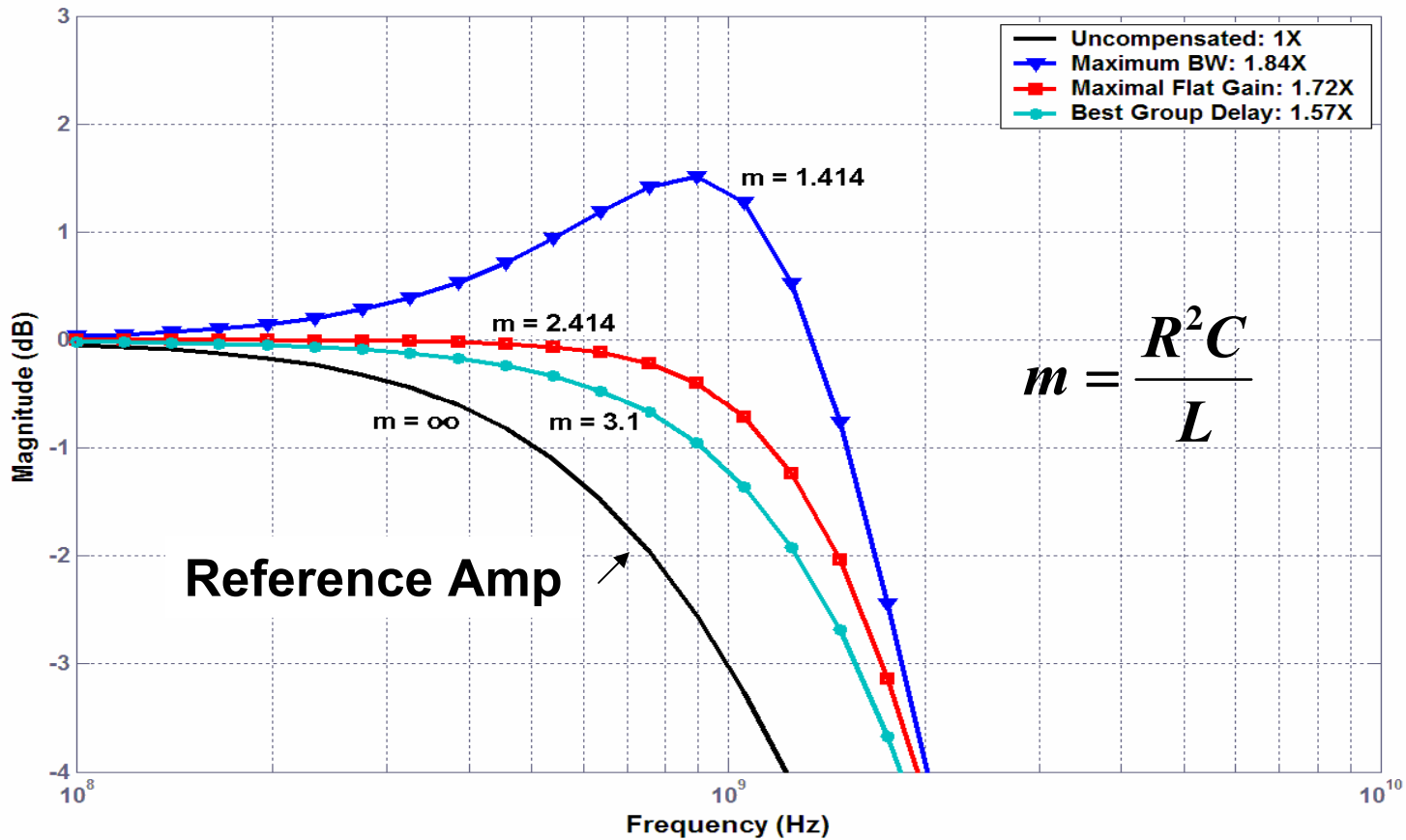


$$Z(s) = \frac{R + sL}{1 + sRC + s^2LC}$$

$$m = \frac{R^2C}{L} \quad \omega_0 = \frac{1}{RC}$$

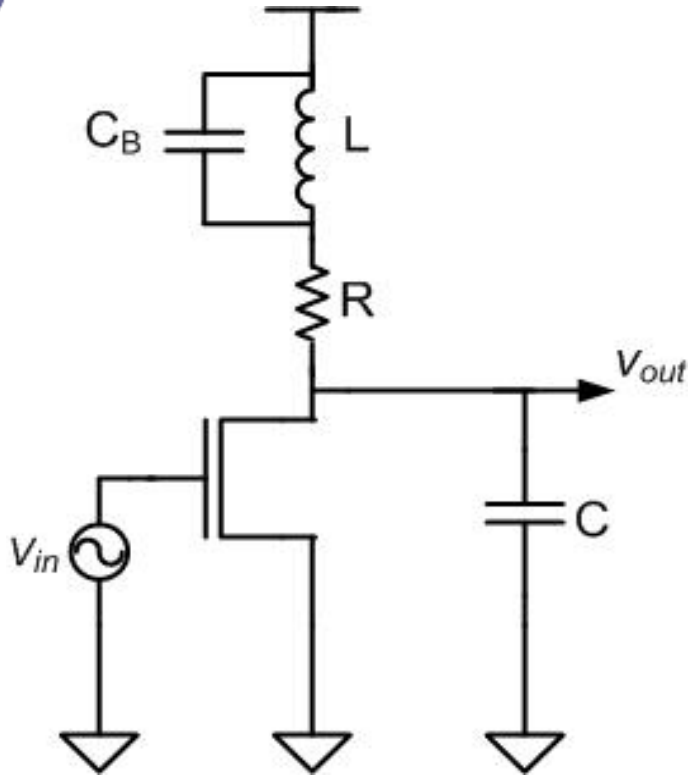
$$Z_N(s) = \frac{1 + s/m\omega_0}{1 + s/\omega_0 + s^2/m\omega_0^2}$$

Conventional Shunt Peaking - II



$m = \sqrt{2}$ **➔** 1.84X & 1.5dB Peaking

Bridged-Shunt Peaking



$$Z_N(s) = \frac{1 + \left(\frac{1}{m}\right) \frac{s}{\omega_0} + \left(\frac{k_B}{m}\right) \frac{s^2}{\omega_0^2}}{1 + \frac{s}{\omega_0} + \left(\frac{k_B + 1}{m}\right) \frac{s^2}{\omega_0^2} + \left(\frac{k_B}{m}\right) \frac{s^3}{\omega_0^3}}$$

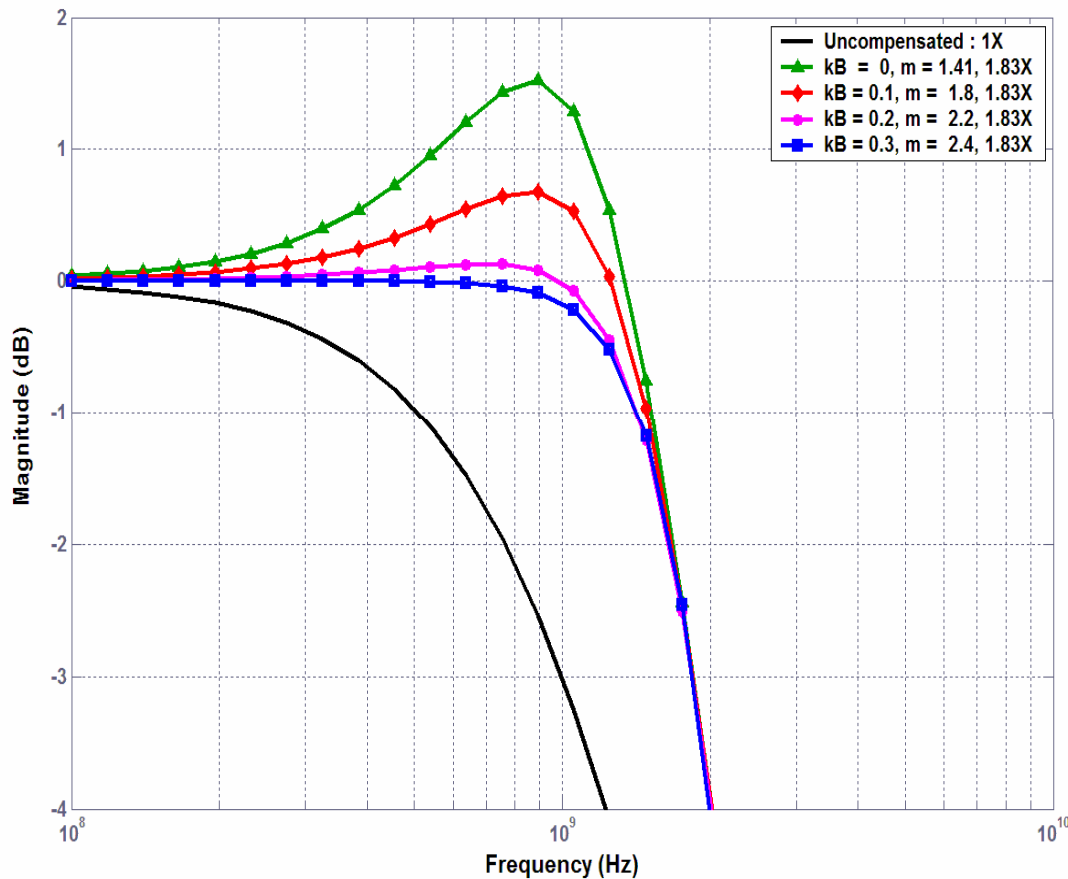
↑

$$m = \frac{R^2 C}{L} \quad \omega_0 = \frac{1}{RC} \quad k_B = \frac{C_B}{C}$$

$$Z_N(s) = \frac{1 + s / m \omega_0}{1 + s / \omega_0 + s^2 / m \omega_0^2}$$

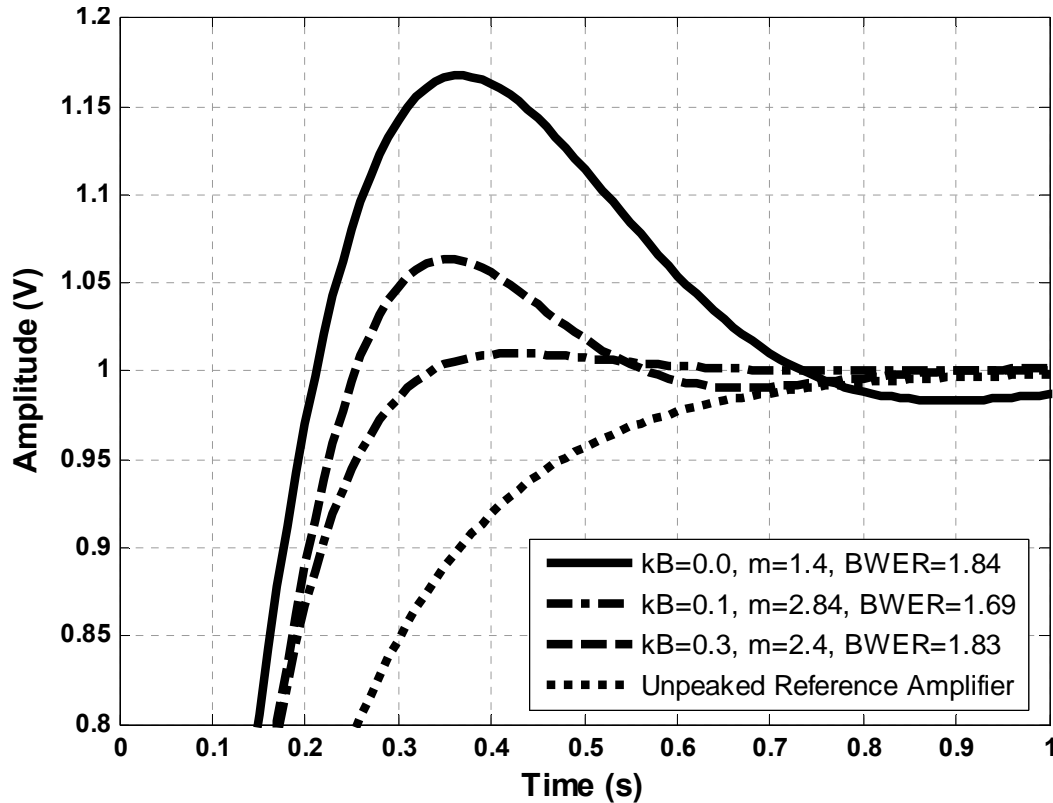
Note: Inductor parasitic forms C_B
Question: Interchange L and R ?

Bridged-Shunt Peaking



$m = 2.4, k_B = 0.3$ \longrightarrow 1.83X and flat gain

Bridged-Shunt Peaking - II



Optimum Depends On Application



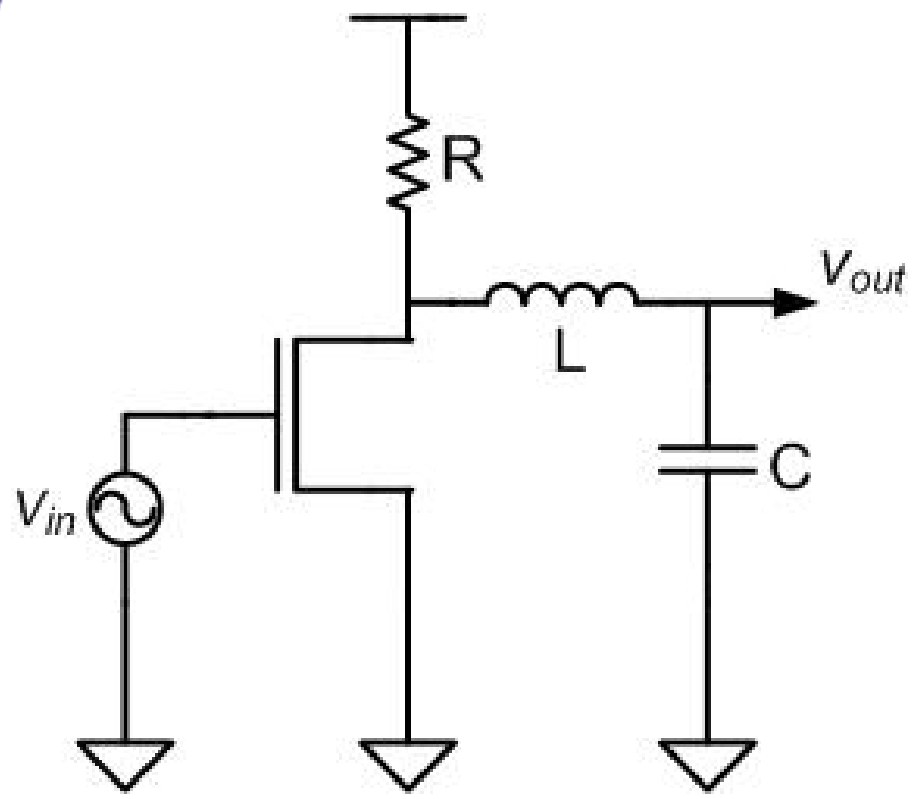
| K_B | m | <i>STRR</i> | <i>RTRR</i> | <i>BWER</i> |
|-------|------|-------------|-------------|-------------|
| 0.0 | 1.4 | 0.70 | 2.18 | 1.84 |
| 0.1 | 2.84 | 2.40 | 1.74 | 1.69 |
| 0.3 | 2.4 | 1.39 | 1.87 | 1.83 |

Bridged-Shunt Peaking

Advantages☺


- Incorporates inductor parasitics (Add more C_B if needed)
- ✓ Maximum BW possible with flat gain (No 1.5dB peaking)
- ✓ $m \uparrow == L \downarrow \rightarrow$ Smaller Area
- ✓ Area overhead for added C_B minimal

Conventional Series Peaking

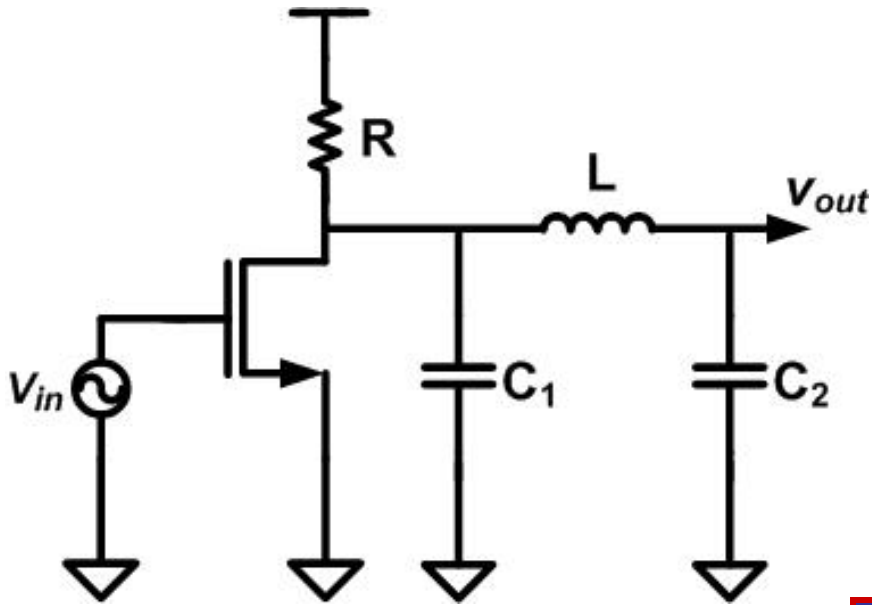


$$Z_N(s) = \frac{1}{1 + s/\omega_0 + s^2/m\omega_0^2}$$

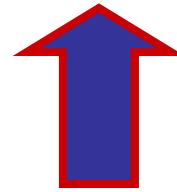
- Lack of Zero
- Inferior to Shunt peaking

m = 2  **1.41X**

Series Peaking with Drain Parasitics



$$Z_N(s) = \frac{1}{1 + \frac{s}{\omega_0} + \left(\frac{1-k_C}{m}\right)\frac{s^2}{\omega_0^2} + \left(\frac{k_C(1-k_C)}{m}\right)\frac{s^3}{\omega_0^3}}$$

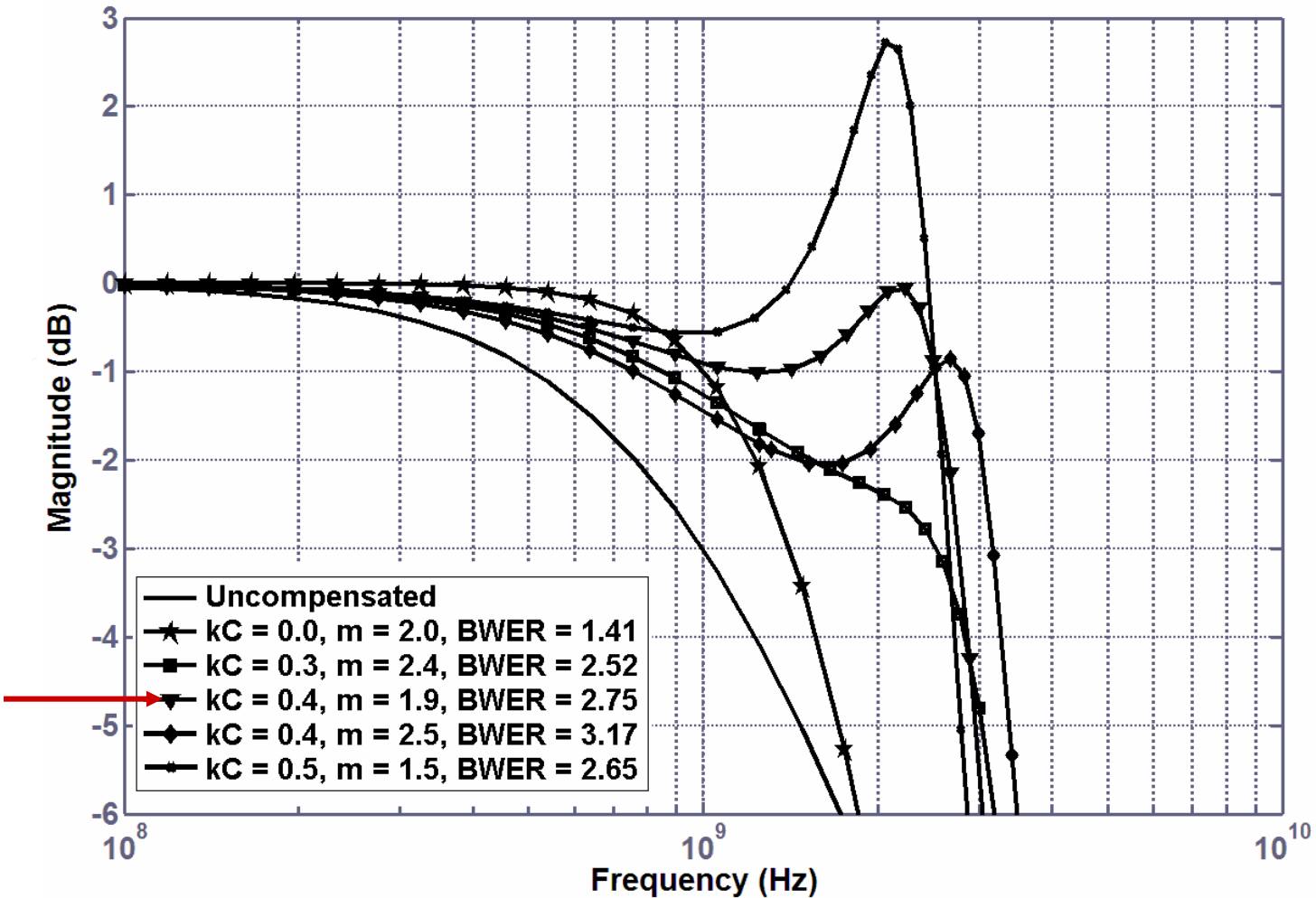


$$k_C = \frac{C_1}{C}$$

$$Z_N(s) = \frac{1}{1 + s/\omega_0 + s^2/m\omega_0^2}$$

**Conventional Series Peaking
Capacitor Splitting Idea**

Series Peaking vs. k_C

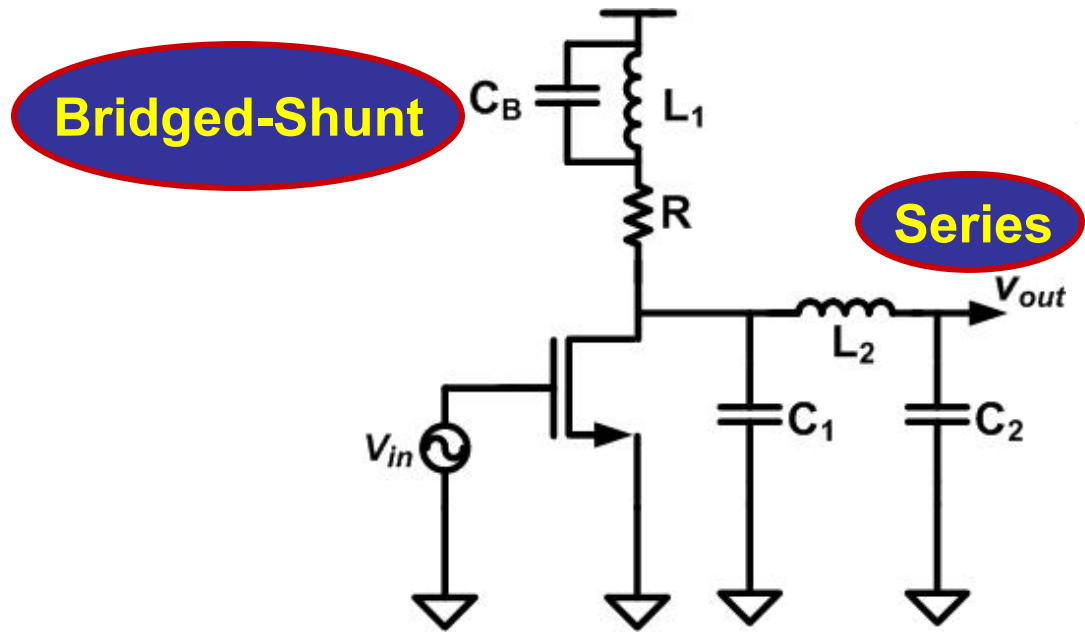


Series Peaking with C_1 : Summary

| $k_C = C_1/C$ | Peaking (dB) | $m = R^2 C/L$ | BWER |
|---------------|--------------|---------------|------|
| 0 | 0 | 2 | 1.41 |
| 0.1 | 0 | 1.8 | 1.58 |
| 0.2 | 0 | 1.8 | 1.87 |
| 0.3 | 0 | 2.4 | 2.52 |
| 0.4 | 1 | 1.9 | 2.75 |
| | 2 | 2.5 | 3.17 |
| 0.5* | 3.3 | 1.5 | 2.65 |

* B. Analui and A. Hajimiri, "Bandwidth enhancement for transimpedance amplifiers," *IEEE J. Solid-State Circuits*, vol. 39, pp. 1263-1270, Aug. 2004.

Bridged-Shunt-Series Peaking



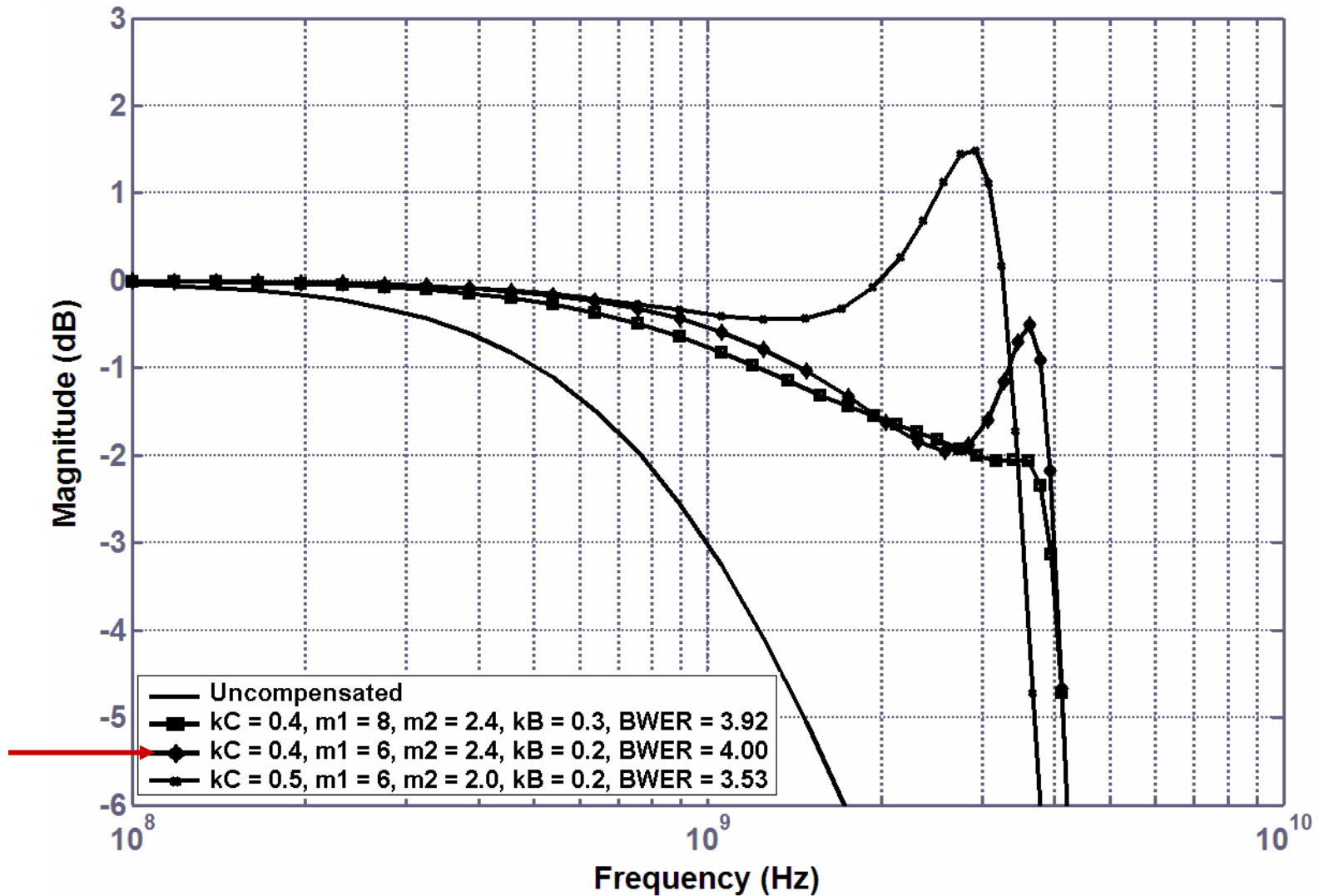
Bridged-Shunt

Series

$$1 + \left(\frac{1}{m_1}\right) \frac{s}{\omega_0} + \left(\frac{k_B}{m_1}\right) \frac{s^2}{\omega_0^2}$$

$$Z_N(s) = \frac{1 + \left(\frac{1}{m_1}\right) \frac{s}{\omega_0} + \left(\frac{k_B}{m_1}\right) \frac{s^2}{\omega_0^2}}{1 + \frac{s}{\omega_0} + \left(\frac{1+k_B}{m_1} + \frac{1-k_C}{m_2}\right) \frac{s^2}{\omega_0^2} + \left(\frac{k_B}{m_1} + \frac{k_C(1-k_C)}{m_2}\right) \frac{s^3}{\omega_0^3} + \left(\frac{(k_C+k_B)(1-k_C)}{m_1 m_2}\right) \frac{s^4}{\omega_0^4} + \left(\frac{k_B k_C(1-k_C)}{m_1 m_2}\right) \frac{s^5}{\omega_0^5}}$$

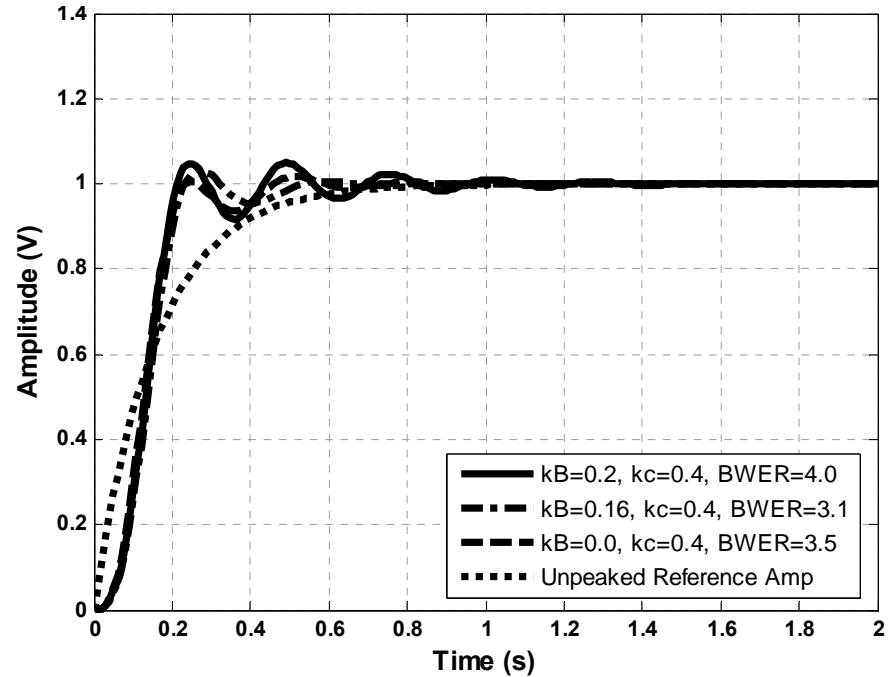
Bridged-Shunt-Series Peaking - II



Bridged-Shunt-Series Summary - I

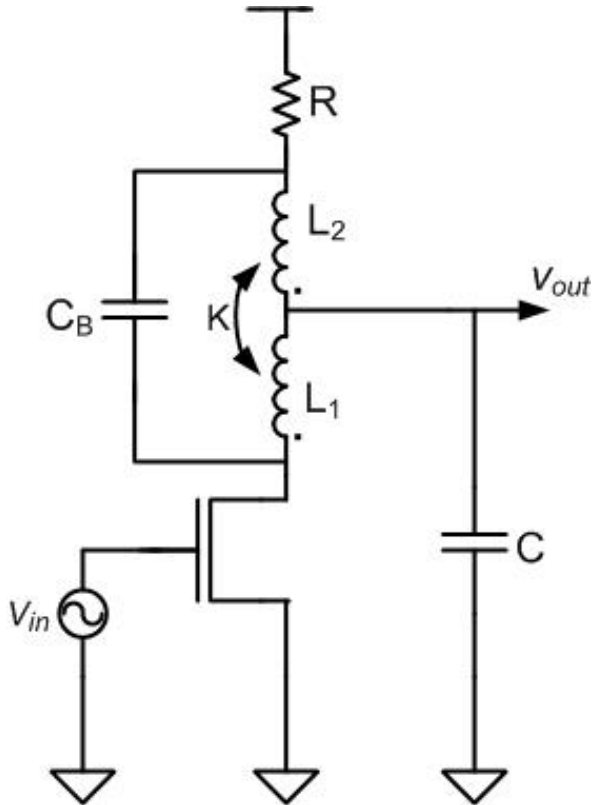
| $k_C = C_1/C$ | Peak (dB) | $m_1 = R^2 C/L_1$ | $m_2 = R^2 C/L_2$ | $k_B = C_B/C$ | BWER |
|---------------|-----------|-------------------|-------------------|---------------|------|
| 0.4 | 0 | 8 | 2.4 | 0.3 | 3.92 |
| | 2 | 6 | 2.4 | 0.2 | 4 |
| 0.5 | 2 | 6 | 2 | 0.2 | 3.53 |

Bridged-Shunt-Series Summary - II



| k_C | k_B | m_1 | m_2 | <i>STRR</i> | <i>RTRR</i> | <i>BWER</i> |
|-------|-------|-------|-------|-------------|-------------|-------------|
| 0.4 | 0.0 | 6.3 | 2.6 | 1.32 | 2.73 | 3.47 |
| | 0.16 | 8 | 2.2 | 1.46 | 2.78 | 3.11 |
| | 0.2 | 6 | 2.4 | 0.71 | 2.89 | 4.00 |
| | 0.3 | 8 | 2.4 | 0.95 | 2.66 | 3.92 |
| 0.5 | 0.1 | 6 | 2 | 0.75 | 2.91 | 3.40 |
| | 0.2 | 6 | 2 | 0.77 | 2.88 | 3.53 |

Conventional Bridged T-Coil Peaking



$$Z_N(s) = \frac{1}{1 + (s/\omega_n)2\zeta + s^2/\omega_n^2}$$

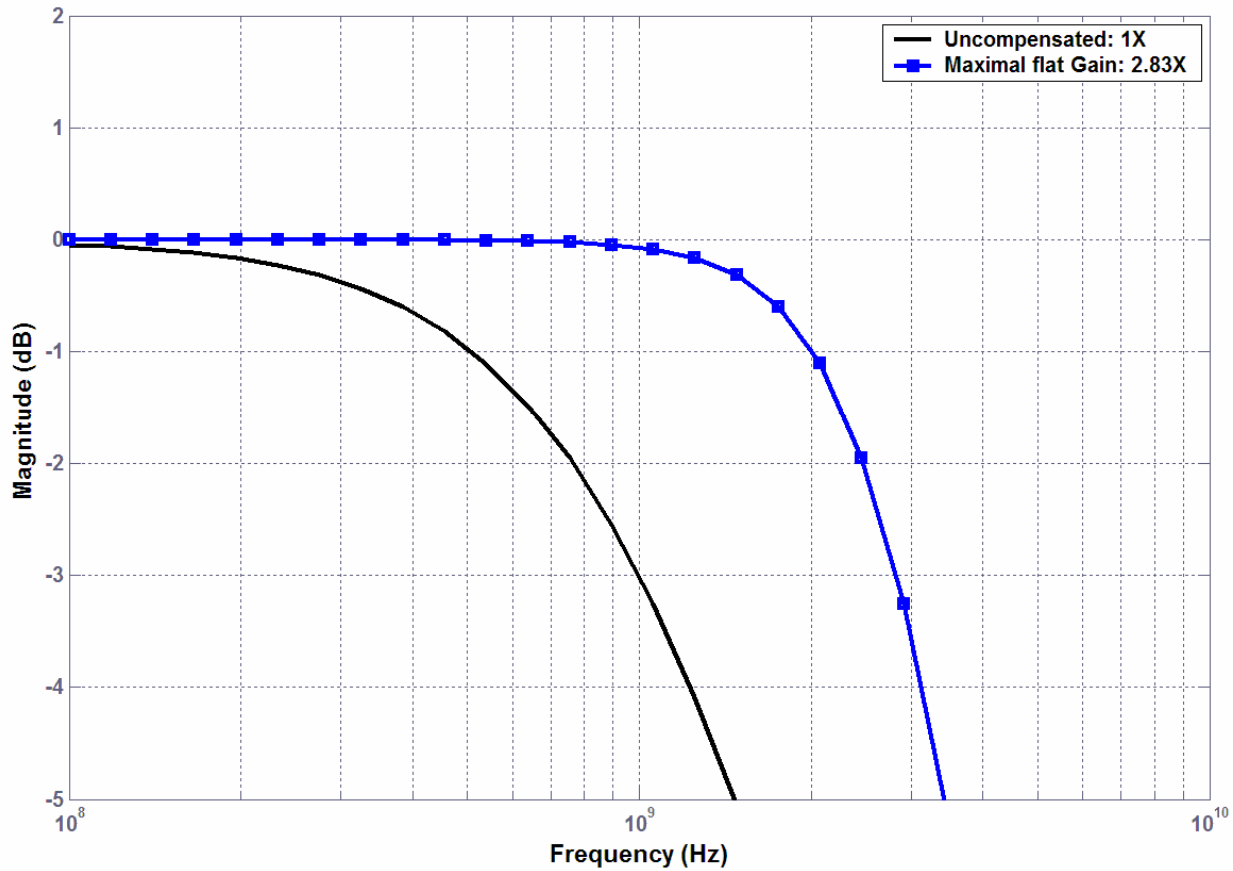
- $L_1 = L_2$
- Butterworth response
- Double shunt-series peaking

$\zeta = 1/\sqrt{2}$ $k = -1/3$ **→** **2.83X**

Capacitor Splitting + Magnetic Coupling

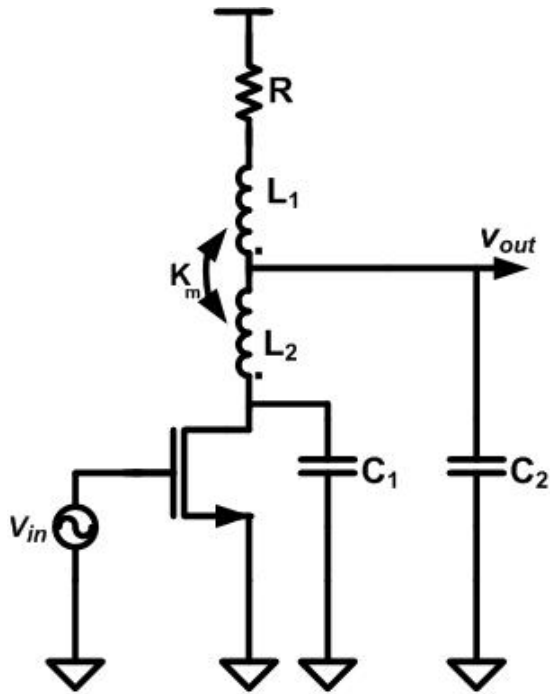
B. Hofer, *Amplifier Frequency and Transient Response (AFTR) Notes*: Tektronix, Inc. , 1982.
 Original notes from Carl Battjes. Tektronix used package lead inductors to implement T-coils circa 1970.

Conventional Bridged T-Coil Peaking-II



$\zeta = 1/\sqrt{2}$ $k = -1/3$ **→** **2.83X**

Asymmetric T-Coil Peaking - 1

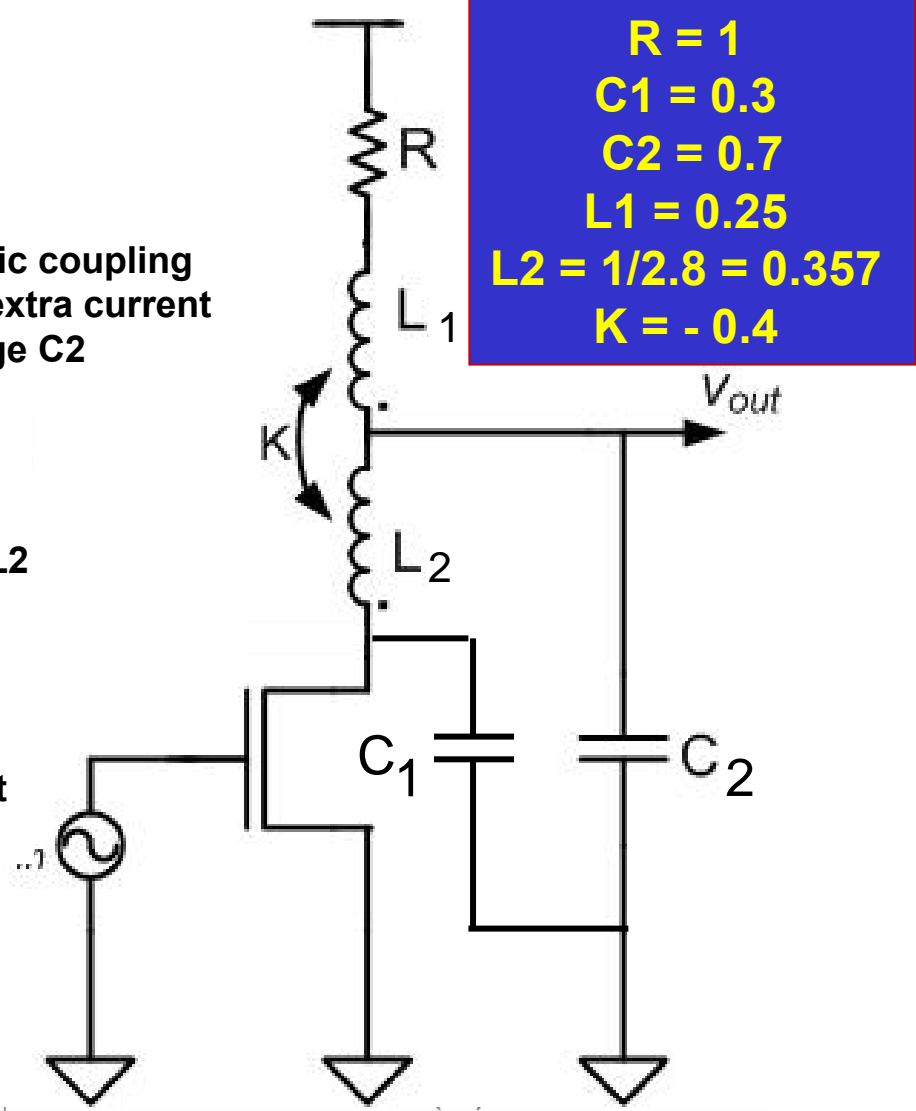
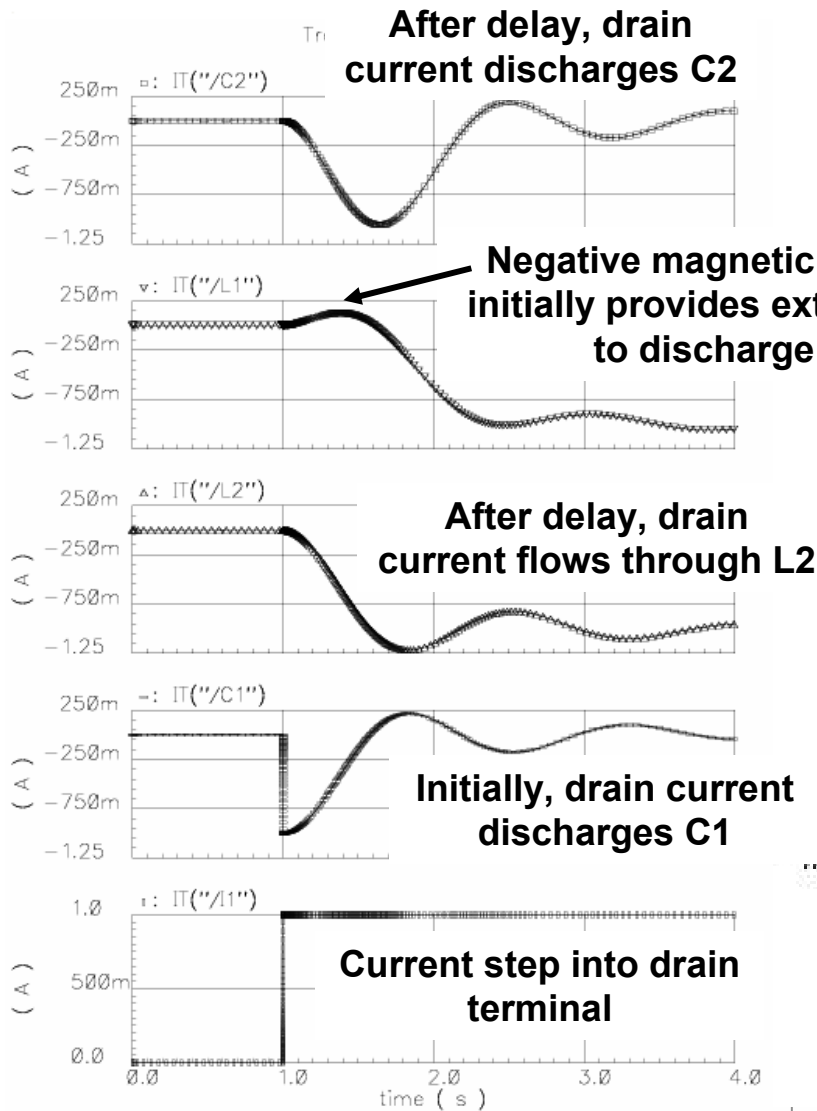


$$k_c = \frac{C_1}{C}$$

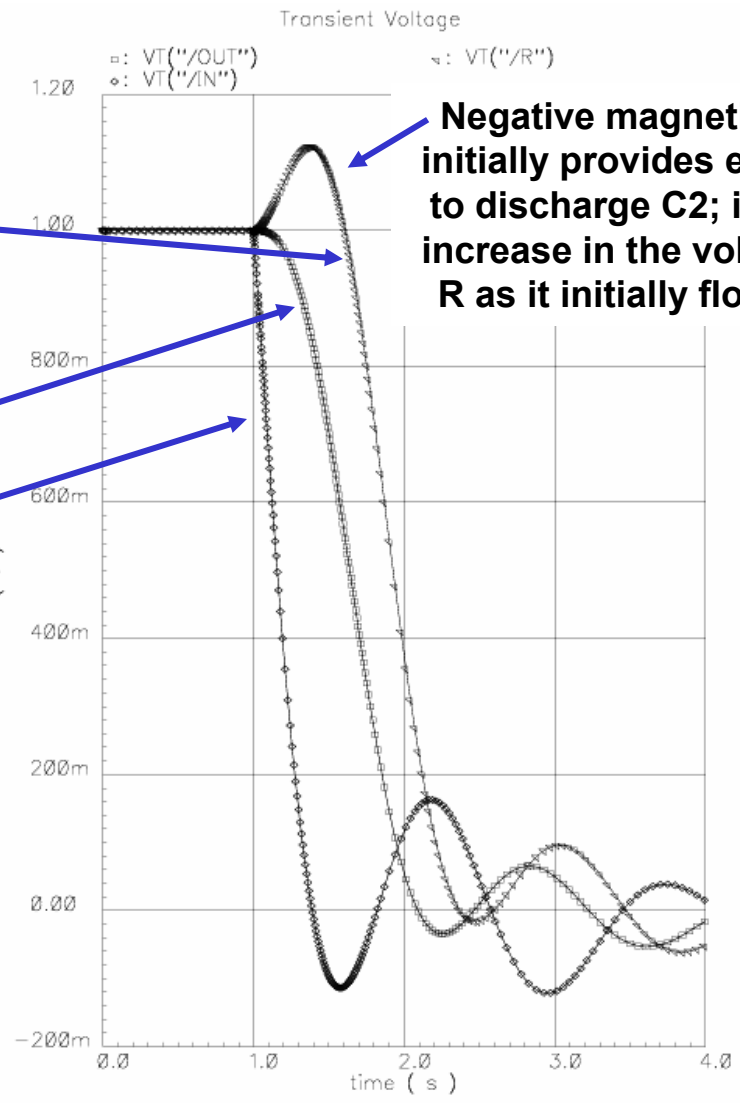
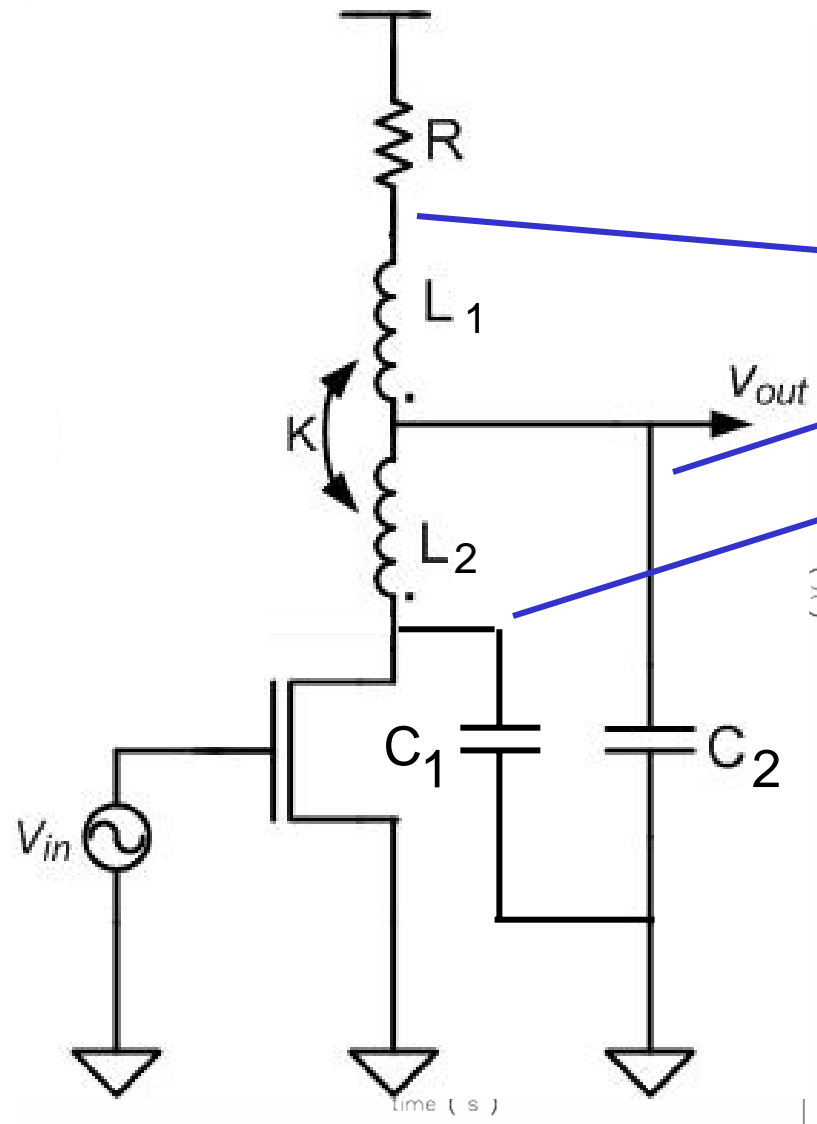
$$k_m = M / \sqrt{L_1 L_2}$$

$$Z_N(s) = \frac{1 + \left(\frac{1}{m_1} + \frac{k_m}{\sqrt{m_1 m_2}} \right) \frac{s}{\omega_0}}{1 + \frac{s}{\omega_0} + \left(\frac{1}{m_1} + \frac{k_c}{m_2} + \frac{2k_c k_m}{\sqrt{m_1 m_2}} \right) \frac{s^2}{\omega_0^2} + \left(\frac{k_c(1 - k_c)}{m_2} \right) \frac{s^3}{\omega_0^3} + \left(\frac{k_c(1 - k_c)(1 - k_m^2)}{m_1 m_2} \right) \frac{s^4}{\omega_0^4}}$$

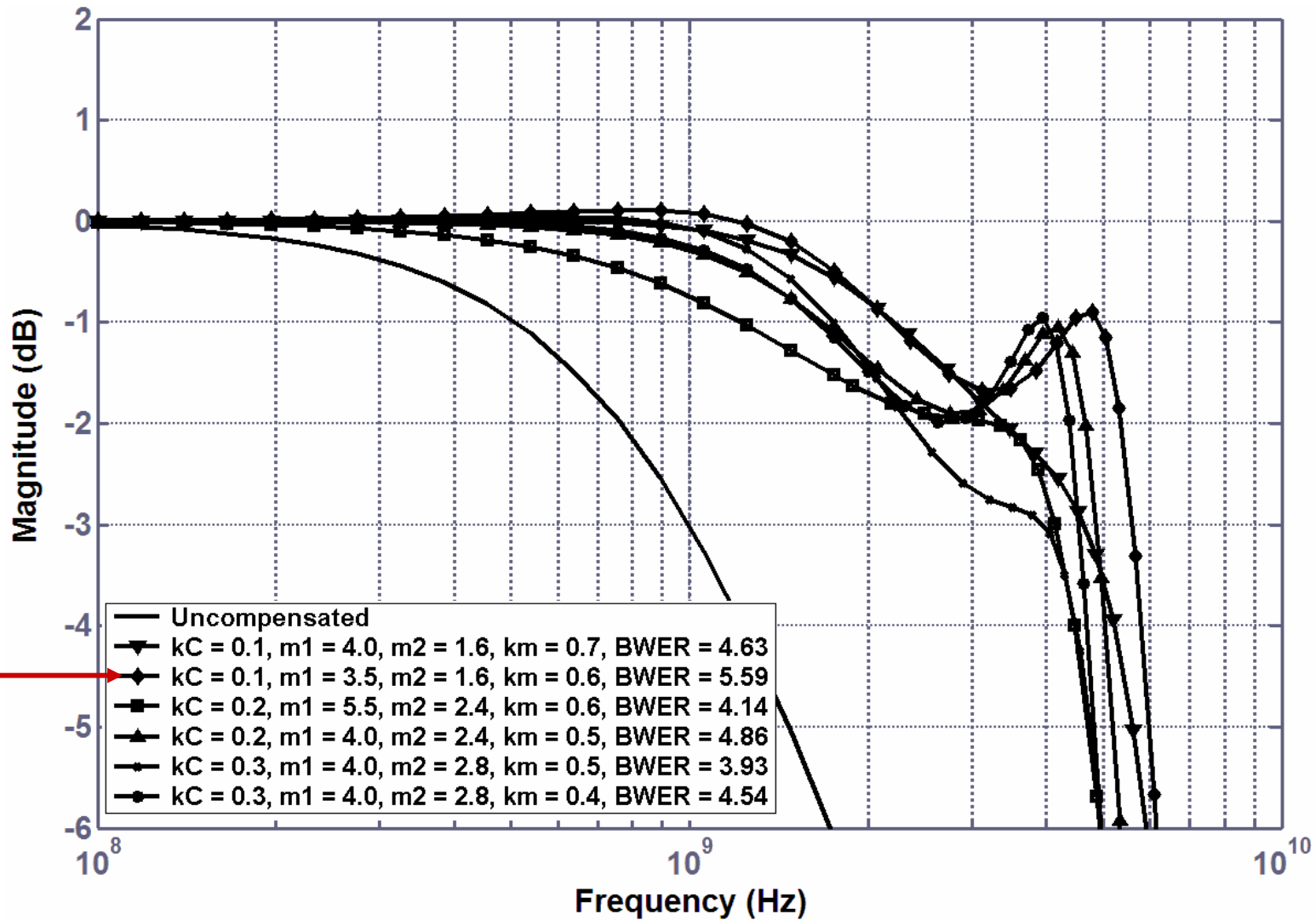
Asymmetric T-Coil Peaking - 2



Asymmetric T-Coil Peaking - 3



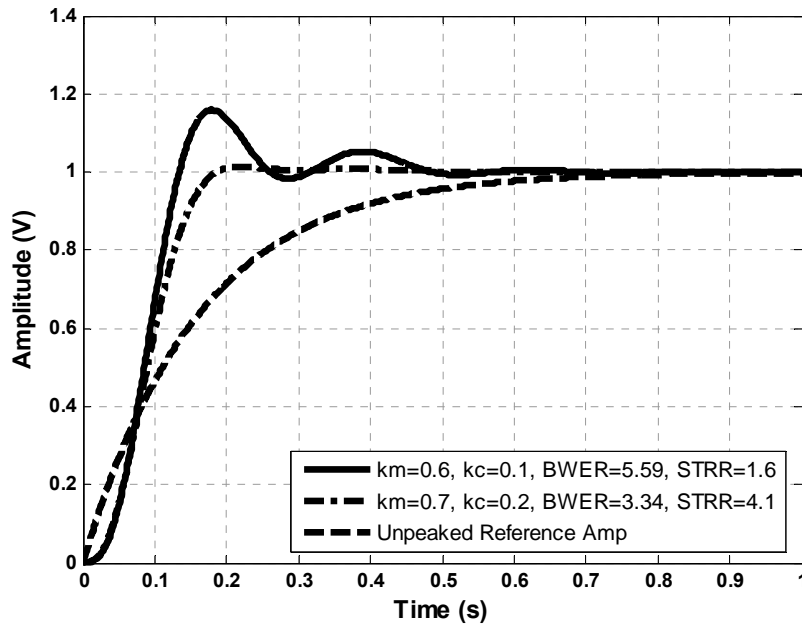
Asymmetric T-Coil Peaking - 4



Asymmetric T-Coil Summary - I

| $k_C = C_1/C$ | Peak (dB) | $m_1 = R^2 C/L_1$ | $m_2 = R^2 C/L_2$ | $k_m = M/\sqrt{L_1 L_2}$ | BWER |
|---------------|-----------|-------------------|-------------------|--------------------------|------|
| 0.1 | 0 | 4 | 1.6 | -0.7 | 4.63 |
| | 1 | 3.5 | 1.2 | -0.6 | 4.92 |
| | 2 | 3.5 | 1.6 | -0.6 | 5.59 |
| 0.2 | 0 | 5.5 | 2.4 | -0.6 | 4.14 |
| | 1 | 3 | 2 | -0.6 | 4.51 |
| | 2 | 4 | 2.4 | -0.5 | 4.86 |
| 0.3 | 0 | 4 | 2.8 | -0.5 | 3.93 |
| | 1 | 3.5 | 2 | -0.4 | 3.98 |
| | 2 | 4 | 2.8 | -0.4 | 4.54 |

Asymmetric T-Coil Summary - II

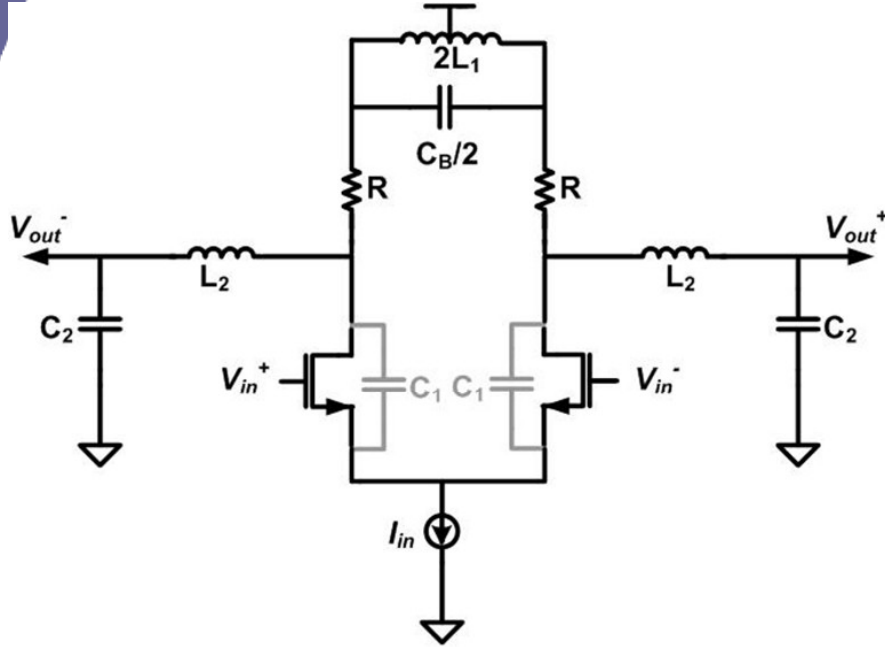


| k_C | k_m | m_1 | m_2 | STRR | RTRR | BWER |
|-------|-------|-------|-------|------|------|------|
| 0.1 | 0.7 | 4.0 | 1.6 | 1.90 | 4.20 | 4.63 |
| | 0.6 | 3.5 | 1.6 | 1.32 | 4.50 | 4.92 |
| | 0.6 | 3.5 | 1.2 | 1.57 | 4.43 | 5.59 |
| | 0.7 | 4.1 | 1.6 | 2.91 | 4.19 | 4.66 |
| 0.2 | 0.6 | 5.5 | 2.4 | 1.94 | 3.39 | 4.14 |
| | 0.6 | 3.0 | 2.0 | 1.23 | 3.91 | 4.51 |
| | 0.5 | 4.0 | 2.4 | 1.42 | 3.80 | 4.86 |
| | 0.7 | 4.6 | 2.2 | 4.11 | 3.35 | 3.34 |
| 0.3 | 0.5 | 4.0 | 2.8 | 1.54 | 3.40 | 3.93 |
| | 0.4 | 3.5 | 2.0 | 1.09 | 3.45 | 3.98 |
| | 0.4 | 4.0 | 2.8 | 1.10 | 3.52 | 4.54 |
| | 0.6 | 5.0 | 2.6 | 3.70 | 3.06 | 3.07 |

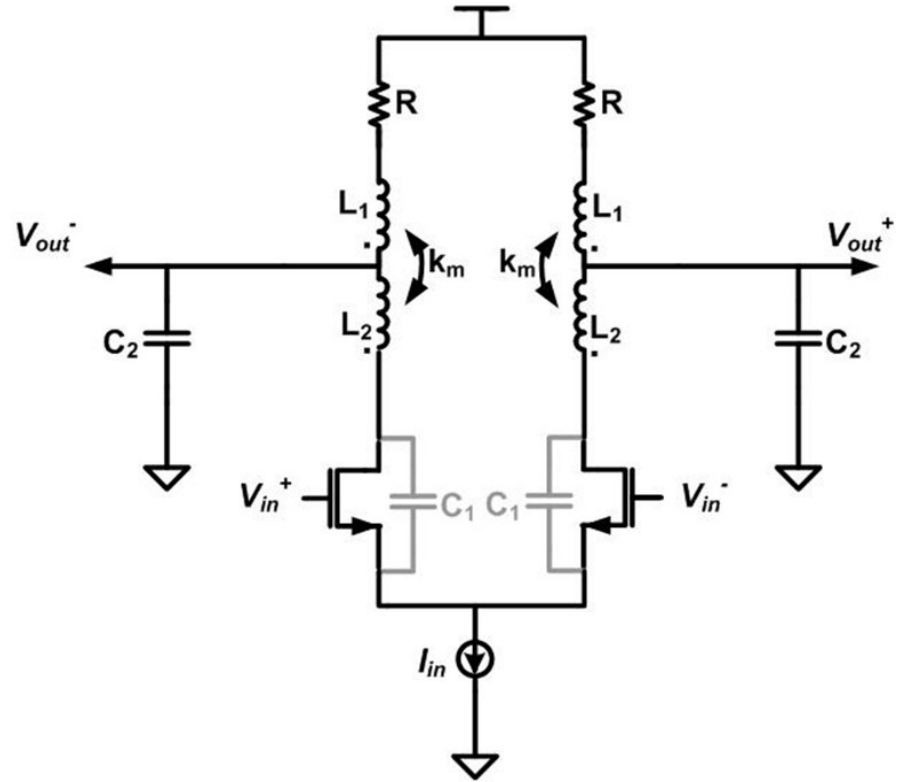
Peaking Techniques: Summary

| k_C | Desired BWER | Desired STRR (1%) | Optimal Peaking Method |
|---------|--------------|-------------------|------------------------|
| 0.1-0.5 | <1.83 | <2.4 | Bridged Shunt |
| 0.1-0.4 | 3-5.59 | <4.1 | Asymmetric T-coil |
| 0.4-0.5 | 3-4 | <1.5 | Bridged-Shunt-Series |

Prototype Amplifiers



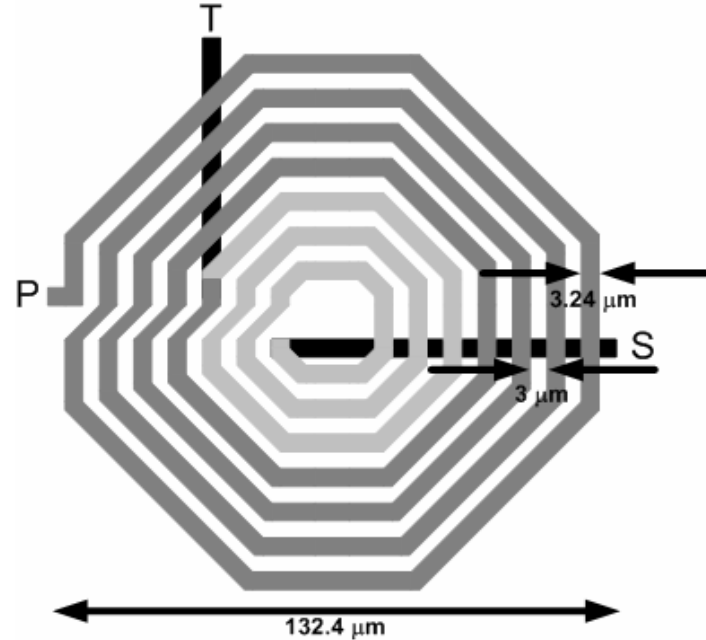
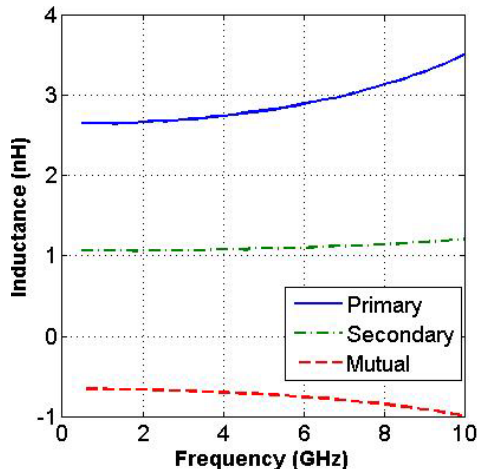
Bridged-Shunt-Series
 $k_C = 0.4, 0.5$
 Gain = 14dB
 BW = 8GHz



Asymmetric T-Coil
 $k_C = 0.3$
 Gain = 12dB
 BW = 10.4GHz

Asymmetric T-coil

- T-coil needs weak-coupling
→ $k_m \sim 0.4$
- Simplicity, weak-coupling
→ concentric-windings
- Two-pronged design method
→ reduced design cycle
 1. Grover Calculations
 2. EM Simulation

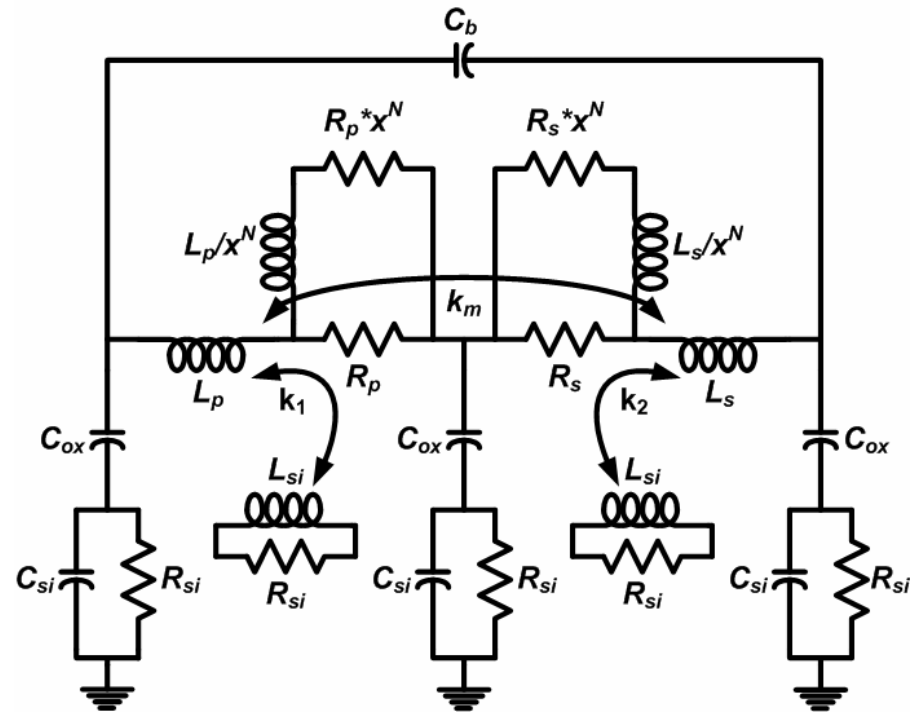


| | |
|-----------------------------|----------------|
| Spacing: | 3 μm |
| Outer Diameter: | 132 μm |
| Inner Diameter: | 51 μm |
| Width: | 3.24 μm |
| Top metal thickness: | 2 μm |

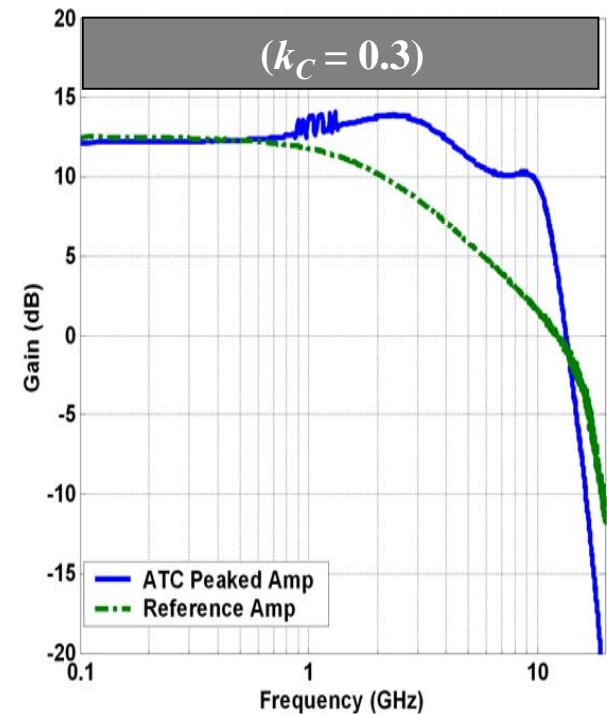
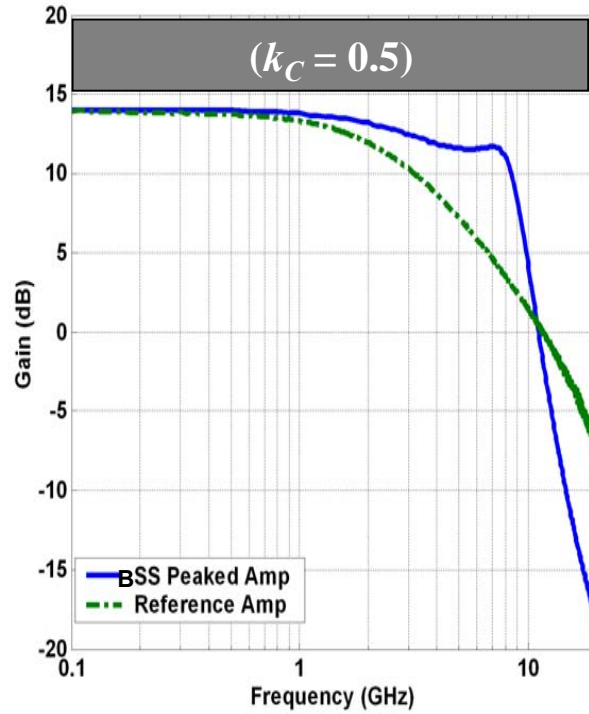
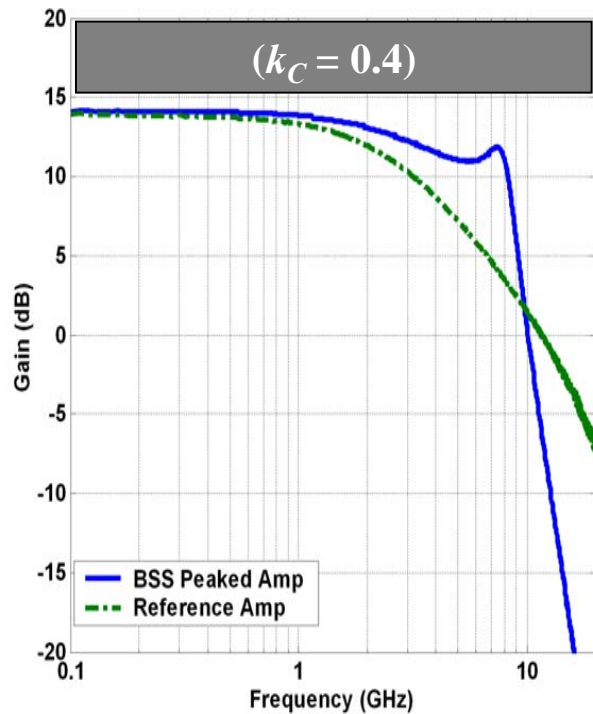
F. W. Grover, *Inductance Calculations: Working Formulas and Tables*. New York: D. Van Nostrand Company, Inc., 1946.

Asymmetric T-coil - II

- T-coil EM simulation
 - freq. domain representation
- Transient simulation needs circuit model
- Proposed equivalent wideband circuit model
 - incorporates skin-effect, bulk-eddy currents
- Good to first self-resonance



Measurement Results



Bridge Shunt-Series
Gain = 14dB
BW = 8GHz
BWER = 3.0

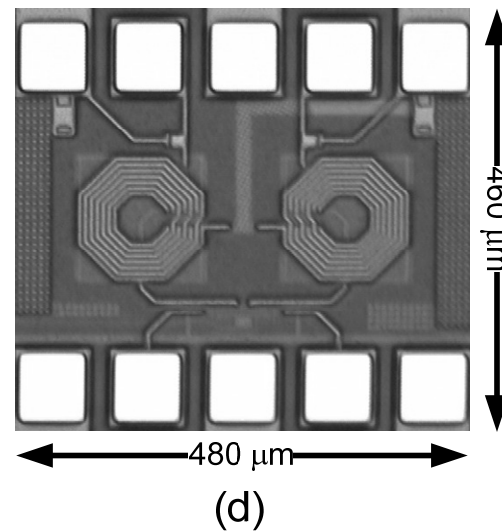
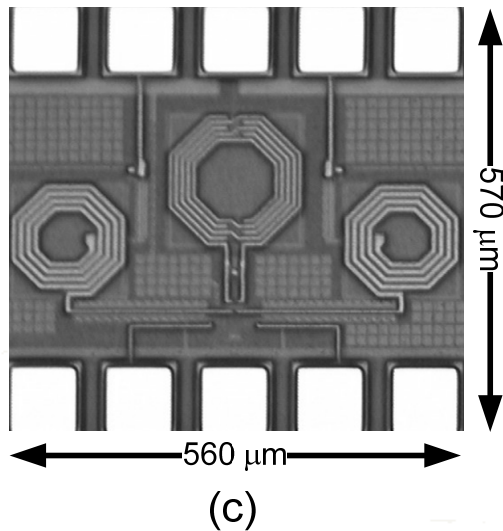
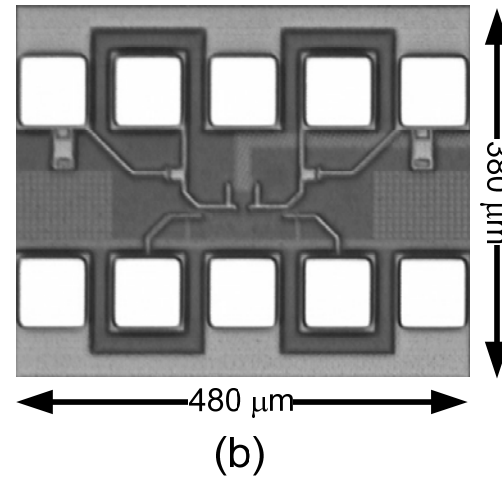
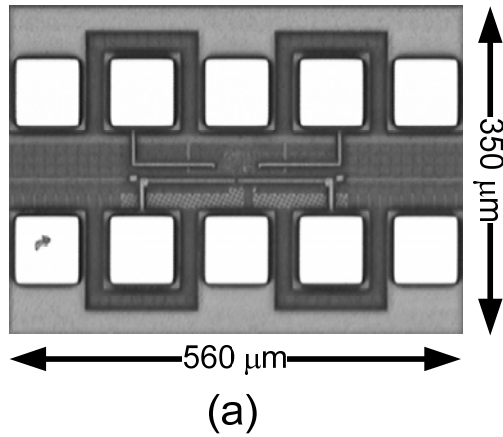
Asymmetric T-Coil
Gain = 12dB
BW = 10.4GHz
BWER = 4.1

Comparison

| Reference | Bandwidth Extension Technique | CMOS Tech. (nm) | Single-stage | | Multi-stage | | | |
|--------------------|---|-----------------|--------------|-------------------------------------|-------------|-----------------|----------------------|----------------|
| | | | Peaking (dB) | Single-stage BWER (Theory/Measured) | # Stages | Total Gain (dB) | Total Power (mW) | Total BW (GHz) |
| This work | Bridged-Shunt-Series | 180 | 0.7 | 4.0/3.0 | 1 | 14.1 | 30 | 8 |
| This work | Bridged-Shunt-Series | 180 | 0.3 | 3.5/3.0 | 1 | 14.1 | 30 | 8 |
| This work | Asymmetric T-coil with Negative Mutual Inductance | 180 | 1.5 | 4.6/4.1 | 1 | 12.1 | 30 | 10.4 |
| Galal, JSSC'04 | Shunt-Series | 180 | 1.8 | 3.5/NA | 5 | 20.3 | 190 | 22 |
| Kim, ISSCC'05 | Asymmetric T-coil with Positive Mutual Inductance | 130 | 0 | 3.23*/NA | - | - | - | 42 |
| Kanda, ISSCC'05 | Shunt-Series | 90 | 2.4 | 2/NA | 2 | - | 21.6 | 20 |
| Analui, ESSCIRC'02 | Series Peaking | 180 | 1.84-3 | 2.46/NA | 3 | 56dBΩ | 137.5 (single-ended) | 9.2 |

* Simulated

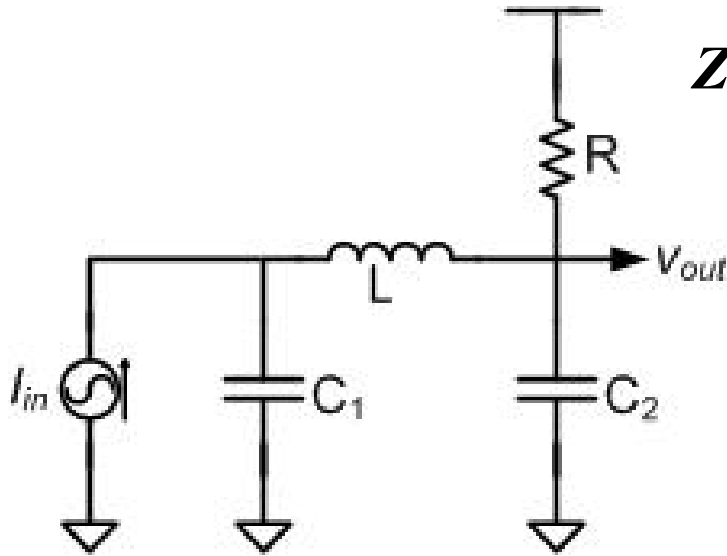
Die Micrographs in 0.18 μm CMOS



Conclusions

- Peaking techniques for larger BW extension
- Applicable to different k_C constraints
- Trade-off gain flatness for BW
- Amplifiers show large gain ($>12\text{dB}$) with largest BWER (4.1) reported.
- Wide bandwidth, high gain \rightarrow fewer stages \rightarrow power, area savings

Modified-Series Peaking



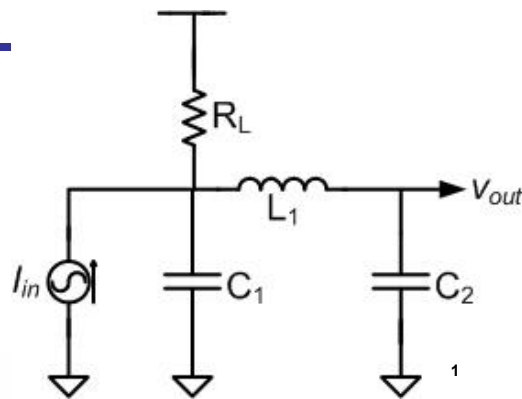
$$Z_N(s) = \frac{1}{1 + \frac{s}{\omega_0} + \left(\frac{k}{m}\right) \frac{s^2}{\omega_0^2} + \left(\frac{k(1-k)}{m}\right) \frac{s^3}{\omega_0^3}}$$

- $C_1 \equiv$ Drain parasitics, etc.
- $C = C_1 + C_2$
- $C_1 = k_C C = kC$
- $m = R^2 C / L$
- Note: R and L interchanged

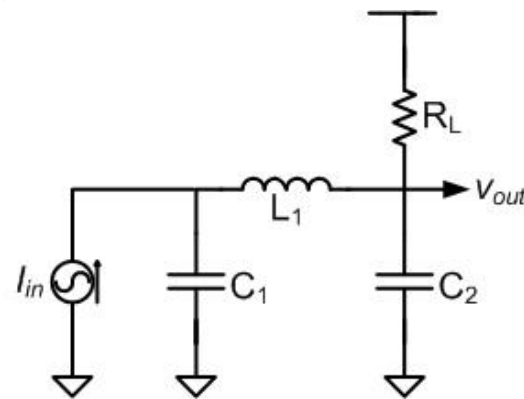
Assuming $k \ll 1$, $Z_N(\omega) \approx \frac{1}{(1 - \omega^2 LC_1)(1 + j\omega RC_2)}$

Peaking Response

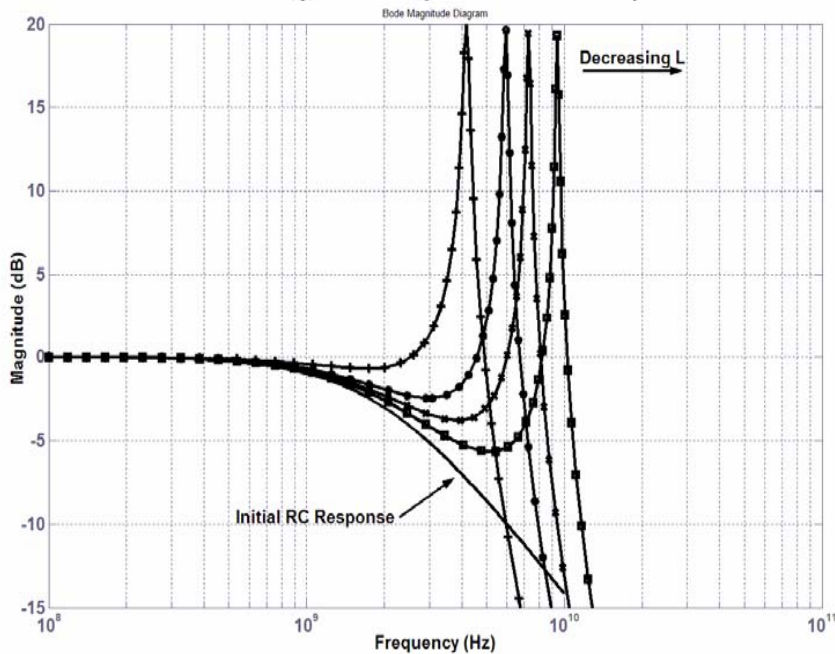
(a)



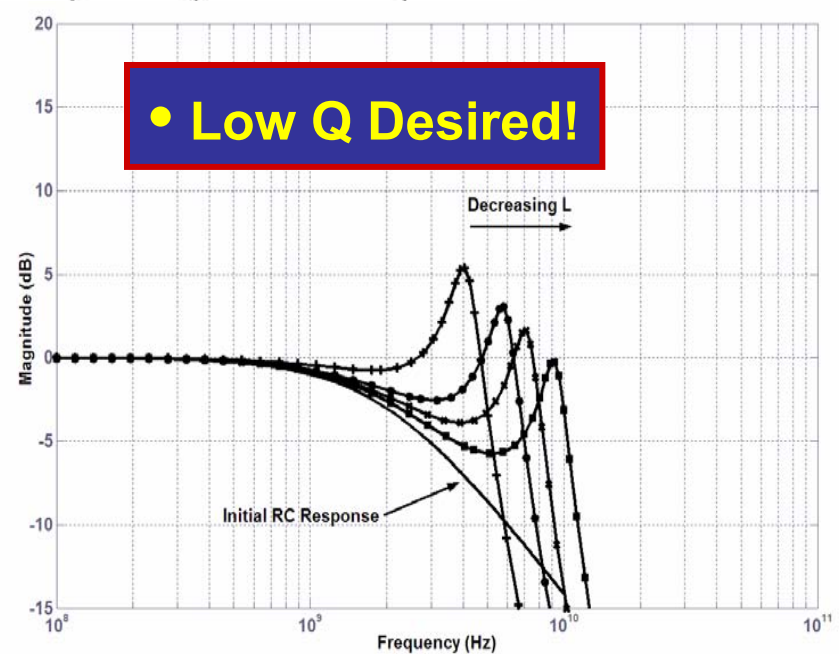
(b)



(c)

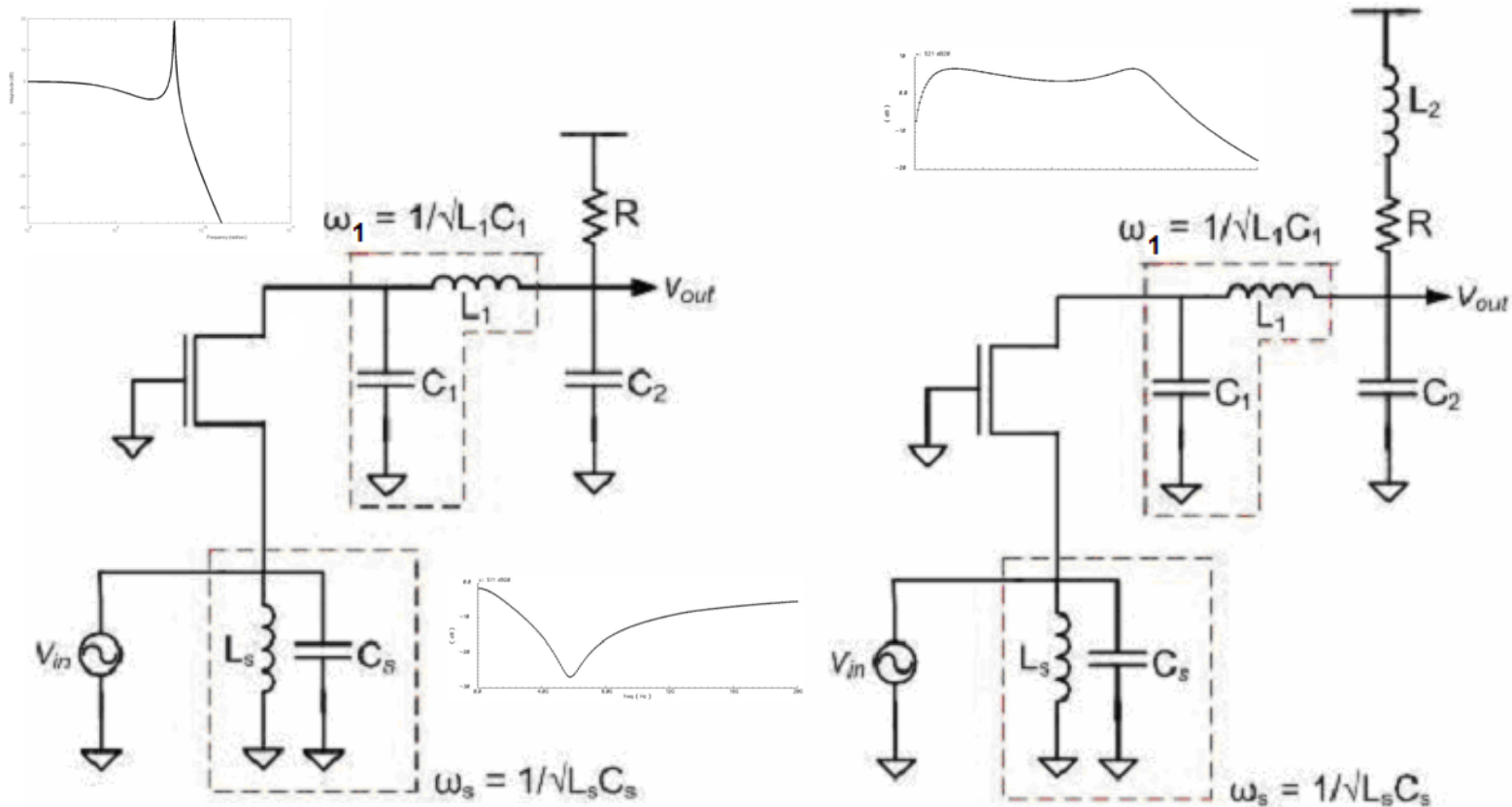


(d)



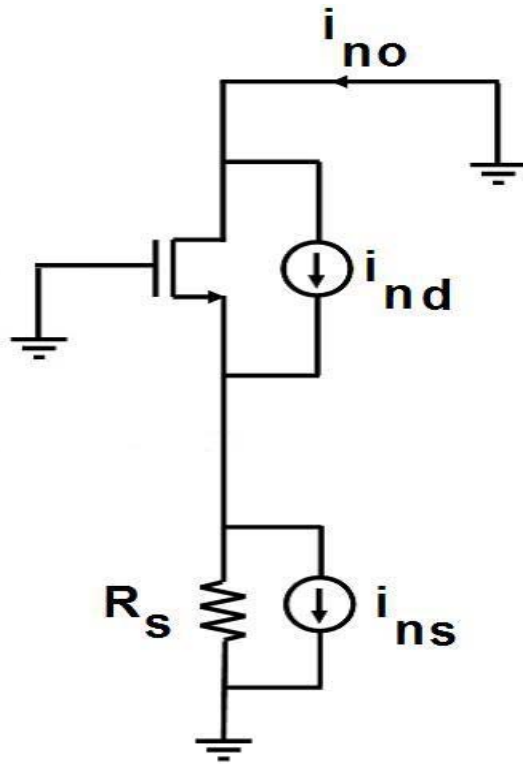
Simulated normalized responses of (b) with (c) L_1 ideal, and (d) L_1 with typical parasitics in a CMOS implementation (π -model)

Anti-Staggered Series Peaking

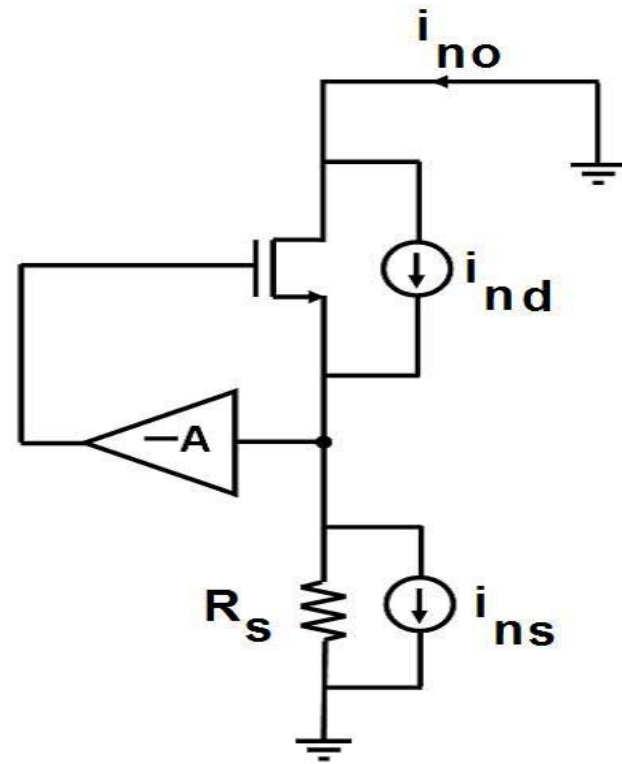


- Similar to Pre-emphasis Idea
- Actually Tuning S_{11} (zero) and S_{21} (pole)
- Common-gate Amplifier!

g_m -Boosted CGLNA



$$F \approx 1 + \frac{\gamma}{\alpha}$$

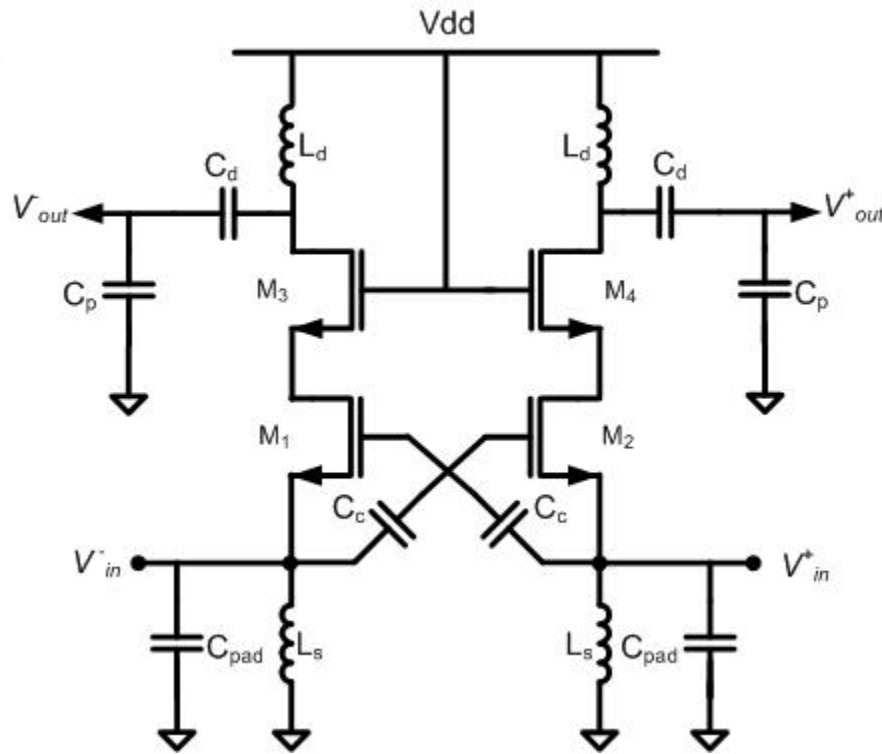


$$F \approx 1 + \frac{\gamma}{\alpha} \cdot \frac{1}{1+A}$$

*** X. Li, S. Shekhar and D.J. Allstot, "Low-power g_m -boosted LNA and VCO circuits in 0.18 μ m CMOS," IEEE Intl. Solid-State Circuits Conference, Feb. 2005, pp. 534,535,615.

*** X. Li, S. Shekhar and D.J. Allstot, "Gm-boosted LNA and VCO Circuits in 0.18 μ m CMOS," IEEE J. Solid-State Circuits, vol. 40, Dec. 2005.

Capacitor Cross-Coupled-CGLNA



W. Zhuo, X. Li, S. Shekhar, S.H.K. Embabi, J. Pineda de Gyvez, D.J. Allstot and E. Sanchez-Sinencio, "A capacitor cross-coupled common-gate low noise amplifier," *IEEE Trans. on Circuits and Systems I: Express Briefs*, vol. 52, 2005.

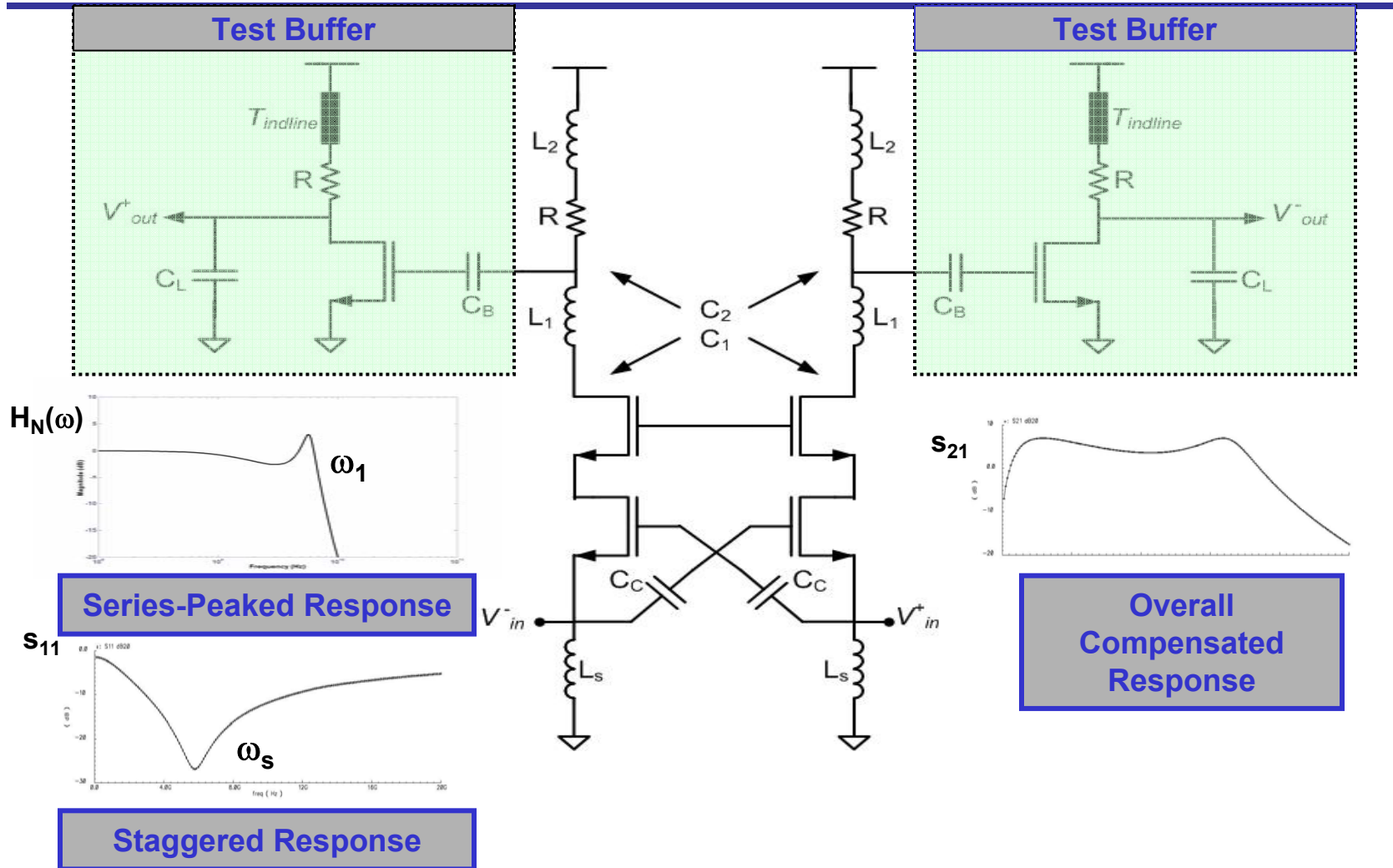
- Lower Noise Figure
- Lower DC Current

$$A = \frac{1}{1 + C_{gs}/C_c}$$

For $C_c \gg C_{gs}$

- $G_m = 2g_m$
- $C_{in} = 4C_{gs}$
- $F \approx 1 + \frac{\gamma}{2\alpha}$

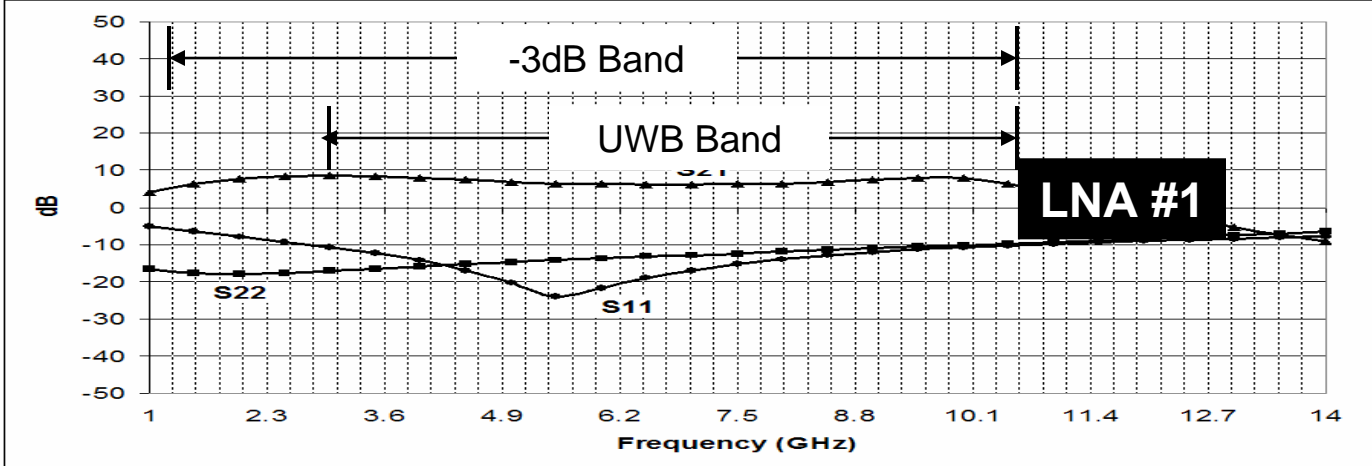
UWB CCCLNA



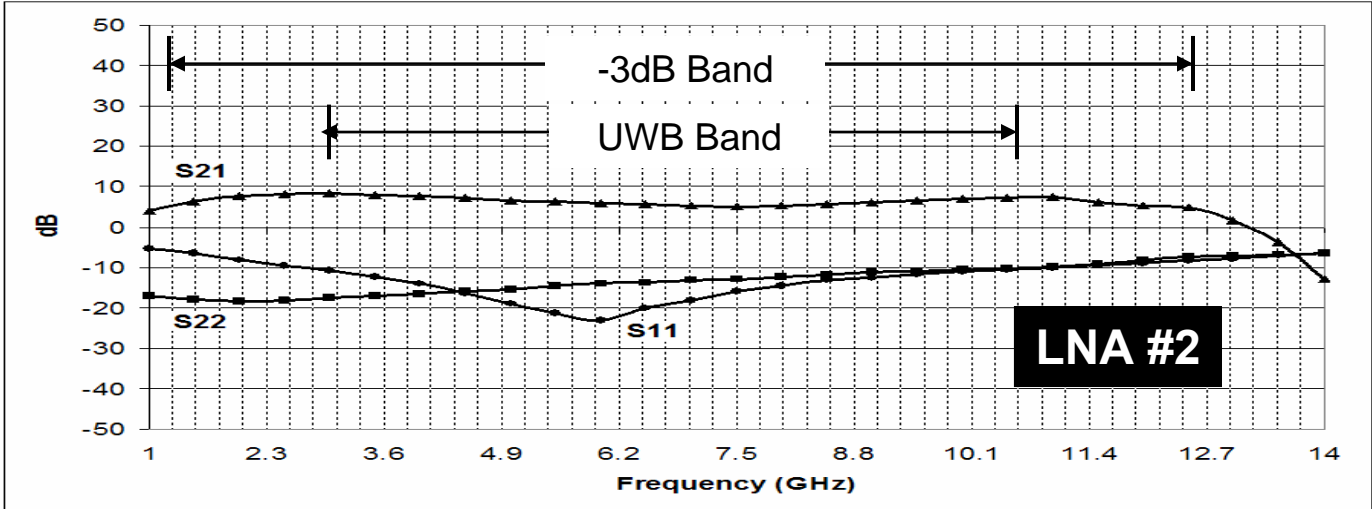
UWB LNA employing anti-stagger-compensated series peaking

Measurement Results

**4.1X with
2.4dB
Passband
Ripple**

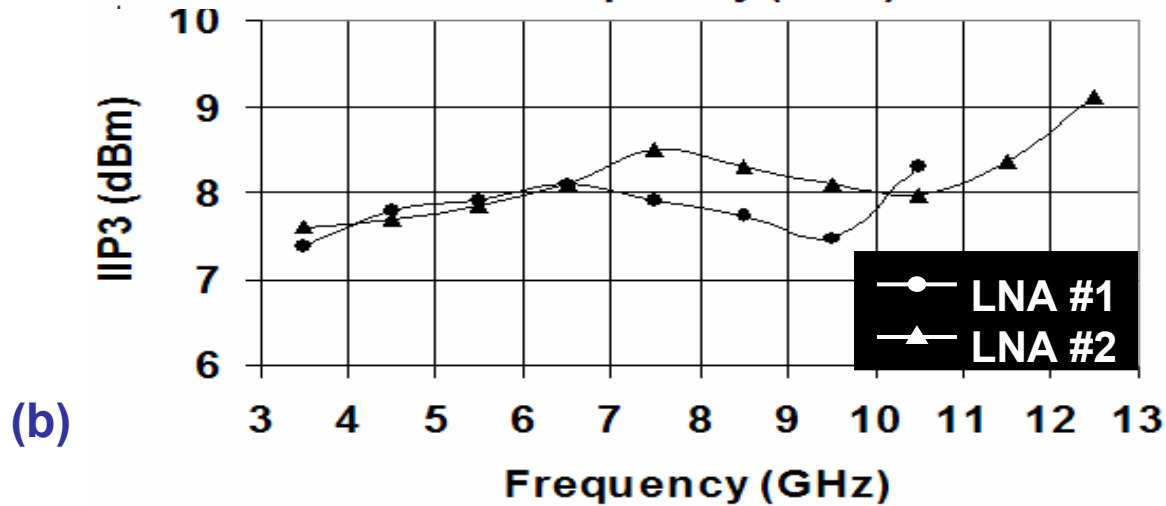
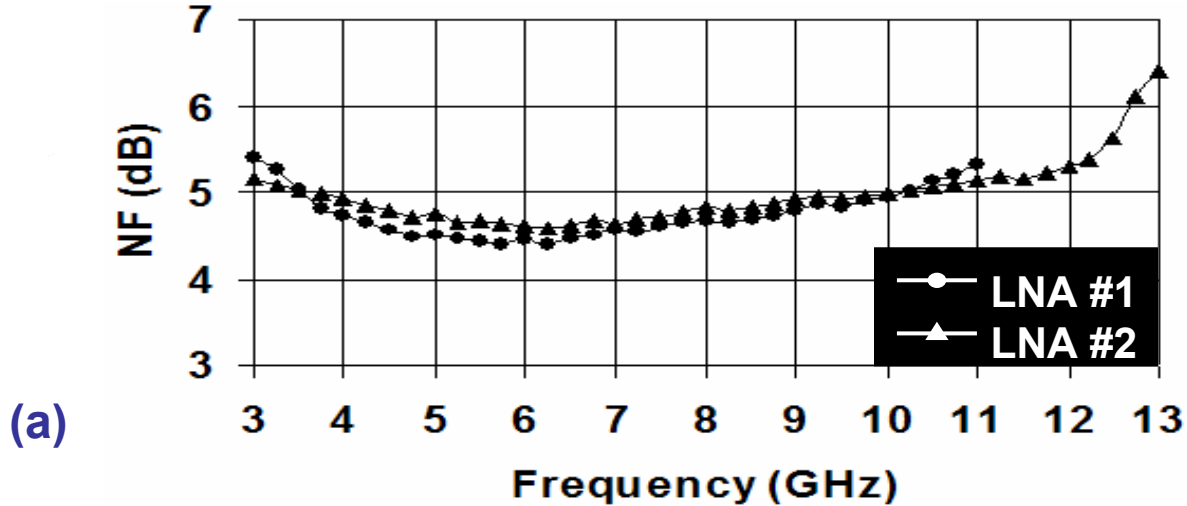


**4.9X with
3.0dB
Passband
Ripple**



Measured S-parameters of two versions of the UWB LNA

Measurement Results



Measured (a) *NF*, and (b) *IIP3* values of two versions of the UWB LNA

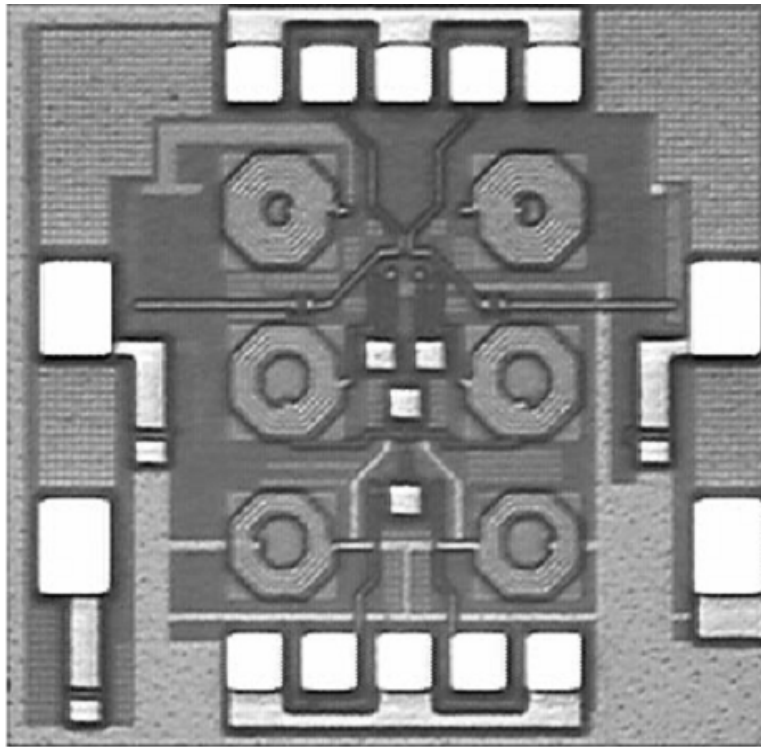
Performance Comparison

| Ref. | CMOS Tech. (nm) | -3dB BW (GHz) | Power (mW) | NF (dB) | Max.S 21 (dB) | IIP3 (dBm) | Area (mm ²) | FOM | |
|-----------------|------------------|---------------|------------|-----------|---------------|--------------|-------------------------|--|--|
| | | | | | | | | $\frac{Gain_{abs} \cdot BW_{GHz}}{(F-1) \cdot P_{mW}}$ | $\frac{Gain_{abs} \cdot IIP3_{mW} \cdot BW_{GHz}}{(F-1) \cdot P_{mW}}$ |
| LNA #1 | 180 | 1.3 - 10.7 | 4.5 | 4.4 - 5.3 | 8.5 | 7.4 to 8.3 | 1.0 | 2.33 to 3.17 | 12.8 to 21.4 |
| | | | | | | | | (differential) | |
| LNA #2 | 180 | 1.3 - 12.3 | 4.5 | 4.6 - 5.5 | 8.2 | 7.6 to 9.1 | 1.0 | 2.69 to 3.64 | 15.5 to 29.6 |
| | | | | | | | | (differential) | |
| [1] | 180 | 2.3 - 9.2 | 9 | 4.0 - 9.0 | 9.3 | -8.2 to -5.6 | 1.1 | 0.32 to 1.48 | 0.05 to 0.41 |
| | | | | | | | | (single-ended) | |
| [2] | 180 | 0.5 - 14 | 52 | 3.4 - 5.4 | 10.6 | 9.4 | 1.6 | 0.36 to 0.74 | 3.11 to 6.45 |
| | | | | | | | | (single-ended) | |
| [2] | 180 | 0.6 - 22 | 52 | 4.3 - 6.1 | 7.3 | 8.7 | 1.35 | 0.31 to 0.56 | 2.3 to 4.18 |
| | | | | | | | | (single-ended) | |
| Heydari, RFIC05 | 180 ⁺ | 0 - 12.6 | 19.8 | 2.9 | 9.6 | -3.4 | 0.76 | 2.02 | 0.92 |
| | | | | | | | | (single-ended) | |
| Yazdi, Isscc05 | 180 ⁺ | 0 - 25 | 54 | 4.8 - 7 | 9.1 | 4.7 | 1.32 | 0.33 to 0.65 | 0.97 to 1.93 |
| | | | | | | | | (differential) | |

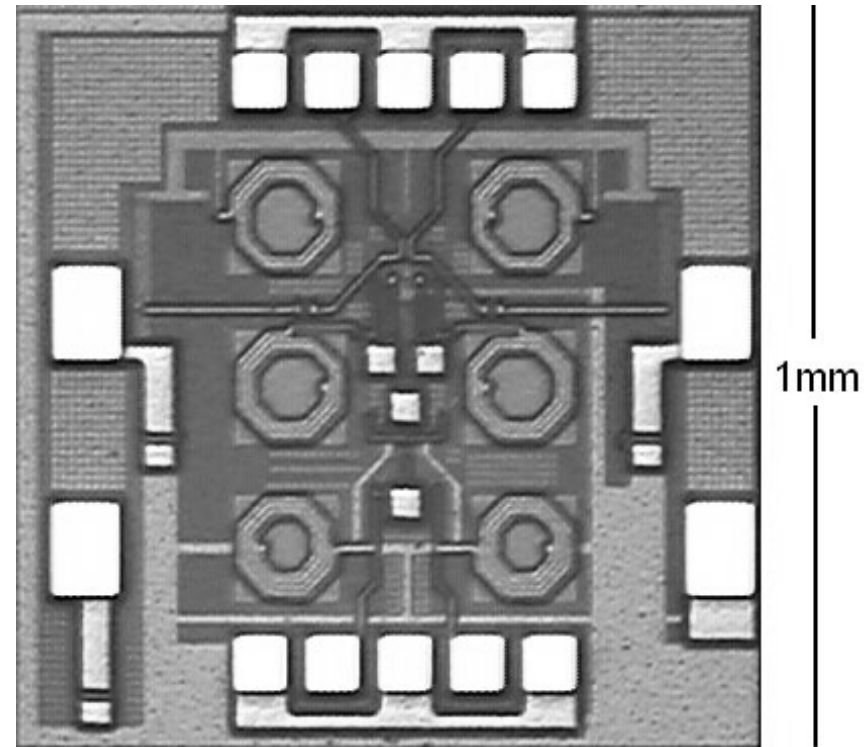
Wideband LNA Measured Performance Comparison

Chip Microphotographs

UWB LNA #1



UWB LNA #2



Chip Microphotographs; 0.18 μ m RF CMOS

S. Shekhar, J.S. Walling and D.J. Allstot, "Bandwidth extension techniques for CMOS amplifiers," *IEEE J. Solid-State Circuits*, vol. 41, Nov. 2006.

Conclusions

- **Pros** 😊
 - Large Bandwidth Extension
 - Low Power
 - Simple Input Match
 - Low Inductor Count
 - Flat Noise Figure
- **Cons** ☹️
 - Low Gain
 - Bandwidth Extension Requires Two Stages/Nodes
 - 3dB Ripple Too Large for Some Applications
 - Sensitive Tuning