

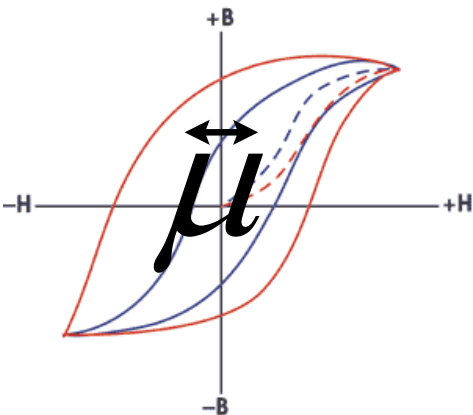


Santa Clara Valley  
CHAPTER

# EXTRACTION OF DIELECTRIC PROPERTIES OF PCB LAMINATE DIELECTRICS ON PCB STRIPLINES TAKING INTO ACCOUNT CONDUCTOR SURFACE ROUGHNESS

SPEAKER: DR. MARINA KOLEDINTSEVA, IEEE SENIOR MEMBER,  
ORACLE

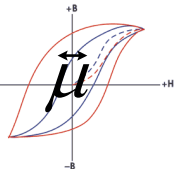
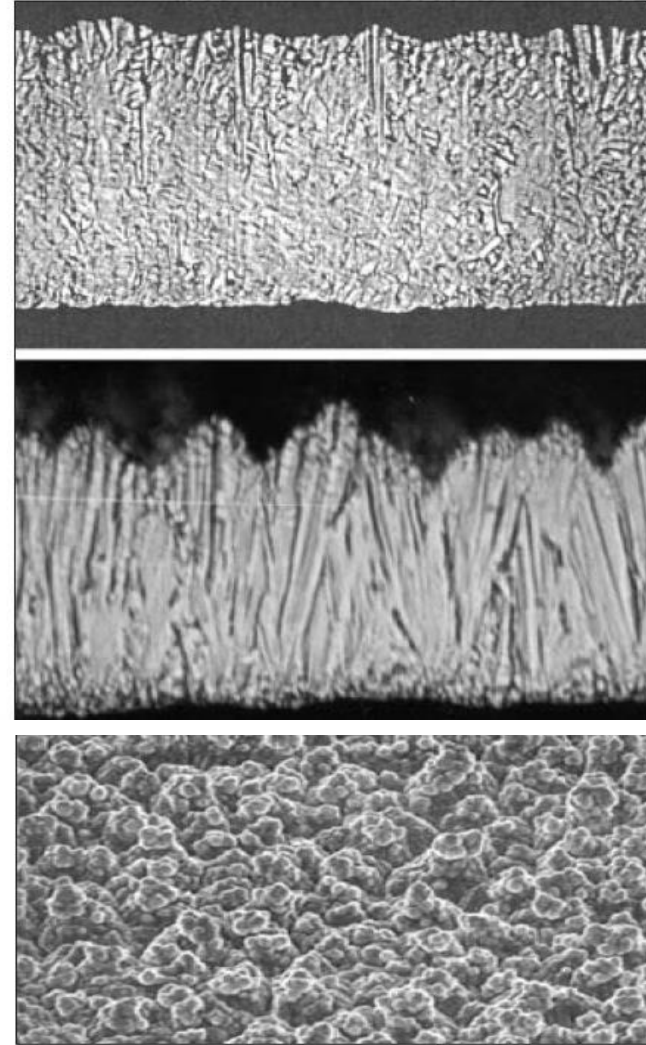
(THE WORK IS DONE IN EMC LAB OF MISSOURI S&T, SPONSORED BY CISCO AND NSF)



Tuesday, May 13, 2014

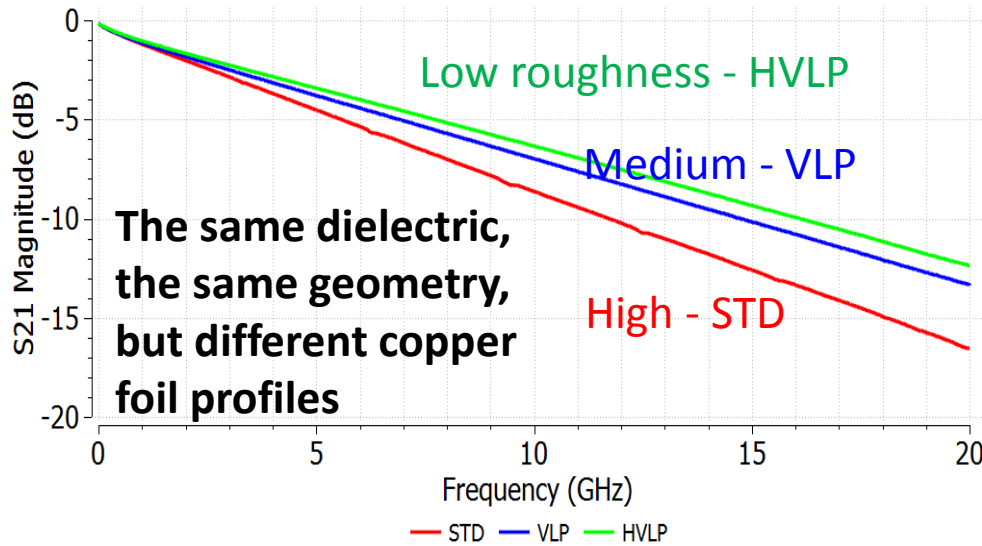
# Outline

- I. Introduction – motivation, objectives, and state-of-the-art
- II. Idea of an “effective roughness dielectric” (ERD)
- III. PCB stripline cross-sectional analysis and roughness profile quantification
- IV. Experiment-based input data for numerical electromagnetic modeling
- V. Modeling results & validation
- VI. Building of “design curves” regarding conductor surface roughness
- VII. Conclusions

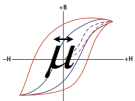
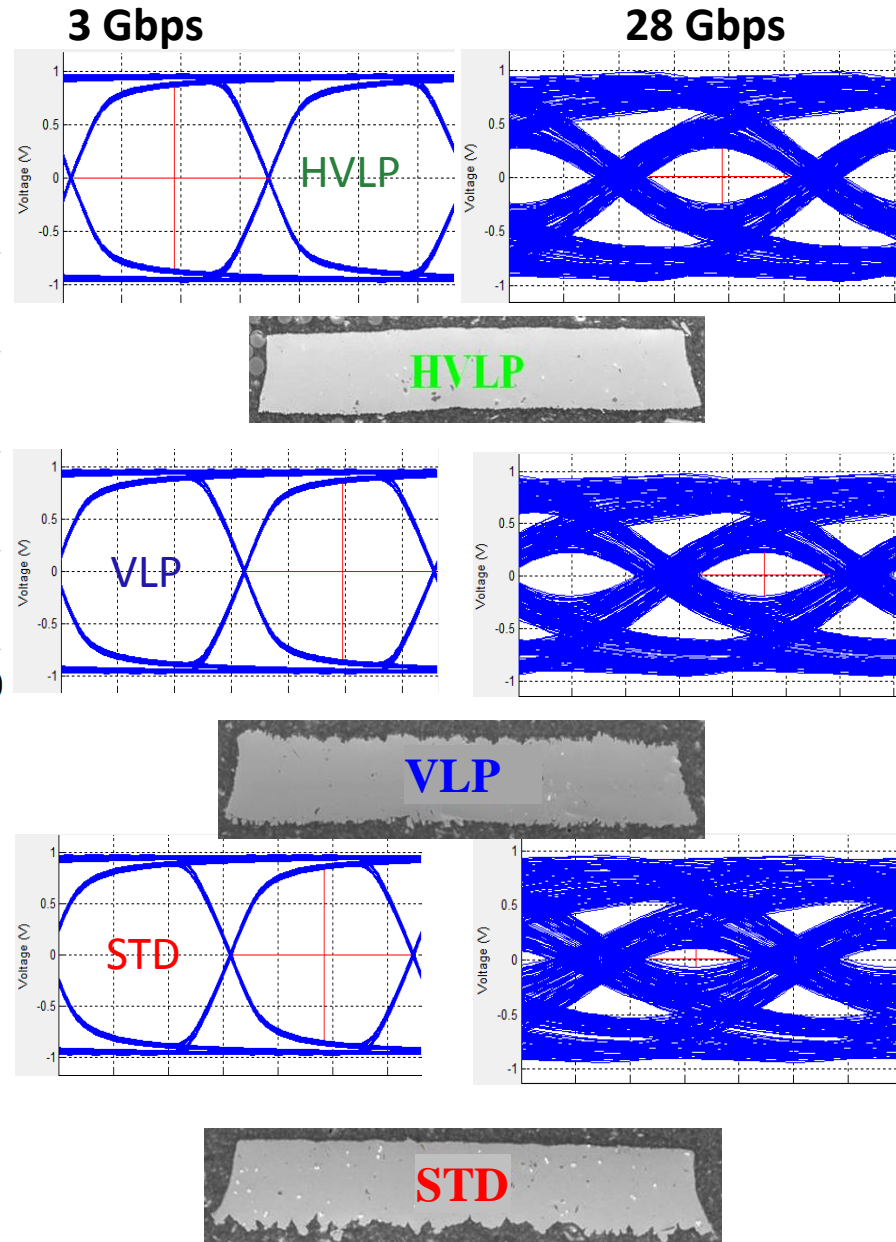


# Motivation

- Conductor roughness affects both phase and loss constants in PCB transmission lines and results in eye diagram closure.

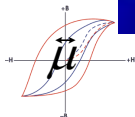
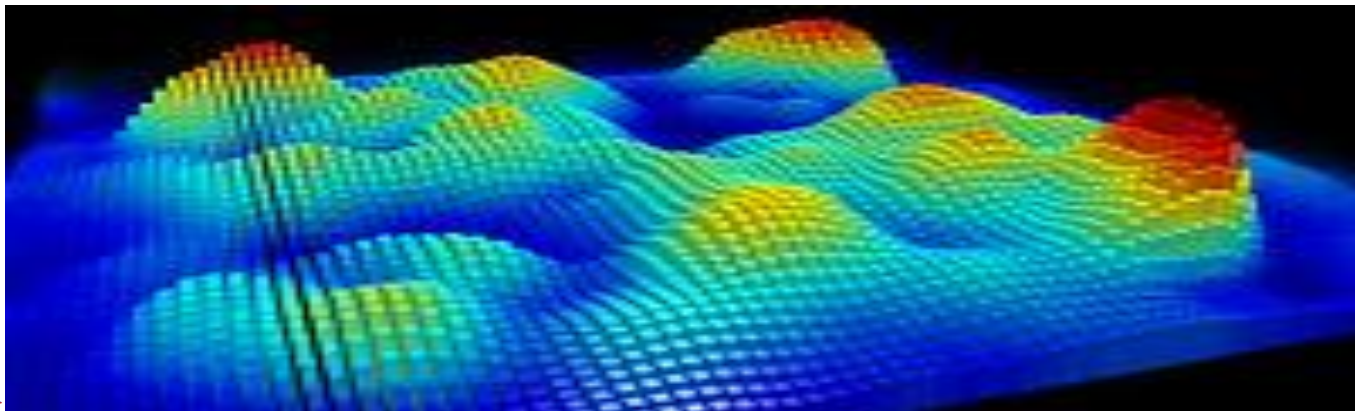


- Conductor surface roughness lumps into laminate dielectric parameters.
- Any existing analytical and numerical models of conductor surface roughness are **approximations**.
- Study and adequate modeling of wideband behavior of dielectrics and conductors in PCBs is important from SI point of view.

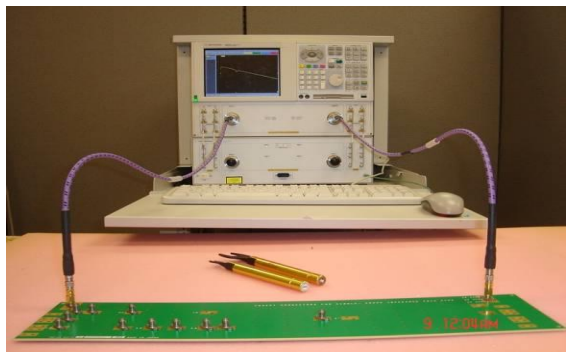
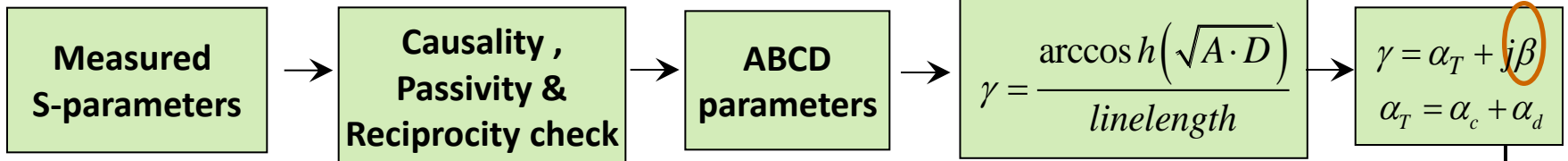


# Objectives

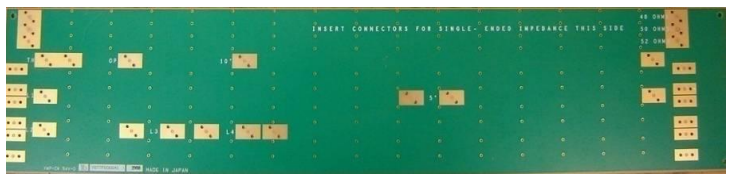
- Develop a technique to accurately measure and extract laminate dielectric parameters ( $DK=\epsilon'$  &  $DF=\tan\delta$ ) removing effects of conductors.
- Develop a physics-based model, which allows for simple incorporation of conductor surface roughness in electromagnetic numerical models of transmission lines.
- Test and validate the proposed model using measurements on a multitude of various test boards with different cross-sections and roughness profiles.
- Test and validate the proposed model using electromagnetic numerical simulations with different software tools.
- Develop a database for roughness parameters, corresponding to different types of copper foils used in PCBs.



# Measurements & Material Parameter Extraction



S-parameters are measured using VNA or TDR with "Through-Reflect-Line" (TRL) calibration in f-domain or t-domain, respectively



A. Koul, M. Koledintseva, et al, *Proc. IEEE Symp. Electromag. Compat.*, Aug. 17-21, Austin, TX, 2009, 191-196

Main problem!

Model or experimentally retrieve conductor loss for rough stripline conductor

$\alpha_d = \alpha_T - \alpha_c$

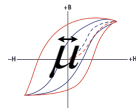
$$\beta = \frac{\omega}{c} \cdot \sqrt[4]{\epsilon_r'^2 + \epsilon_r''^2} \cdot \cos\left(\frac{\delta}{2}\right)$$

$$\alpha_d = \frac{\omega}{c} \cdot \sqrt[4]{\epsilon_r'^2 + \epsilon_r''^2} \cdot \sin\left(\frac{\delta}{2}\right)$$

Solve the system of equations to obtain complex permittivity

- OPTIONS

  - Analytical Models
  - Numerical Models
  - Experimental



# Existing Methods for Conductor Roughness Modeling

## I. Correction coefficients for attenuation

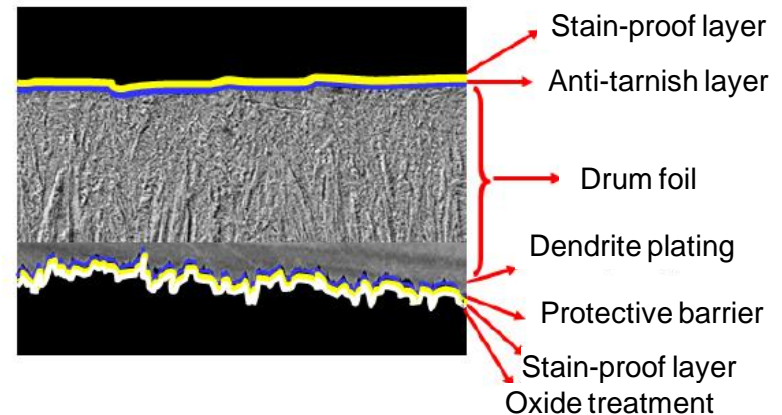
- Periodic roughness models (Morgan, Sanderson, Sundstroem, Lukic)
- Hammerstad model (Hammerstad, Bekkadal, Jensen)
- “Snowball” model (Huray)
- Roughness hemispheres (Hall, Pytel)
- Stochastic models (Sanderson, Tsang, Braunisch)

## II. Impedance boundary conditions

- Holloway, Kuester

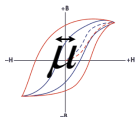
## III. Numerical electromagnetic modeling

- Deutsch
- Shlepnev
- X. Chen



## IV. Experimental separation of conductor & dielectric loss

- Koledintseva et al



# Our Recently Published Works

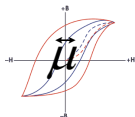
- Experiment-based Differential and Extrapolation Roughness Measurement techniques (**DERM** and **DERM-2**) have been proposed to refine wideband DK and DF from roughness.

[1] A. Koul, M.Y. Koledintseva, S. Hinaga, and J.L. Drewniak, “Differential extrapolation method for separating dielectric and rough conductor losses in printed circuit boards”, *IEEE Trans. Electromag. Compat.*, vol. 54, no. 2, Apr. 2012, pp. 421-433.

[2] M.Y. Koledintseva, A.V. Rakov, A.I. Koledintsev, J.L. Drewniak, and S. Hinaga, “Improved experiment-based technique to characterize dielectric properties of printed circuit boards”, *IEEE Trans. Electromag. Compat.* (to be published soon in 2014)

- An Effective Roughness Dielectric (**ERD**) approach has been proposed to substitute inhomogeneous roughness boundary layer by a layer with homogenized dielectric properties.

[3] M.Y. Koledintseva, A. Razmadze, A. Gafarov, S. De, S. Hinaga, and J.L. Drewniak, “PCB conductor surface roughness as a layer with effective material parameters”, *IEEE Symp. Electromag. Compat.*, Pittsburg, PA, 2012, pp. 138- 142.

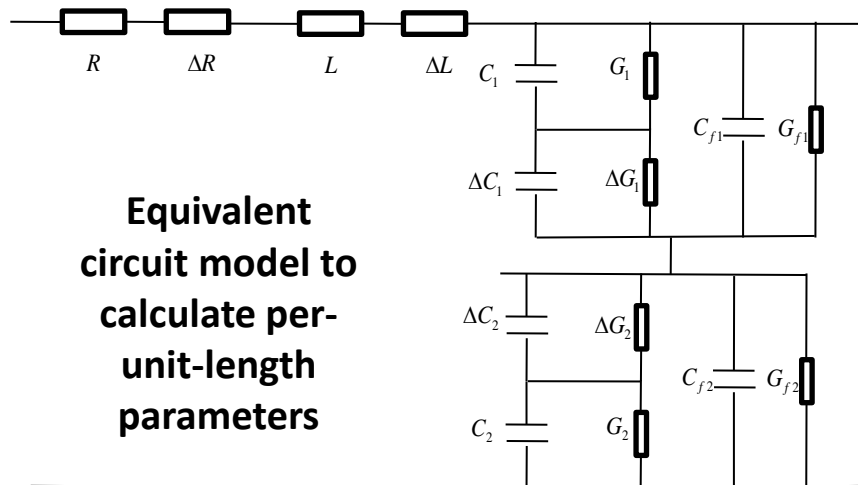
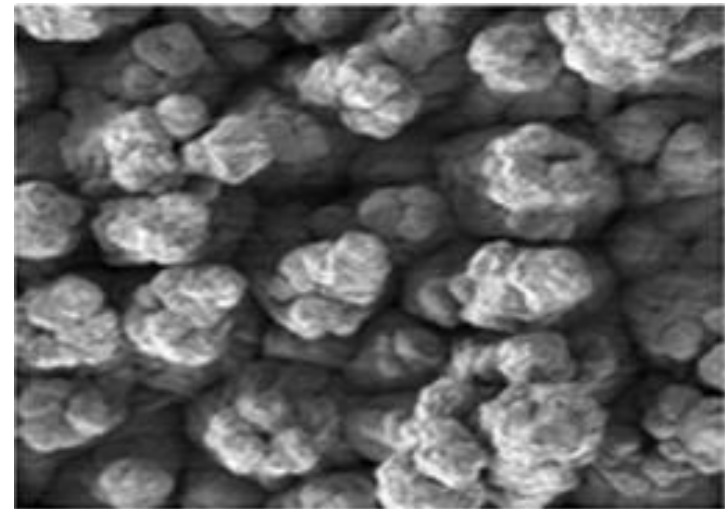
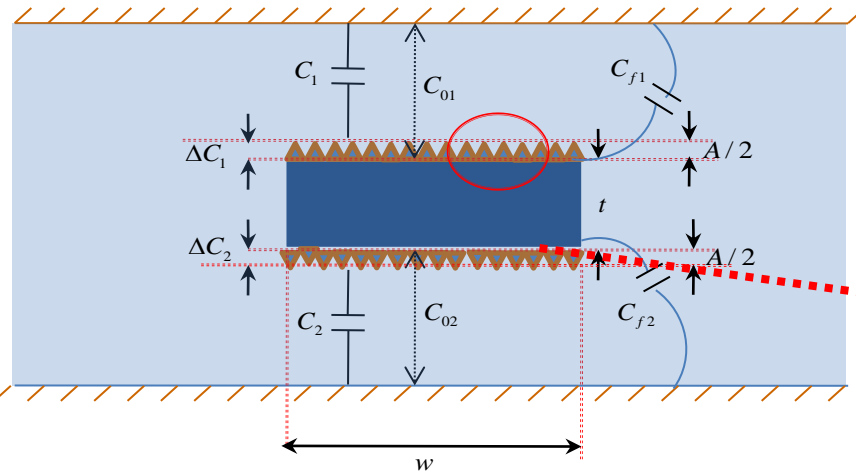


# Idea of “Effective Roughness Dielectric”

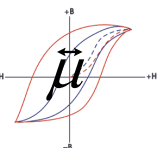
Roughness leads to the capacitance increase!

This effect was first noticed in:

A. Deutsch, A. Hueber, et al, “Accuracy of dielectric constant measurement using the full-sheet-resonance technique IPC-T650 2.5.5.6”, 311-314, *IEEE Symp. Electrical Performance of Electronic Packaging*, 2002.

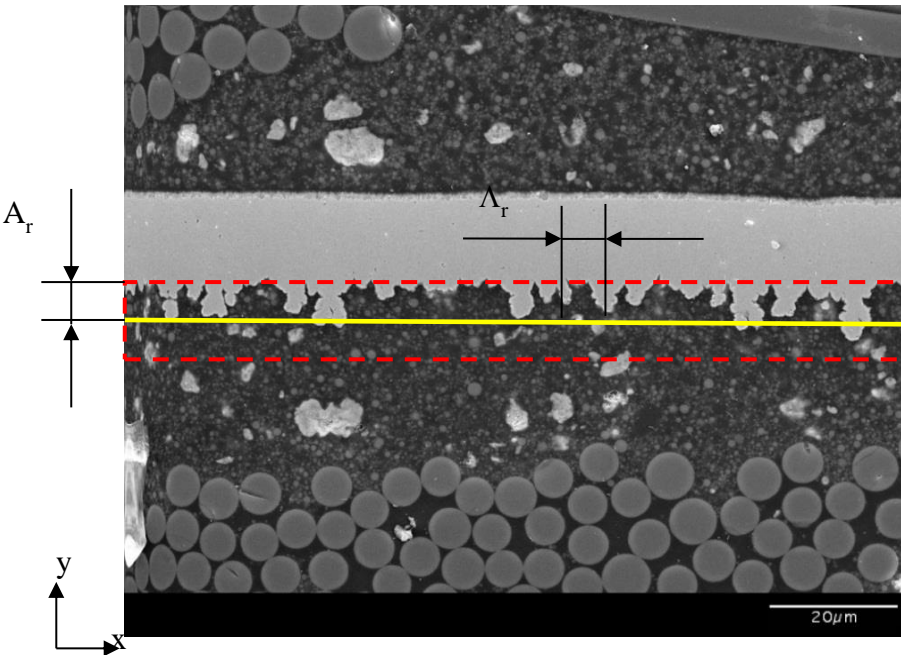


Equivalent circuit model to calculate per-unit-length parameters





# Mixing Rule for “Effective Roughness Dielectric”



## Maxwell Garnett Mixing Rule for aligned metallic inclusions

A.H. Sihvola, *Electromagnetic Mixing Formulas and Applications*, IEE, 1999.

$$\epsilon_{eff,y} = \epsilon_{matrix} \left( 1 + v_{incl} \frac{\epsilon_{incl} - \epsilon_{matrix}}{\epsilon_{matrix} + (1 - v_{incl}) N_y (\epsilon_{incl} - \epsilon_{matrix})} \right)$$

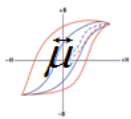
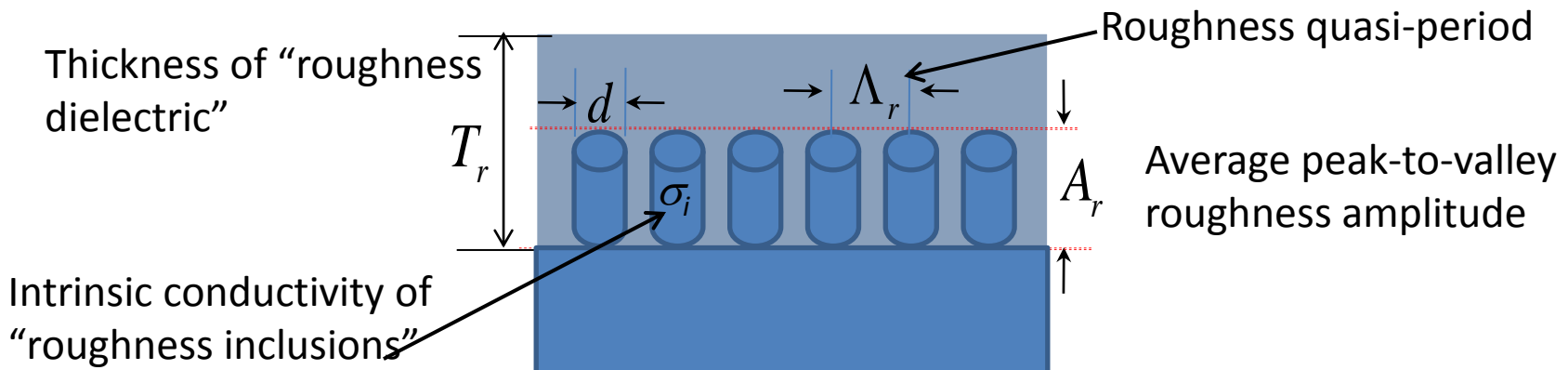
$$N_y = \frac{1}{a^2} \ln(a)$$

Depolarization factor of cylindrical inclusions

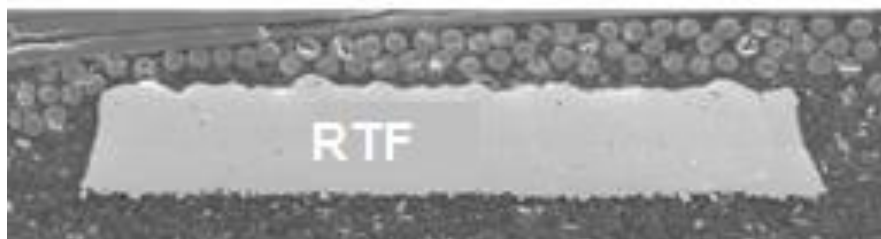
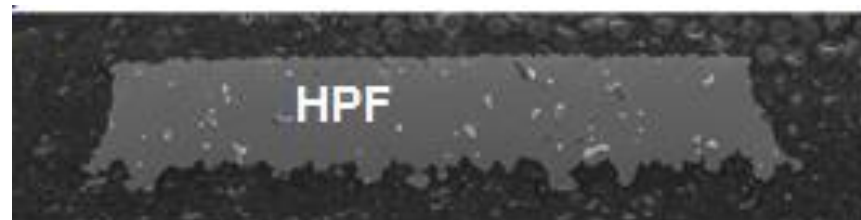
$$a = A_r / d$$

Aspect ratio of inclusions

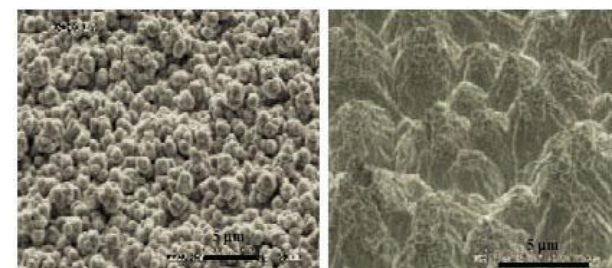
$$\epsilon_{incl} = \epsilon_i - \frac{j\sigma_i}{\omega\epsilon_0} \quad \epsilon_{matrix} = \epsilon'_m - j\epsilon''_m$$



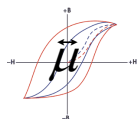
# Various Types of Foils



- **HPF** (high-performance foil) -  $10 \mu\text{m} < R_z < 15 \mu\text{m}$
- **STD** (standard foil) -  $5 \mu\text{m} < R_z < 10 \mu\text{m}$
- **VLP** (very-low profile foil) -  $3 \mu\text{m} < R_z < 6 \mu\text{m}$
- **RTF** (reverse-treatment foil) -  $3 \mu\text{m} < R_z < 6 \mu\text{m}$
- **HVLP** (hyper-very-low profile foil) -  $1 \mu\text{m} < R_z < 3 \mu\text{m}$
- **ULP** (ultra-low roughness foil) -  $0.5 \mu\text{m} < R_z < 1 \mu\text{m}$



Foils are mostly isotropic in X and Z



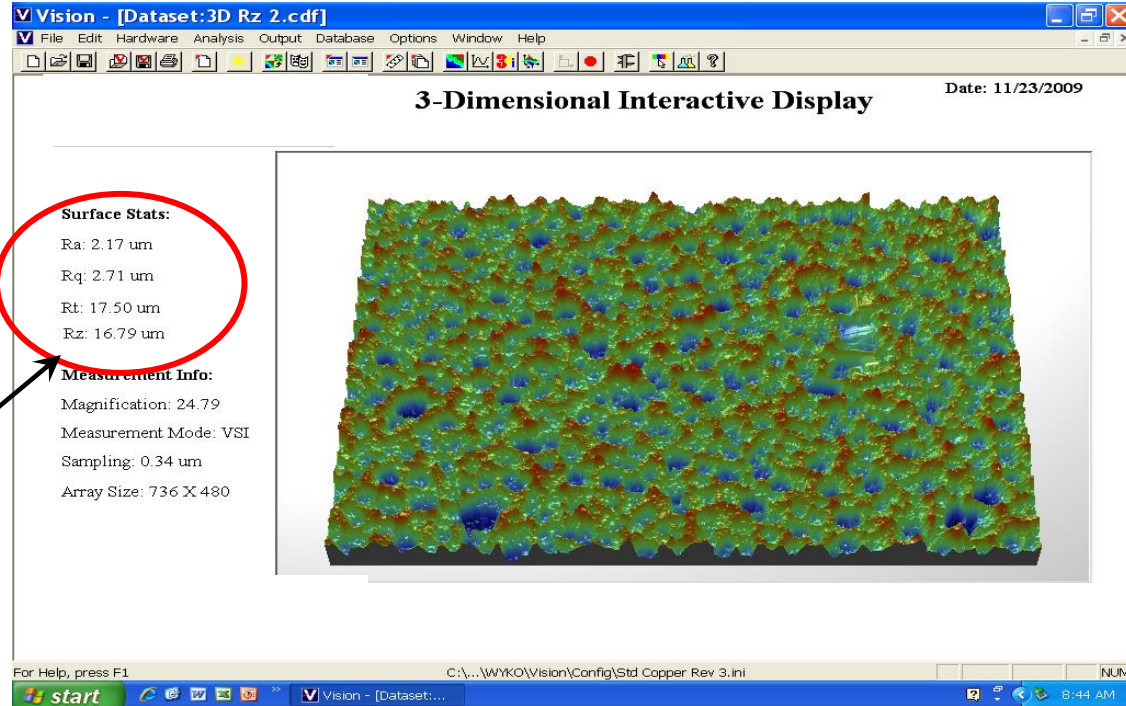
# Standard Profilometer Roughness Evaluation

## Surface Profilometer



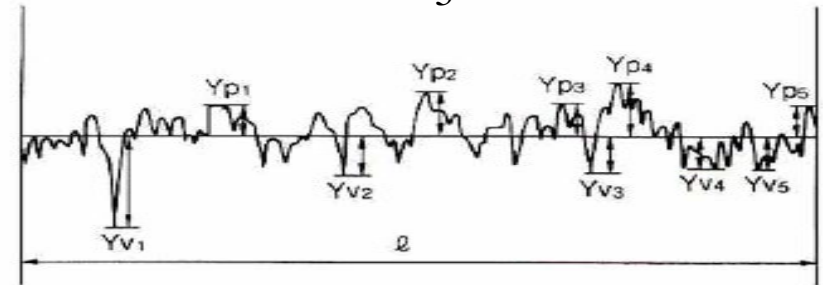
- Mechanical
- Optical

Roughness of conductors on PCB are evaluated based on the **amplitude data only**: Ra, Rq, **Rz**, and Rt.

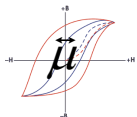


Foil / Trace Thickness	t=12μm	t=18μm	t=35μm
Low rough (HVLP)	1.5 μm	1.5 μm	1.5 μm
Medium rough (VLP)	3 μm	3.5 μm	4 μm
Standard foil (STD)	5 μm	6 μm	8 μm

$$R_z = \frac{|Y_{p1} + Y_{p2} + Y_{p3} + Y_{p4} + Y_{p5}| + |Y_{v1} + Y_{v2} + Y_{v3} + Y_{v4} + Y_{v5}|}{5}$$



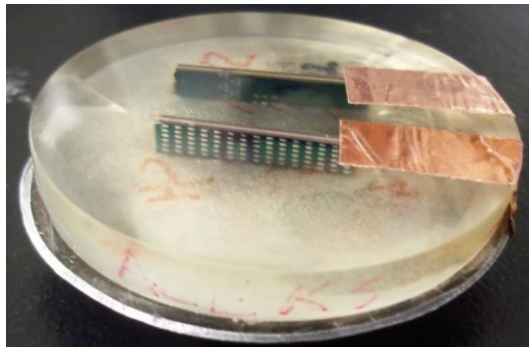
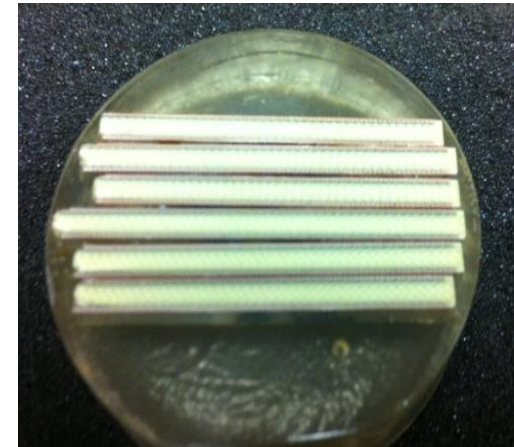
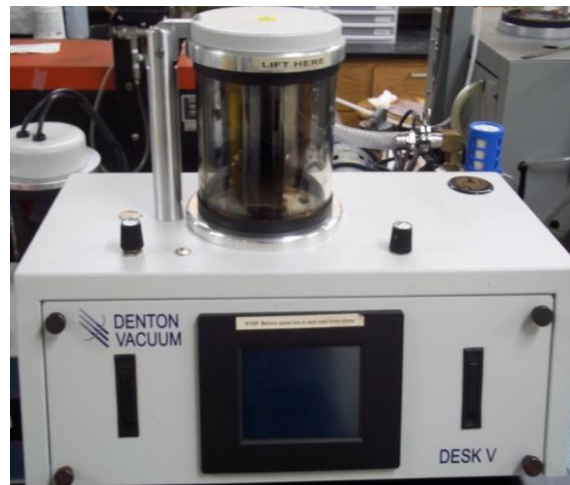
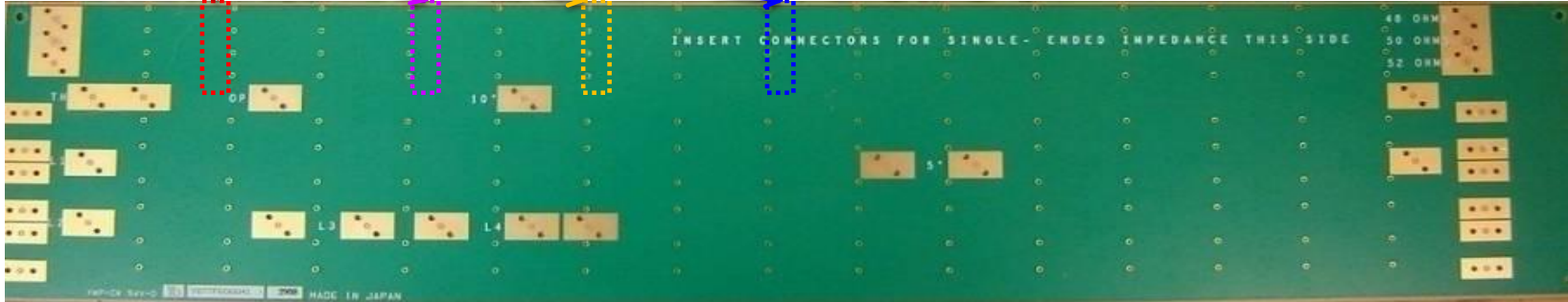
**Problem: foil measured is not the same as "in situ".**



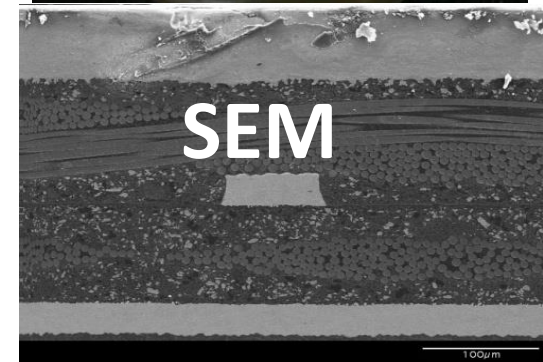
# SEM & Optical Cross-sectional Analysis of PCB

Cutting board for cross-sections

## Striplines

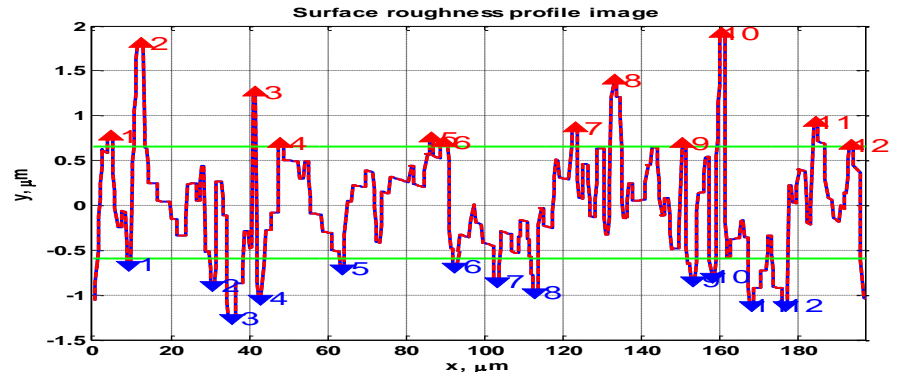
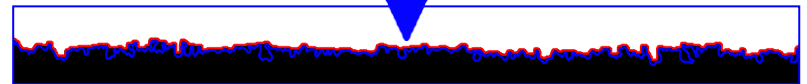
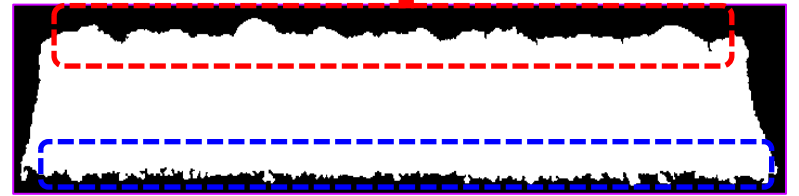
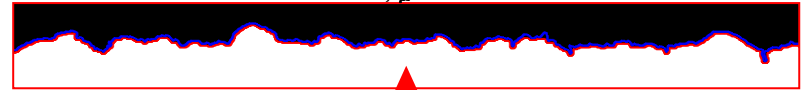
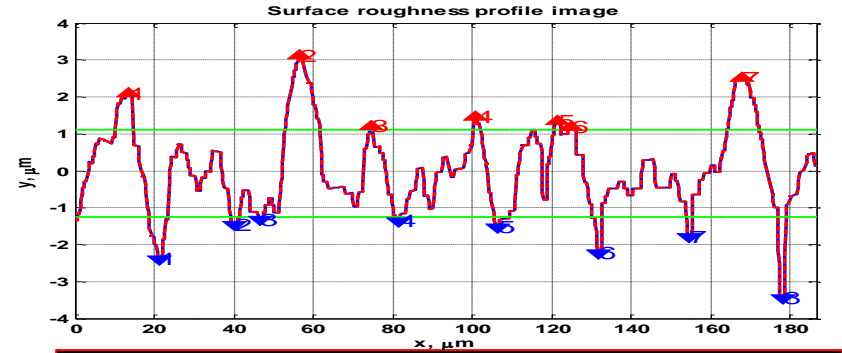
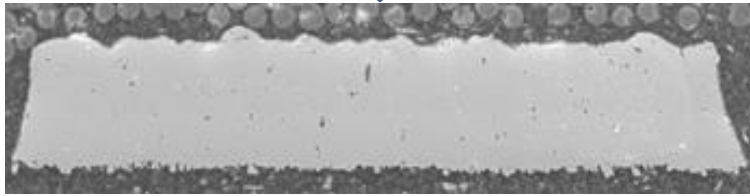
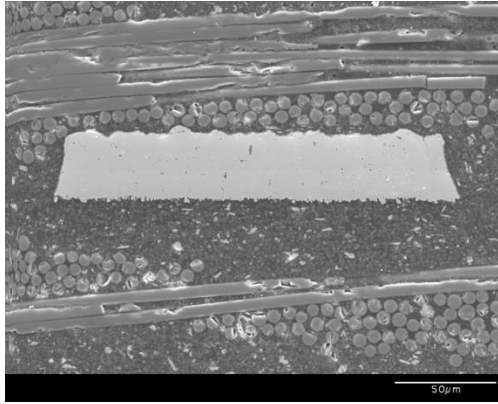


Optical



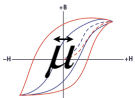
SEM

# Conductor Roughness Profile Extraction

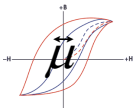
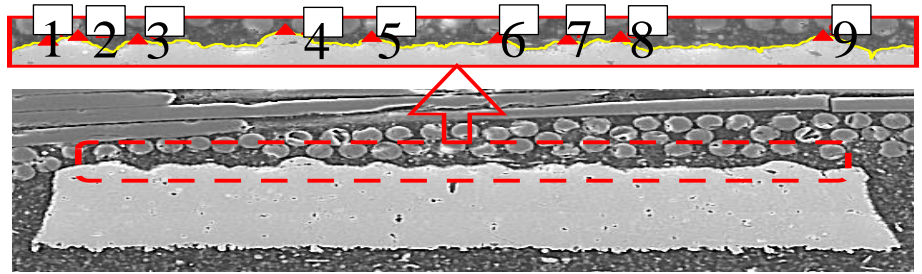
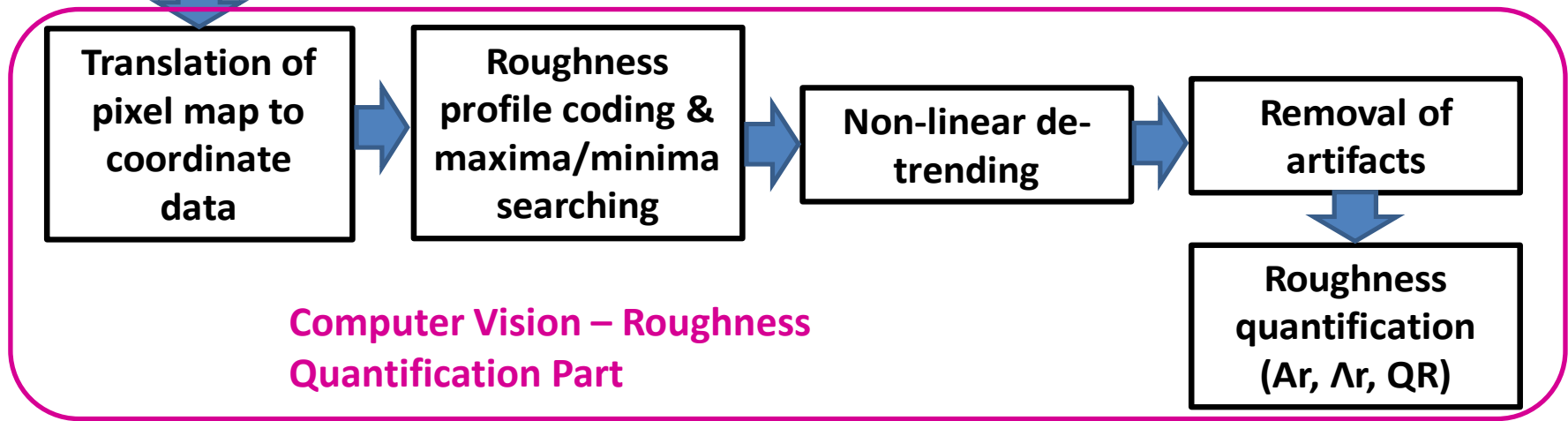
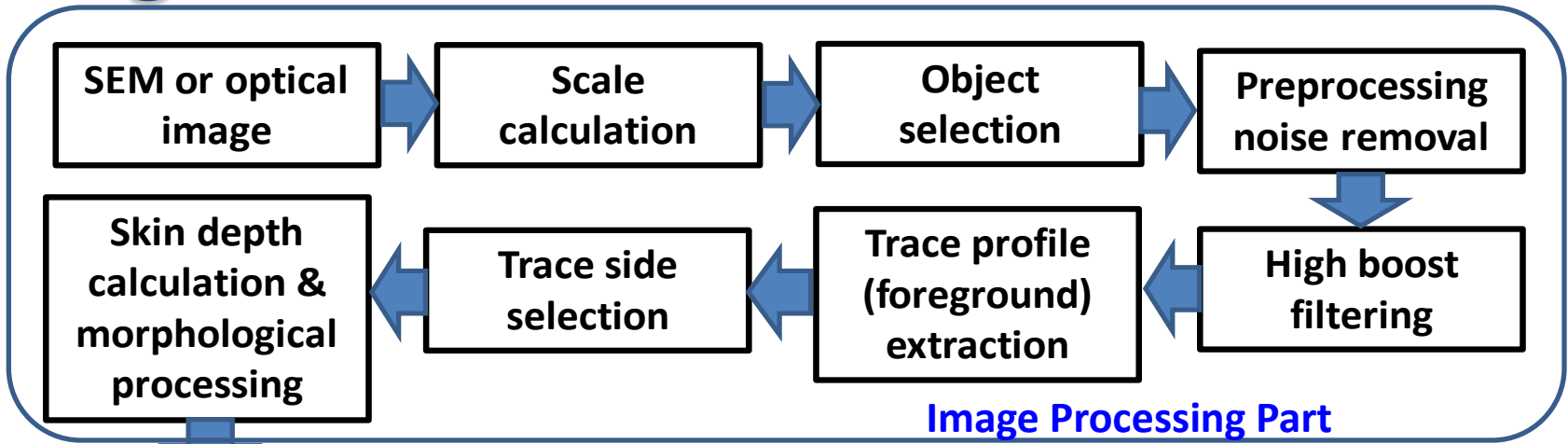


[S. Hinaga, S. De, A.Y. Gafarov, M.Y. Koledintseva, and J.L. Drewniak, "Determination of copper foil surface roughness from microsection photographs", *Techn. Conf. IPC Expo/APEX 2012*, Las Vegas, Apr. 2012].

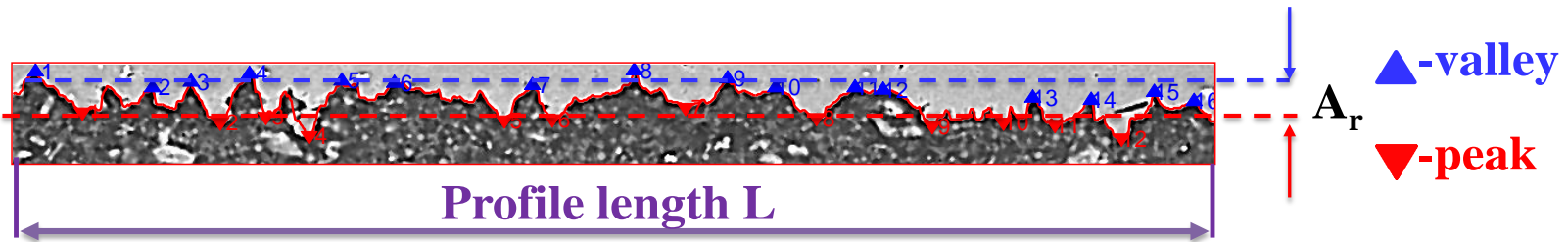
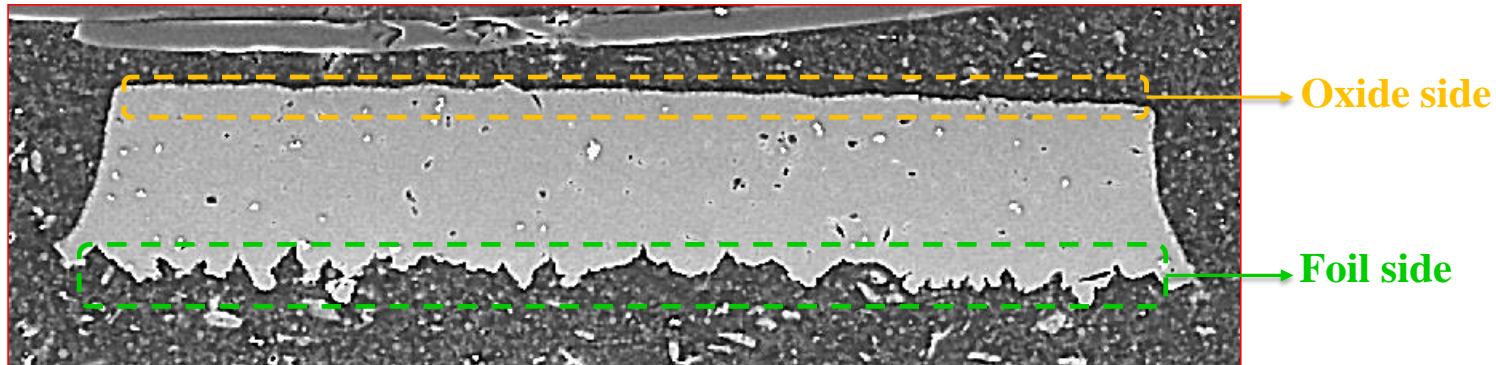
[S. De, A.Y. Gafarov, M.Y. Koledintseva, S. Hinaga, R.J. Stanley, and J.L. Drewniak, "Semi-automatic copper foil surface roughness detection from PCB microsection images", *IEEE Symp. EMC.*, Pittsburg, PA, 2012, pp. 132-137].



# Roughness Characterization Flow Chart



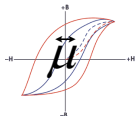
# Roughness Factor QR



Average peak-to-valley amplitude: 
$$A_r = \frac{\sum_{i=1}^{N_{peak}} |Y_{i\ peak}|}{N_{peak}} + \frac{\sum_{i=1}^{N_{valley}} |Y_{i\ valley}|}{N_{valley}}$$

Roughness quasi-period: 
$$\Lambda = \frac{L \times N_{valley} + L \times N_{peak}}{2 \times N_{valley} \times N_{peak}}$$

**Roughness factor:** 
$$QR = \left( \frac{A_r}{\Lambda} \right)_{oxide} + \left( \frac{A_r}{\Lambda} \right)_{foil}$$

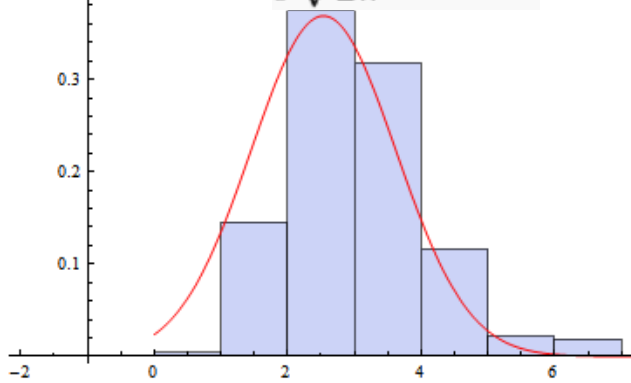


# Roughness Surface Generation from Statistical Analysis of Profile

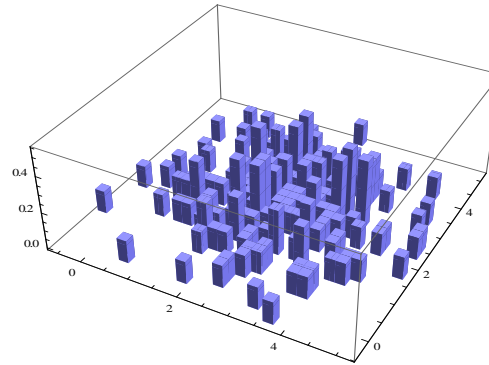
Gauss

2D PDF

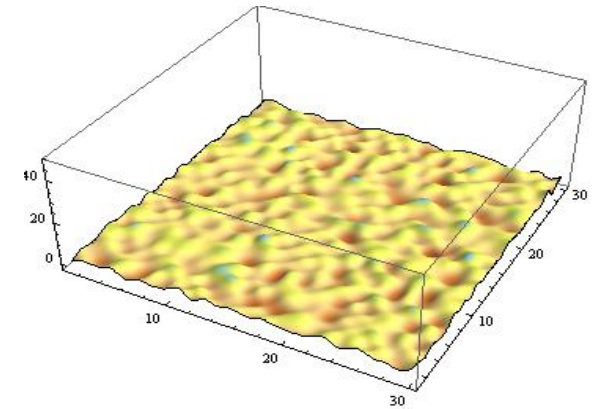
$$f_x(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$



3D PDF



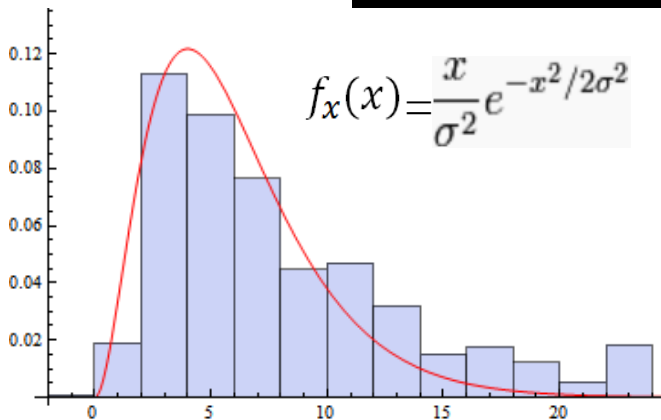
Generated Surfaces



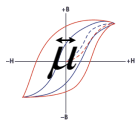
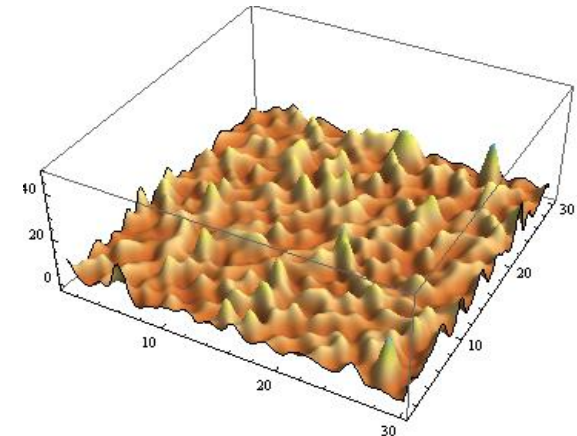
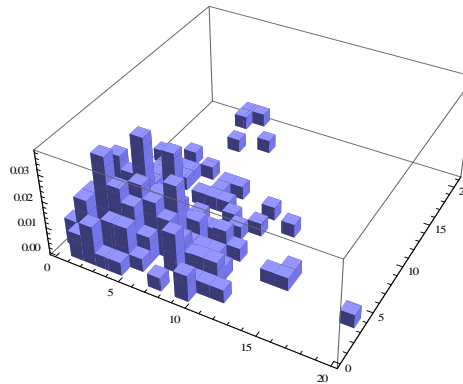
Oxide Side

Rayleigh

$$f_x(x) = \frac{x}{\sigma^2} e^{-x^2/2\sigma^2}$$



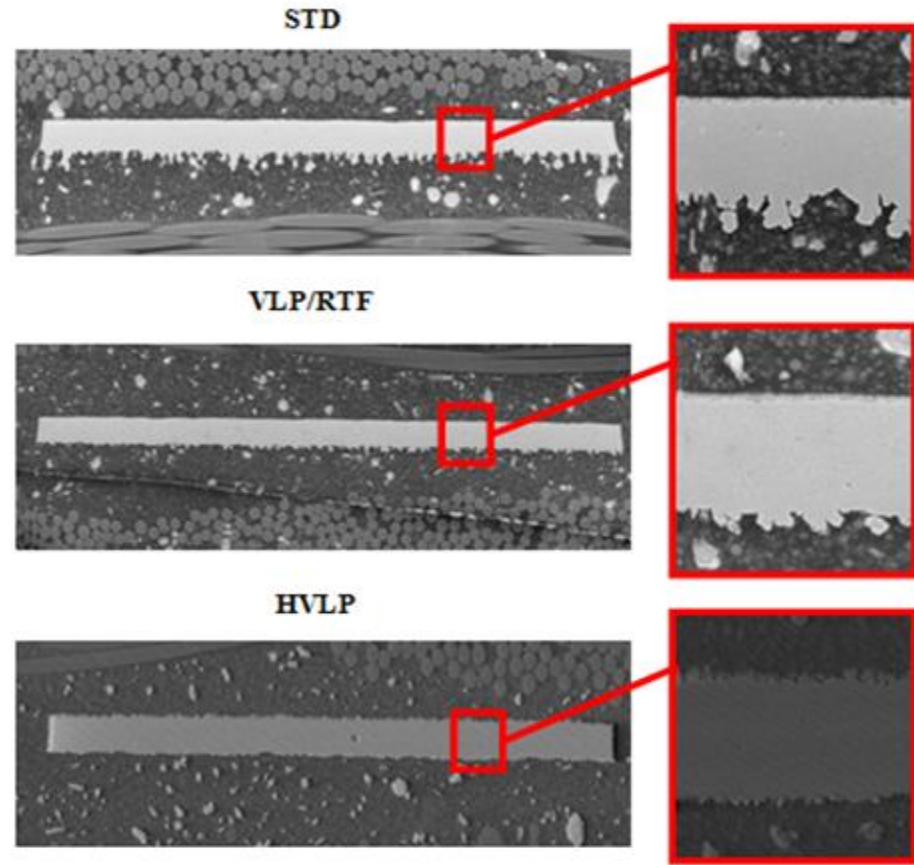
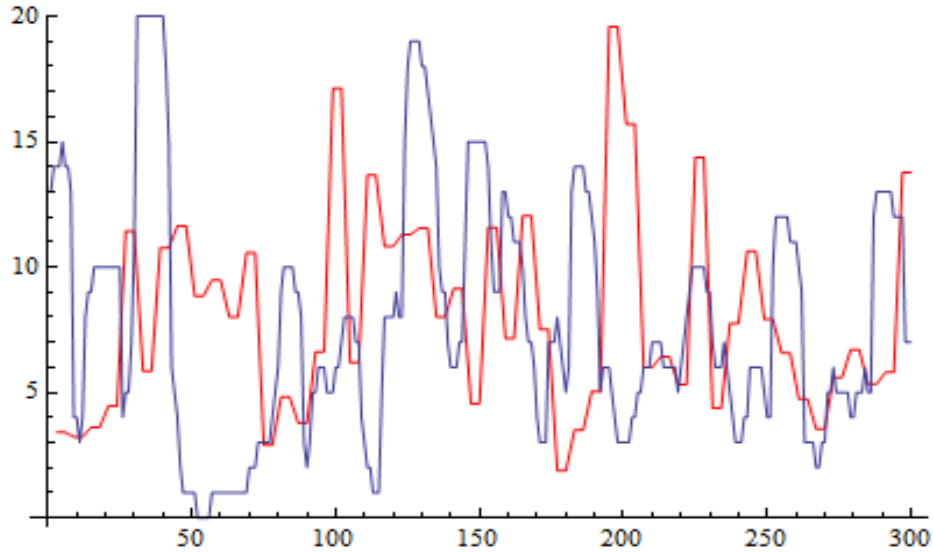
Foil Side





# Finding $A_r$ from PDF

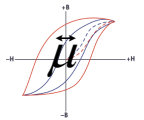
Side	STD	VLP	HVLP
Oxide	Gaussian	Gaussian	Gaussian
Foil	Rayleigh	Rayleigh	Gaussian



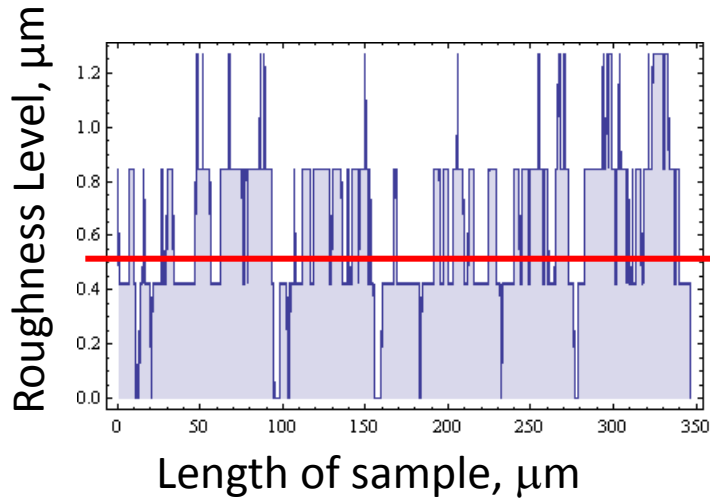
Blue line is measured from actual profile  
 Red line is generated from PDF

$$\text{mean}[\text{pixel}] \Rightarrow A_r = 2 \cdot \text{mean}[\text{pixel}] \cdot \text{pix}$$

$$\text{mean is } E[x] = \int_0^{\infty} x f_x(x) dx \Rightarrow A_r = 2 \cdot E[x] \cdot \text{pixel's value}$$



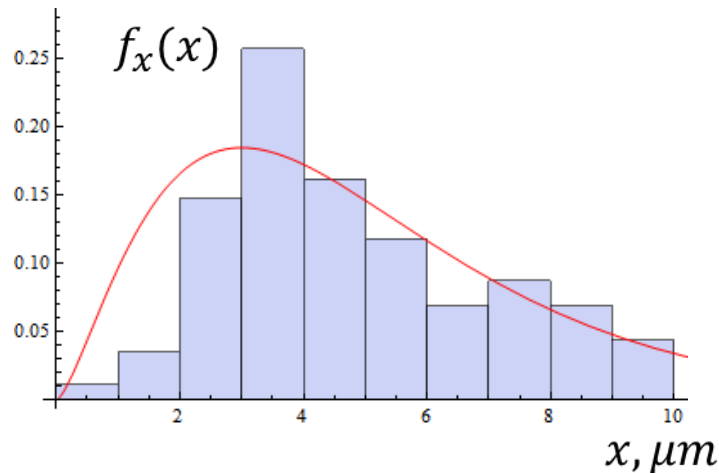
# Average Peak-to-Valley Roughness Amplitude and PDF



Mean



$$A_r = 2 \cdot E[x] \cdot \text{pixel's value}$$

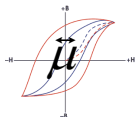
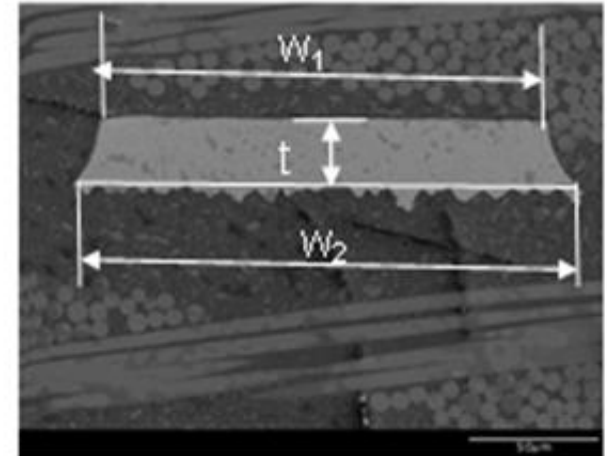
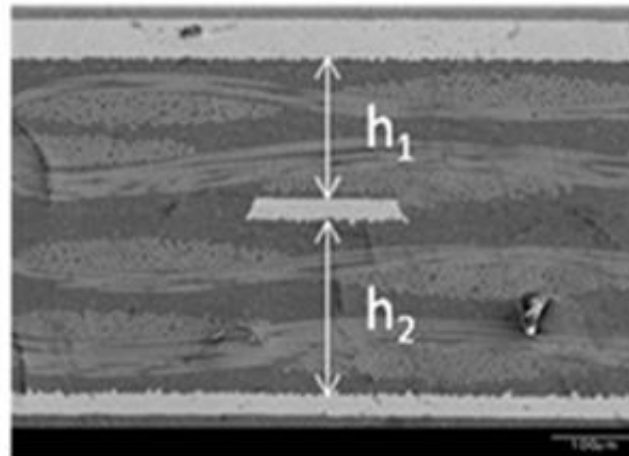


		STD	VLP	HVLP
Set 1	Oxide	0.862 $\mu\text{m}$	0.914 $\mu\text{m}$	0.863 $\mu\text{m}$
	Foil	6.250 $\mu\text{m}$	2.557 $\mu\text{m}$	1.234 $\mu\text{m}$
Set 2	Oxide	1.100 $\mu\text{m}$	1.195 $\mu\text{m}$	1.250 $\mu\text{m}$
	Foil	6.066 $\mu\text{m}$	3.430 $\mu\text{m}$	1.119 $\mu\text{m}$
Set 3	Oxide	1.318 $\mu\text{m}$	1.308 $\mu\text{m}$	1.778 $\mu\text{m}$
	Foil	6.169 $\mu\text{m}$	2.592 $\mu\text{m}$	1.217 $\mu\text{m}$

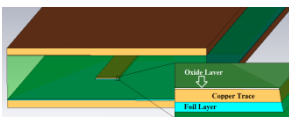
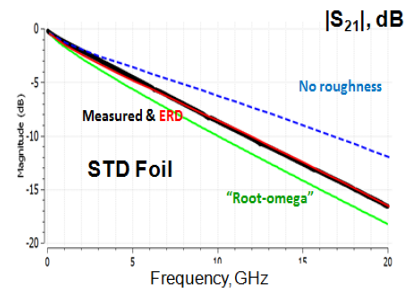
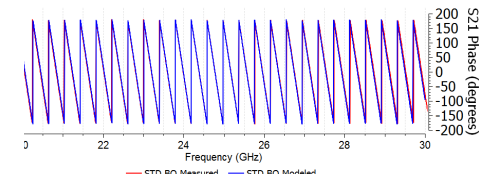
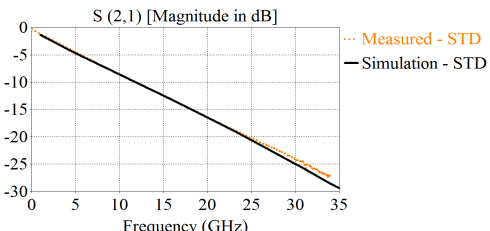
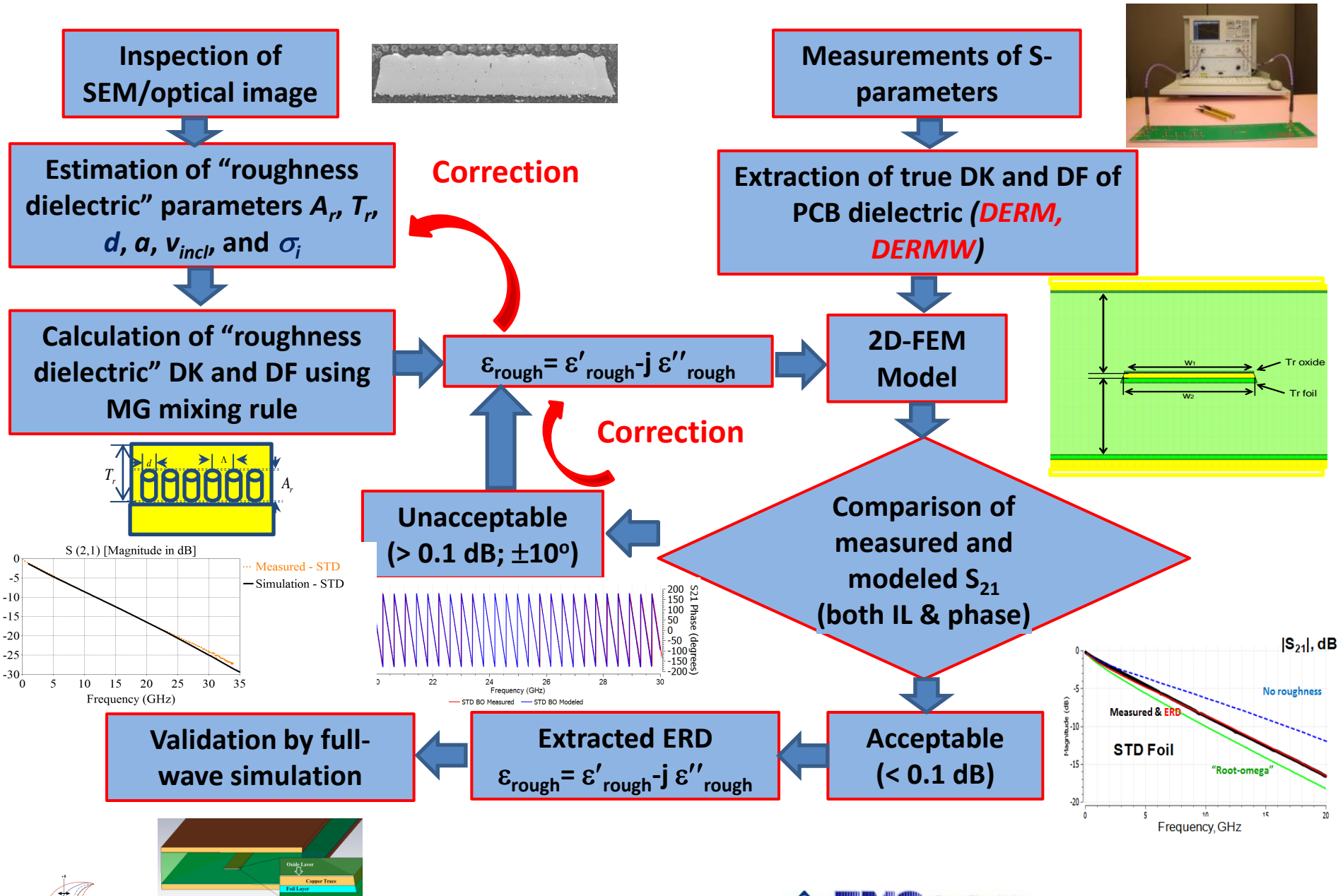
# Geometry and Roughness Parameters of Some Test Samples with Different Foils

	$w_1, \mu\text{m}$	$w_2, \mu\text{m}$	$H, \mu\text{m}$	$P, \mu\text{m}$	$h_1, \mu\text{m}$	$h_2, \mu\text{m}$	$A_{r1}, \mu\text{m}$	$A_{r2}, \mu\text{m}$	$\Lambda_1, \mu\text{m}$	$\Lambda_2, \mu\text{m}$	$QR_1$	$QR_2$	QR
STD	337.9	343.2	16.44	712.8	308	286	0.85	6.2	25	14.2	0.034	0.44	0.474
VLP	364.3	368.5	16.8	769	308	286.4	0.87	2.38	24.7	13	0.035	0.18	0.215
HVLP	329.3	331.3	15.3	691.7	303	292	1.25	1.13	14.3	19.2	0.087	0.06	0.147

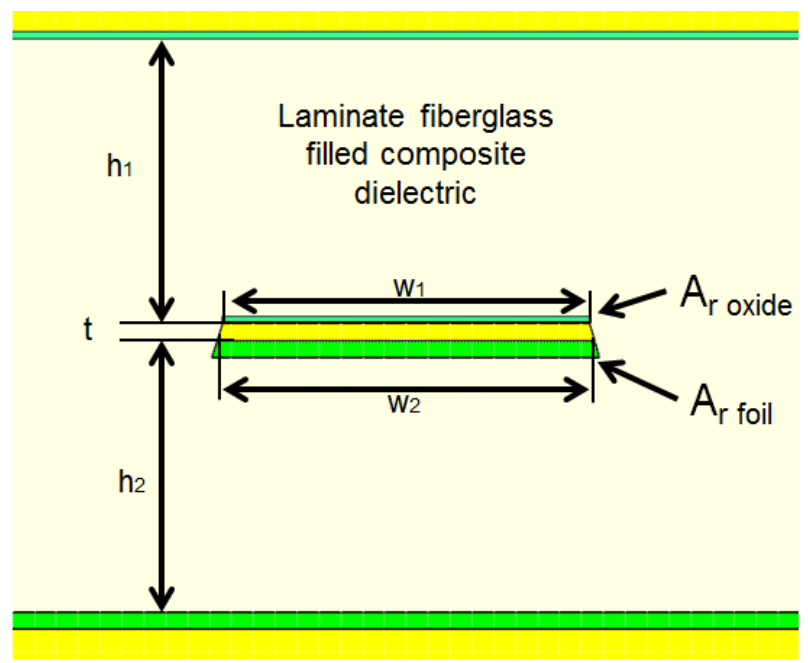
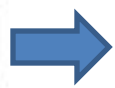
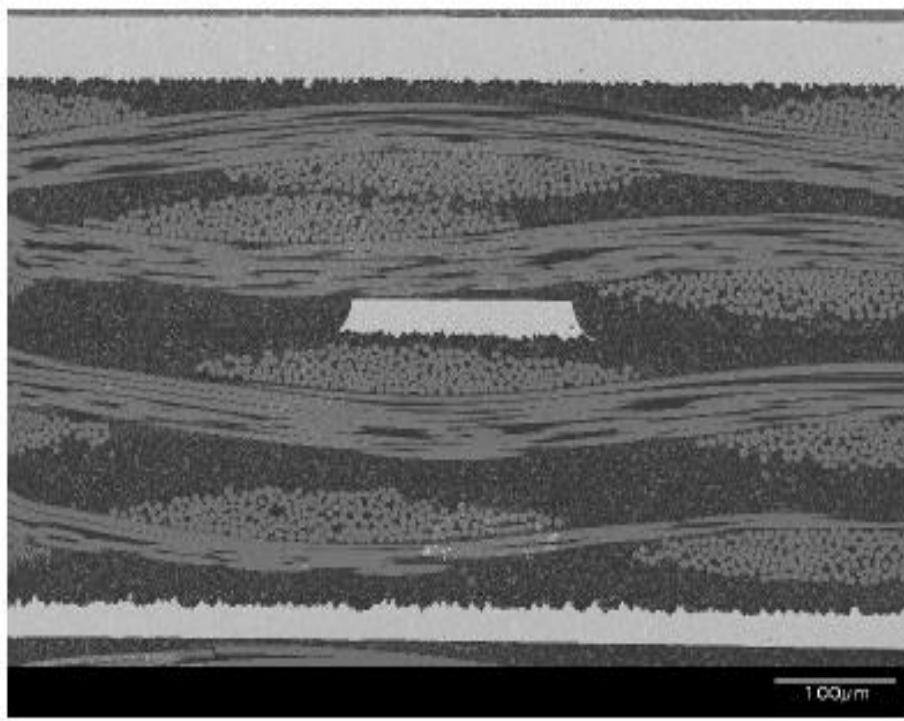
The presented samples have almost the same cross-sectional geometry, but different copper foil roughness profiles.



# “Effective Roughness Dielectric” Extraction



# Numerical Model Setup Using ERD Layers



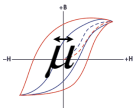
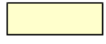
Copper foil conductors



Effective 'roughness dielectric'



Laminate dielectric



# Spectral Approach to Propagation Constant

$$\alpha_T = K_1 \sqrt{\omega} + K_2 \omega + K_3 \omega^2 + K_{r1} \sqrt{\omega} + K_{r2} \omega + K_{r3} \omega^2$$

Smooth conductor loss + Dielectric loss + Loss due to conductor roughness

Curve-fit data behaves as  $\sqrt{\omega}, \omega$  &  $\omega^2$

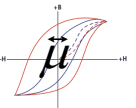
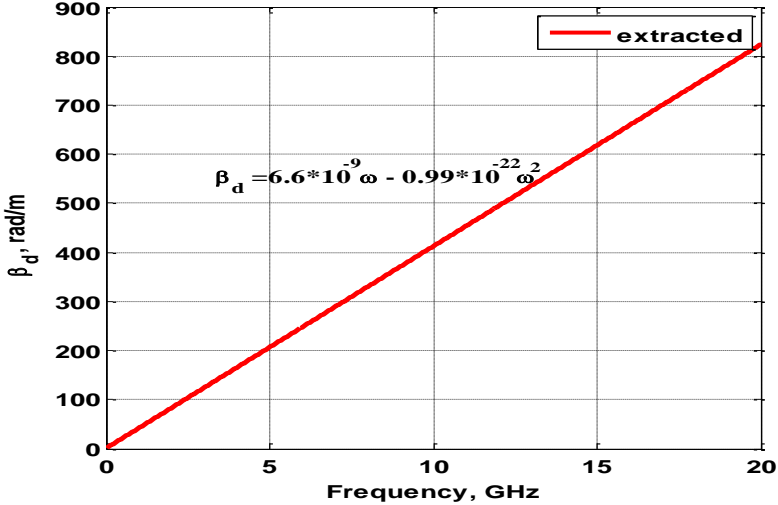
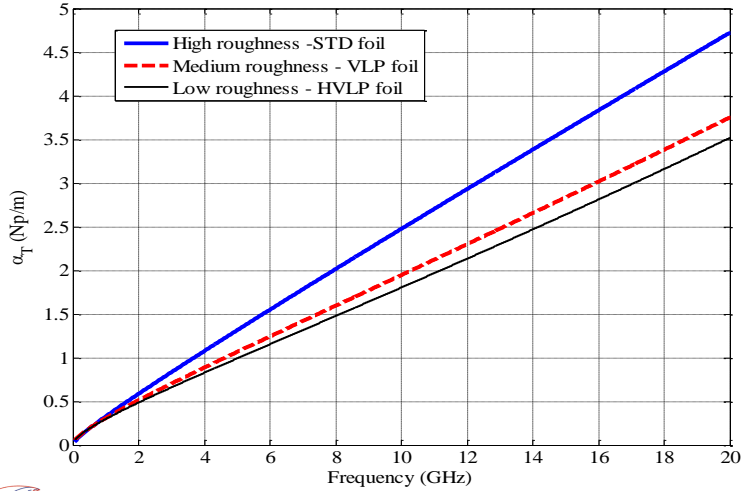
$$\alpha_T = \alpha_c + \alpha_d$$

$$\beta_T = B_1 \sqrt{\omega} + B_2 \omega + B_3 \omega^2 + B_{r1} \sqrt{\omega} + B_{r2} \omega + B_{r3} \omega^2$$

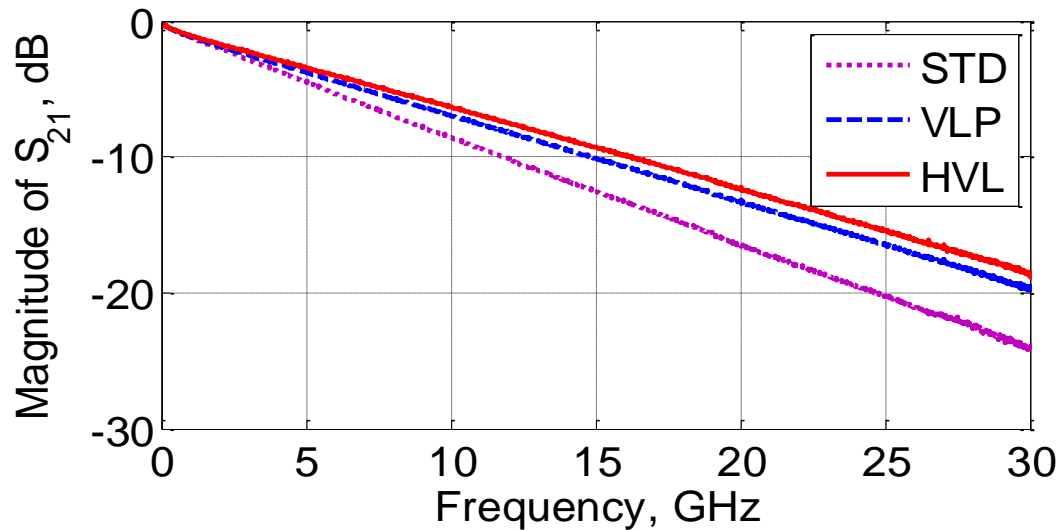
Due to skin depth in conductor + Due to propagation in the dielectric + Due to conductor roughness

Curve-fit data behaves as  $\sqrt{\omega}, \omega$  &  $\omega^2$

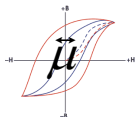
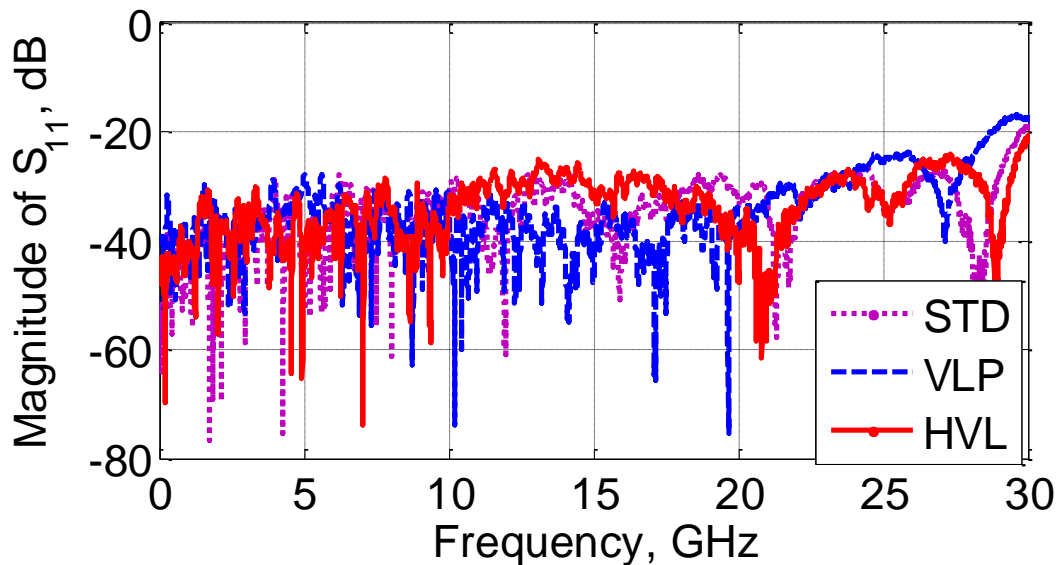
$$\beta_T = \beta_c + \beta_d$$



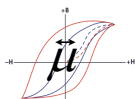
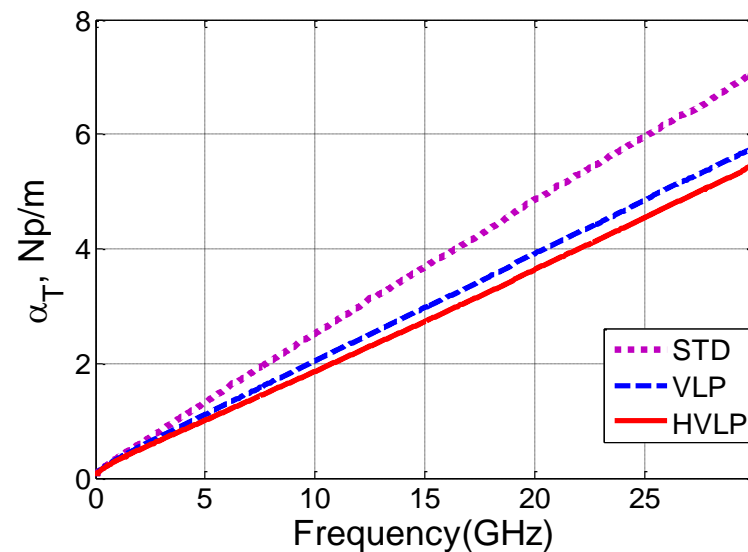
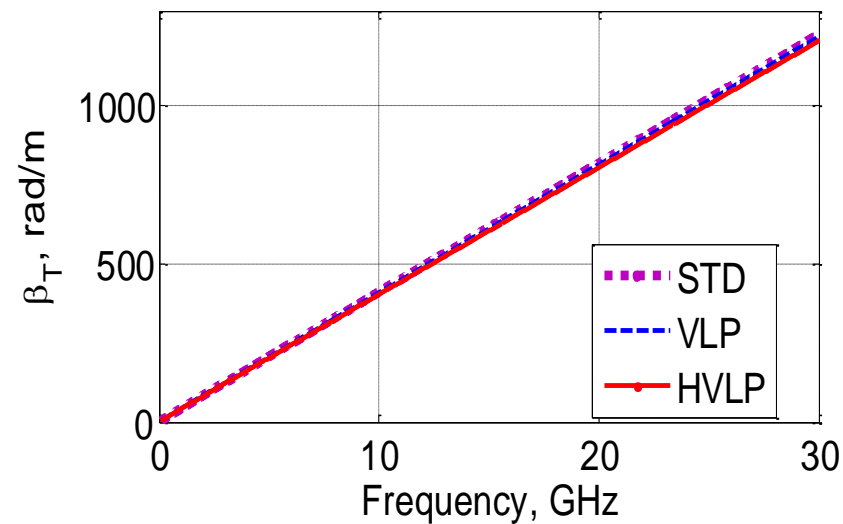
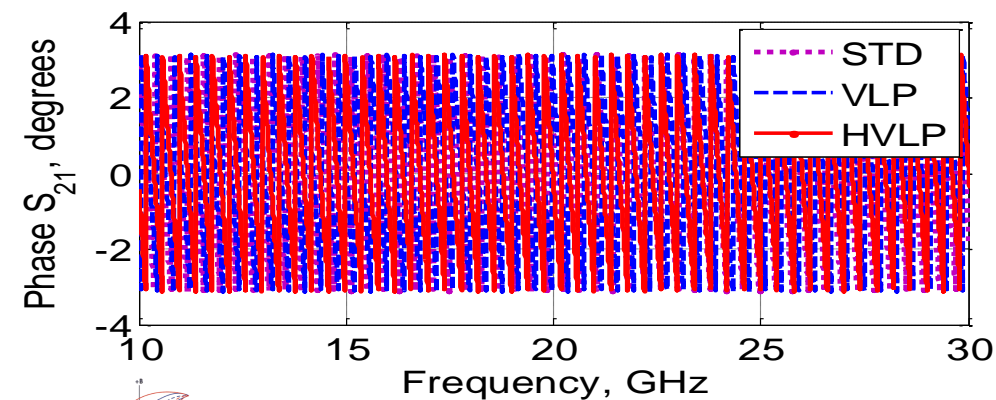
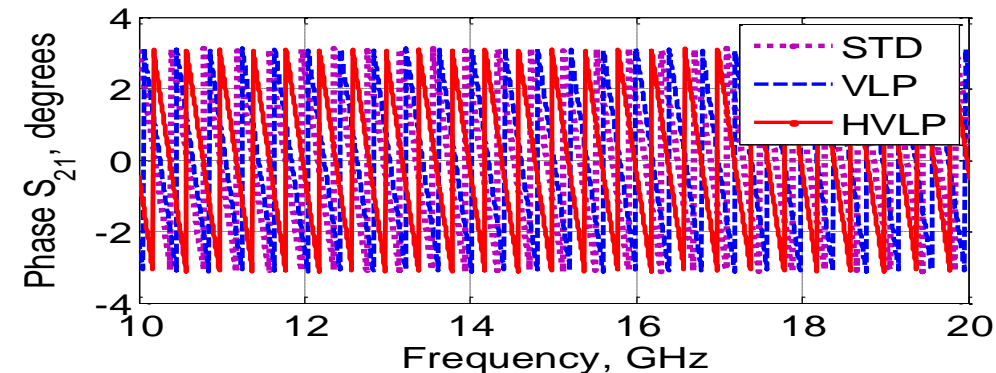
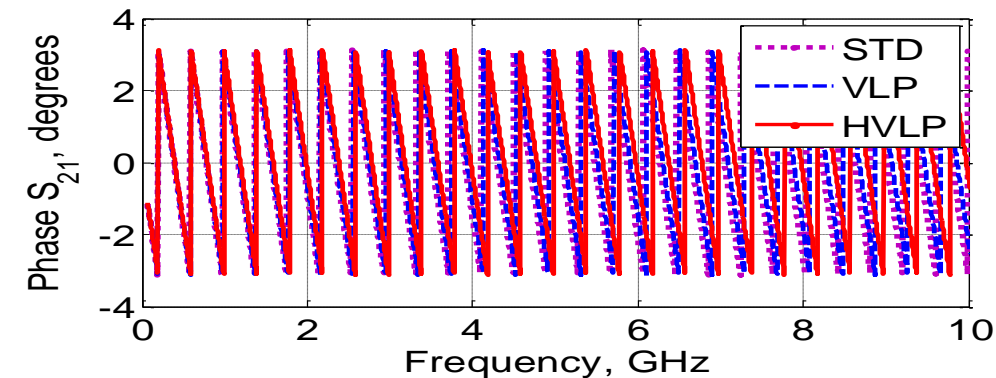
# Measured Magnitudes of $S_{11}$ and $S_{21}$



- Length of all the test striplines =15,410 mils.
- Striplines are 13 mils wide.
- Laminate dielectric and cross-sectional geometry are the same for all the boards.

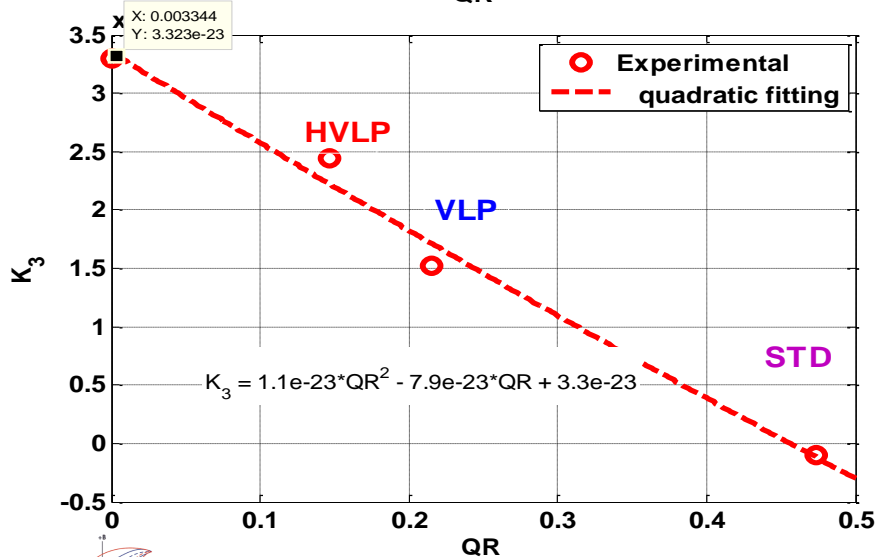
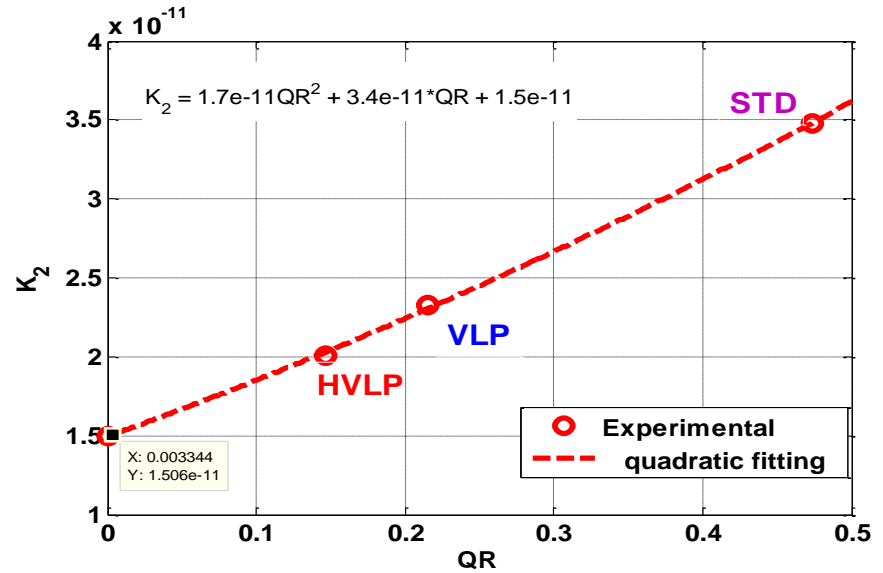
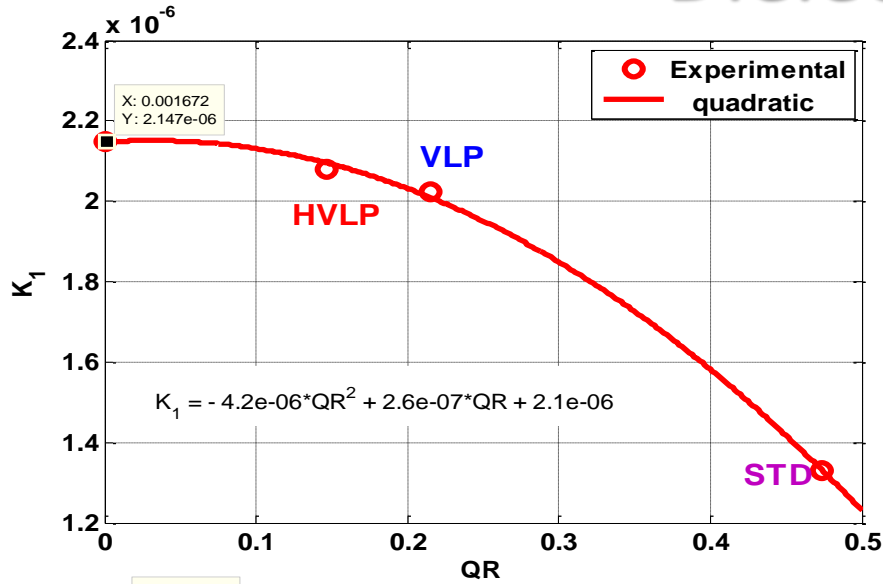


# Measured Phase of $S_{21}$ and Propagation Constant



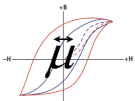


# Extrapolation to Zero Roughness in $\alpha$ to Refine Dielectric Loss

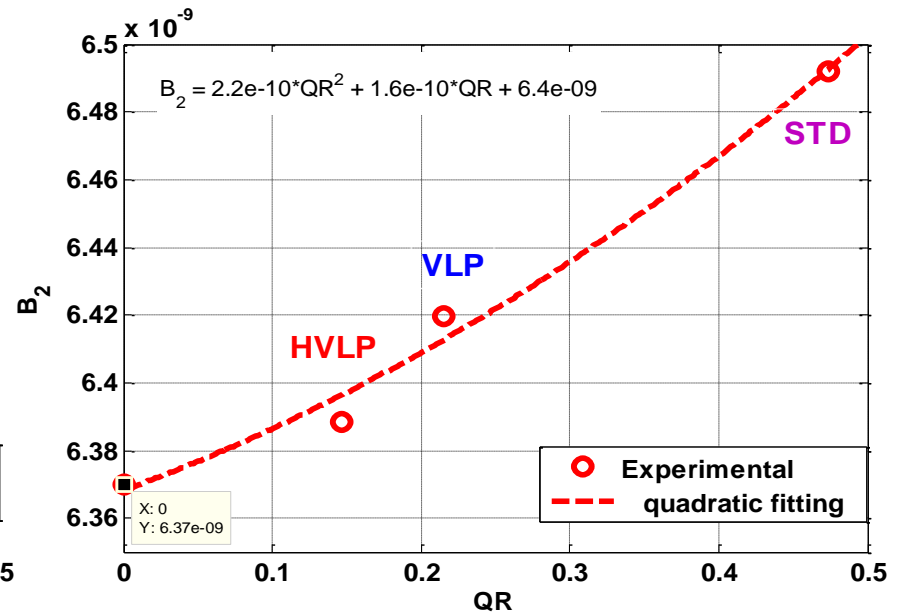
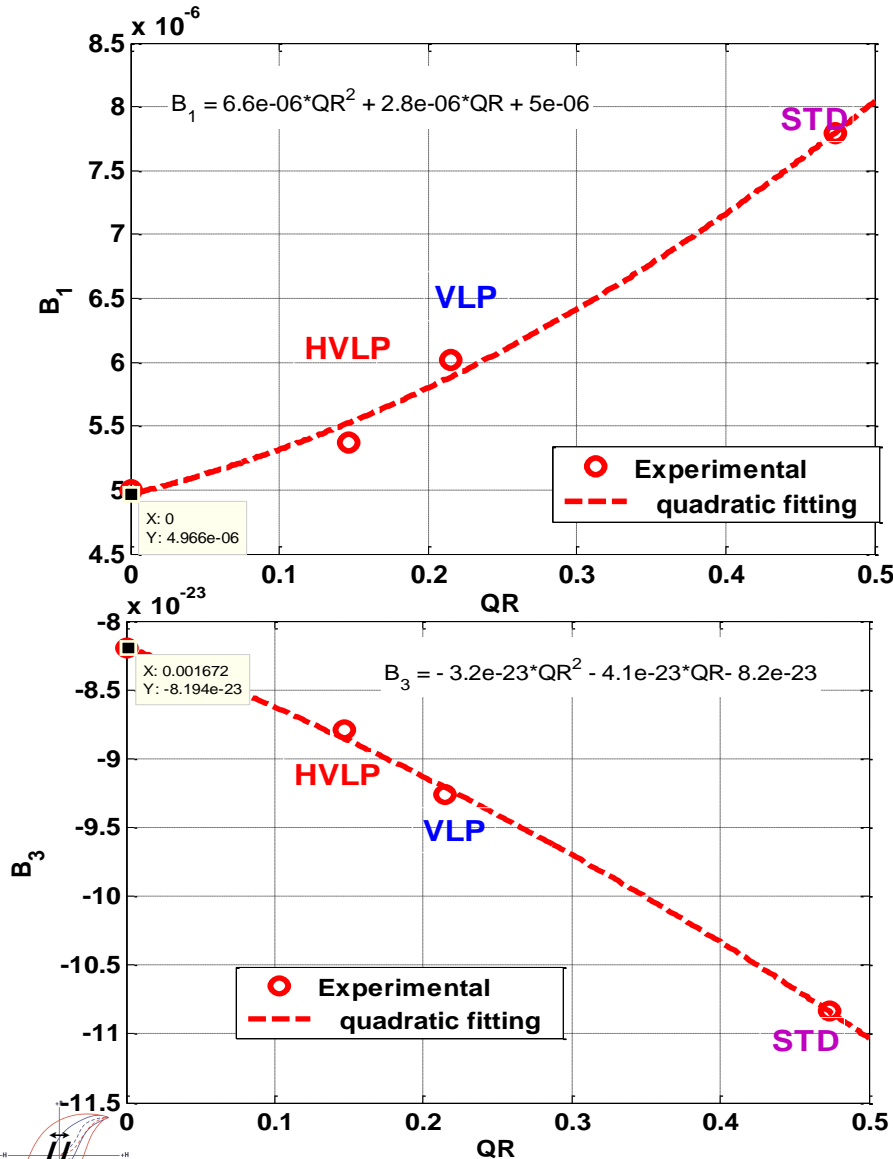


$$\alpha_{c0} = 2.15 \times 10^{-6} \sqrt{\omega}$$

$$\alpha_d = 1.51 \times 10^{-11} \omega + 3.3 \times 10^{-23} \omega^2$$

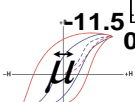


# Extrapolation to Zero Roughness in $\beta$ to Refine Dielectric-Related Phase Constant

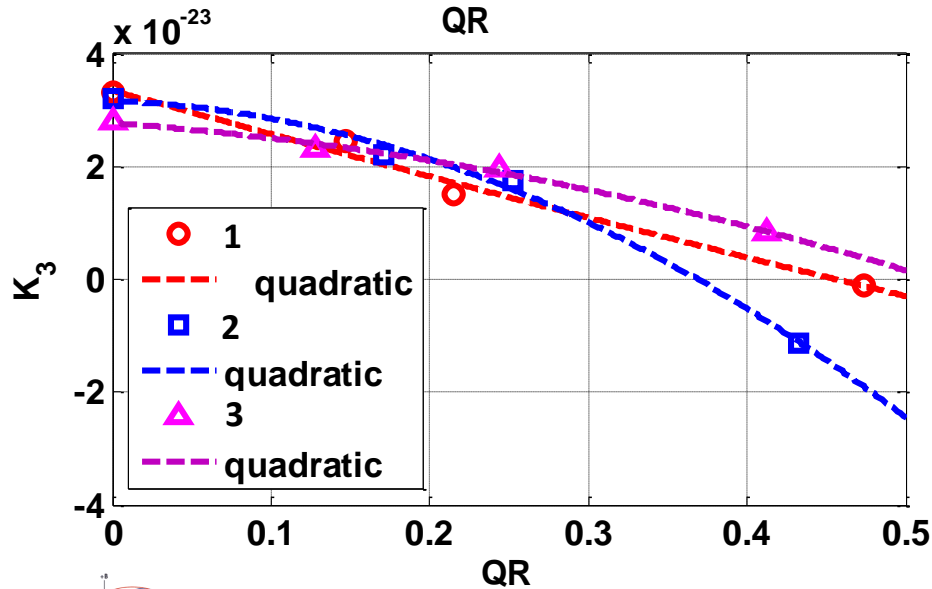
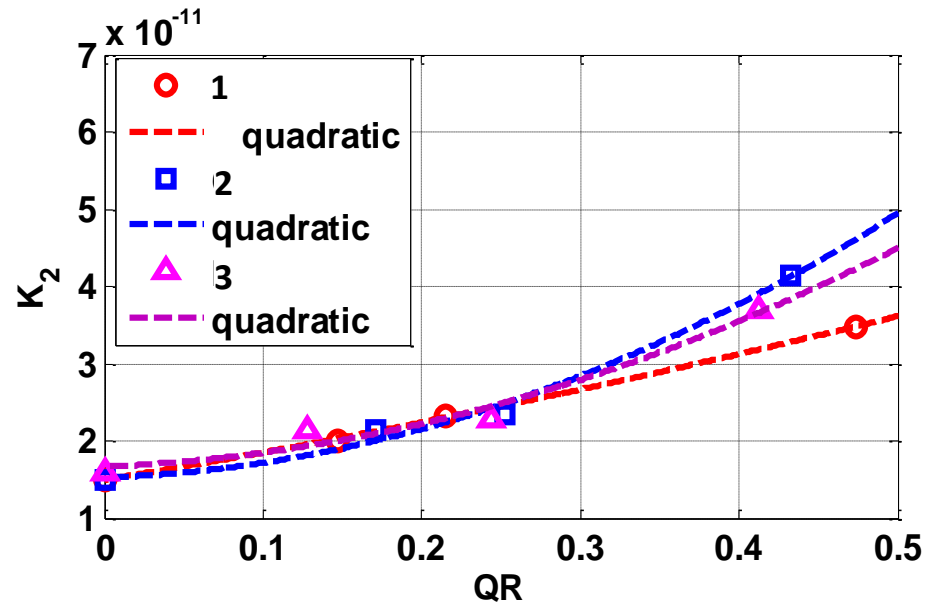
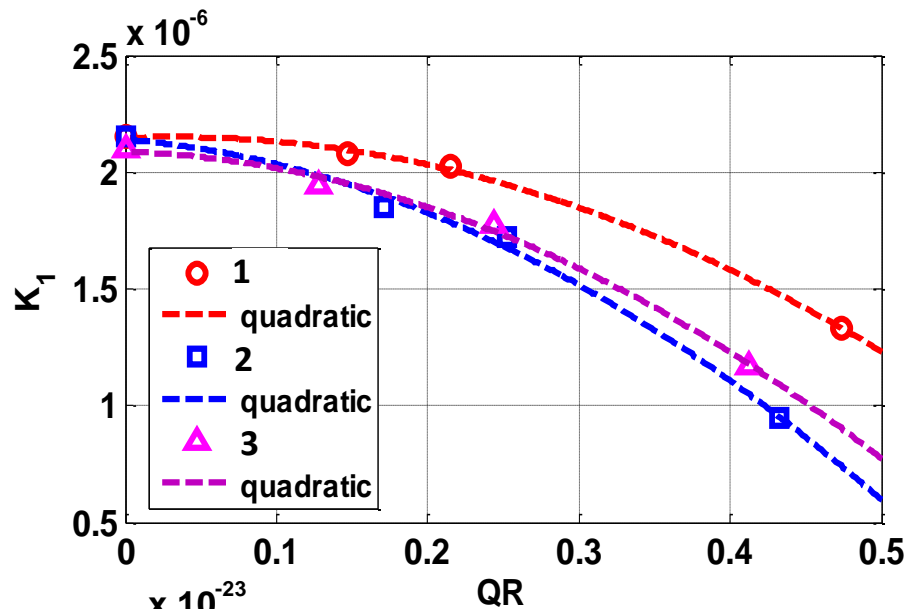


$$\beta_c = 5.0 \times 10^{-6} \sqrt{\omega}$$

$$\beta_d = 6.37 \times 10^{-9} \omega - 0.82 \times 10^{-23} \omega^2$$



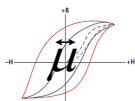
# Additional Procedure to Refine Dielectric Loss (with Two other Sets of Test Vehicles with Different Types of Foil)



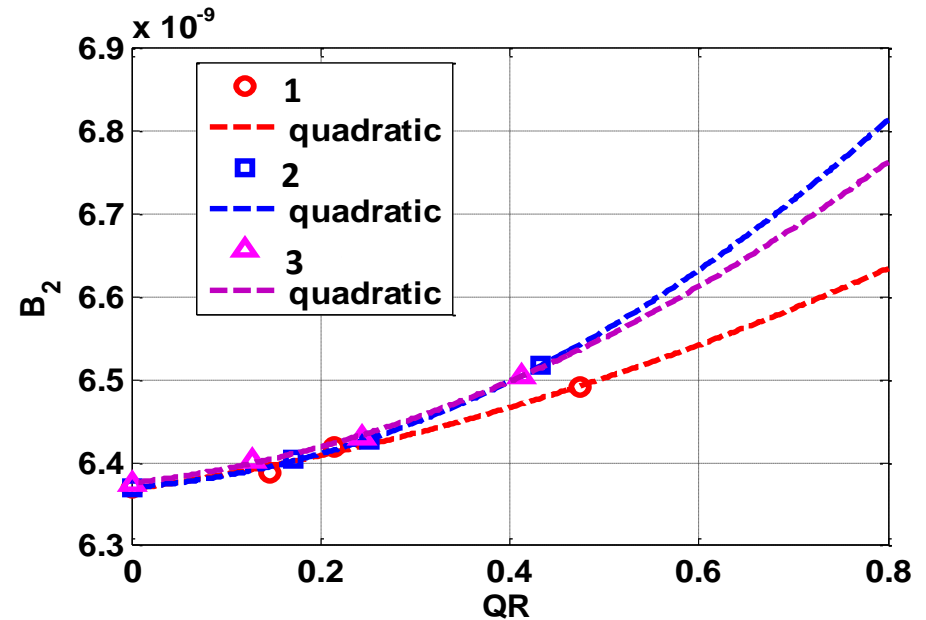
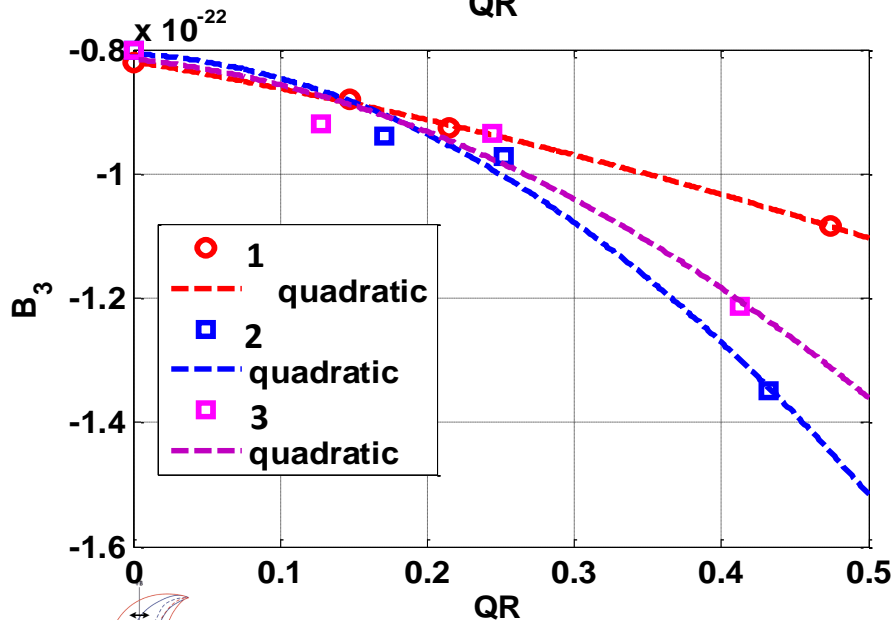
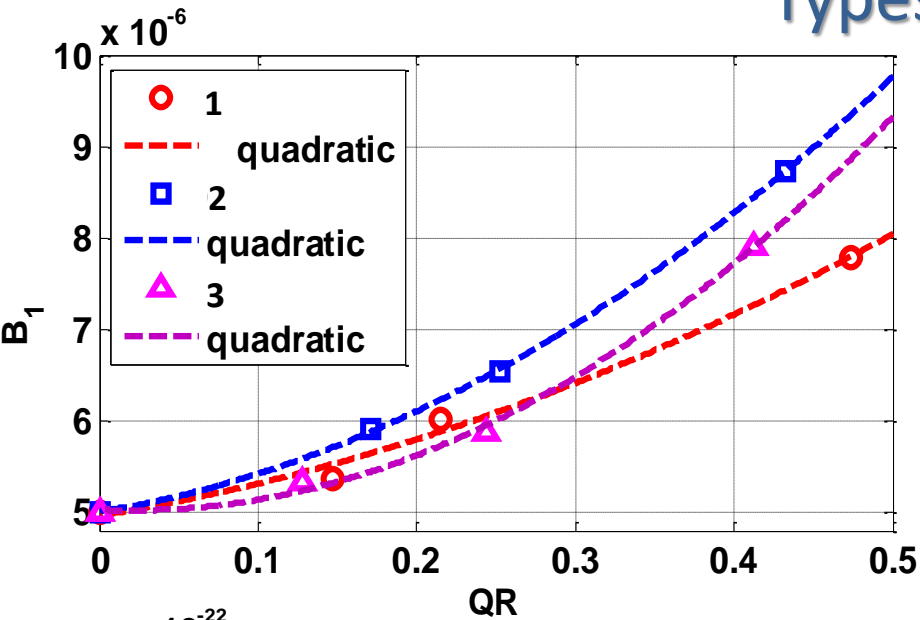
This increases accuracy of extraction.

$$\alpha_{c0} = 2.15 \times 10^{-6} \sqrt{\omega}$$

$$\alpha_d = 1.5 \times 10^{-11} \omega + 3.0 \times 10^{-23} \omega^2$$



# Additional Procedure to Refine Phase Constant (with Two other Types of Foil)



This increases accuracy of extraction.

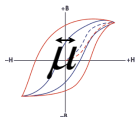
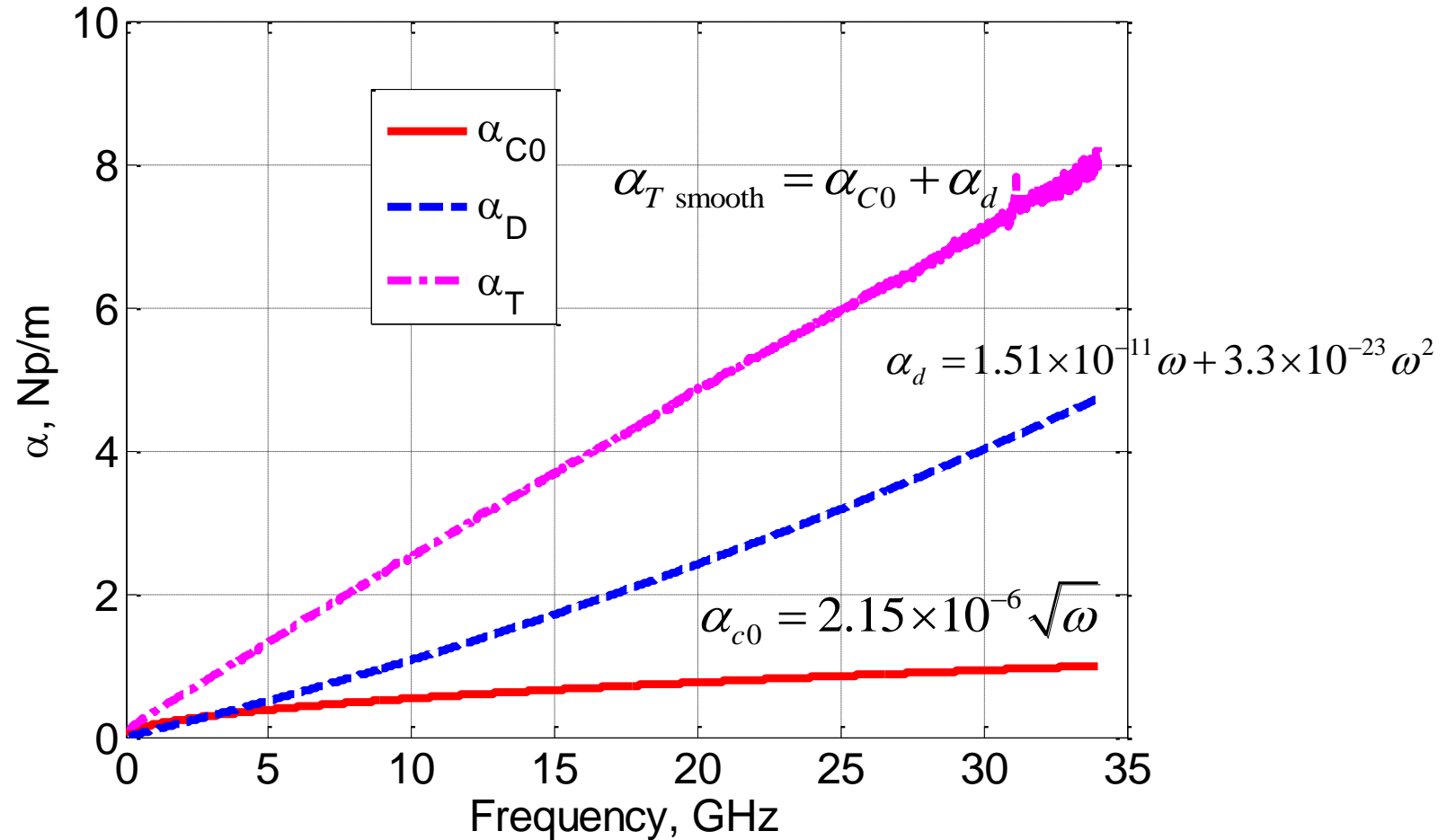
$$\beta_c = 5.0 \times 10^{-6} \sqrt{\omega}$$

$$\beta_d = 6.38 \times 10^{-9} \omega - 0.8 \times 10^{-23} \omega^2$$



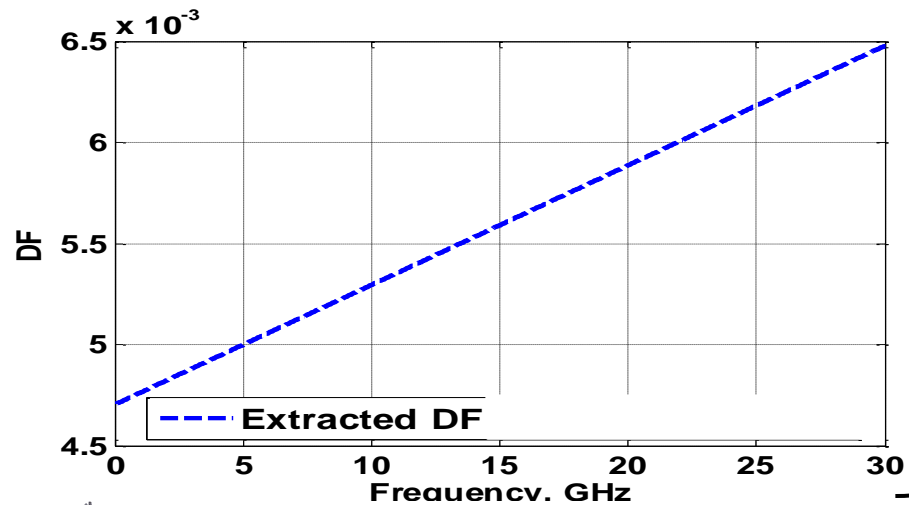
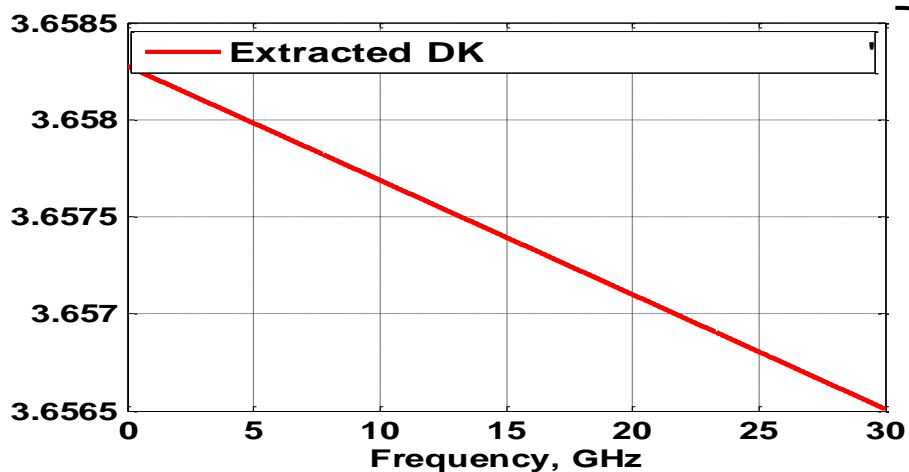
# Extracted Loss in a Smooth Conductor

(Roughness Parts are Removed)

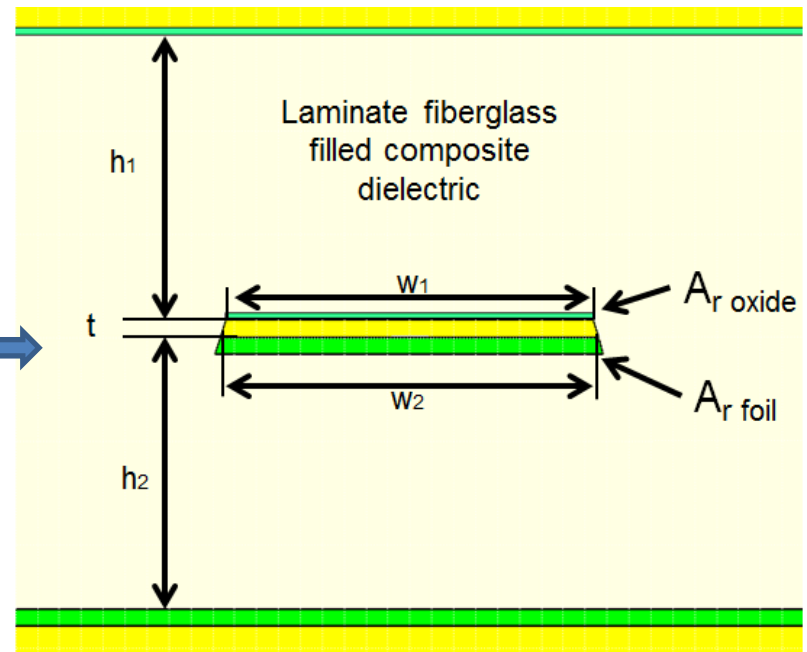


# Extracted Dielectric Properties of PCB Laminate Substrate

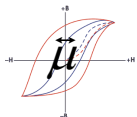
The refined dielectric data (DK and DF) for all the test vehicles is used in numerical electromagnetic modeling (2D-FEM)



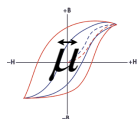
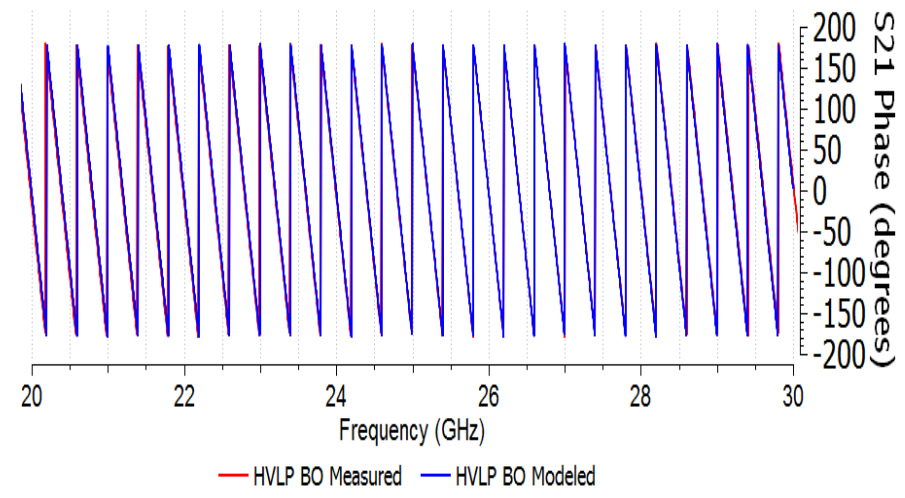
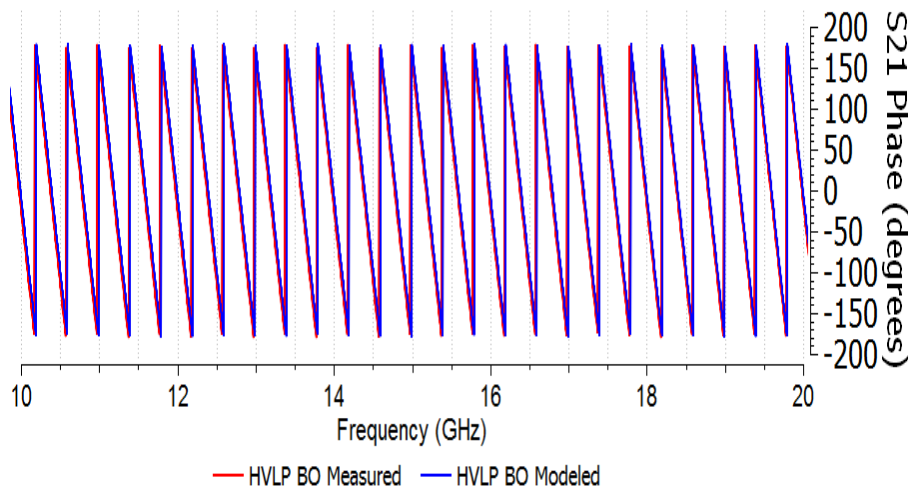
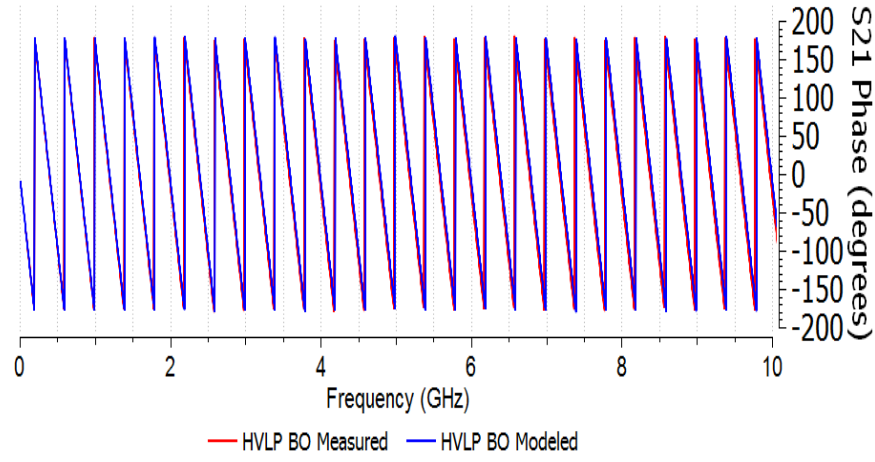
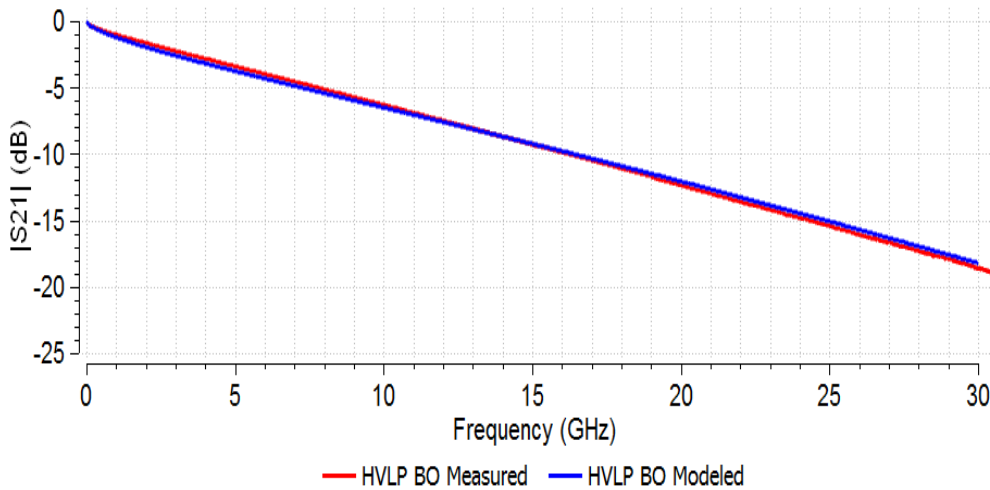
Numerical model 1: Ansoft Q2D (2DFEM)



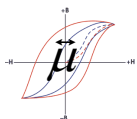
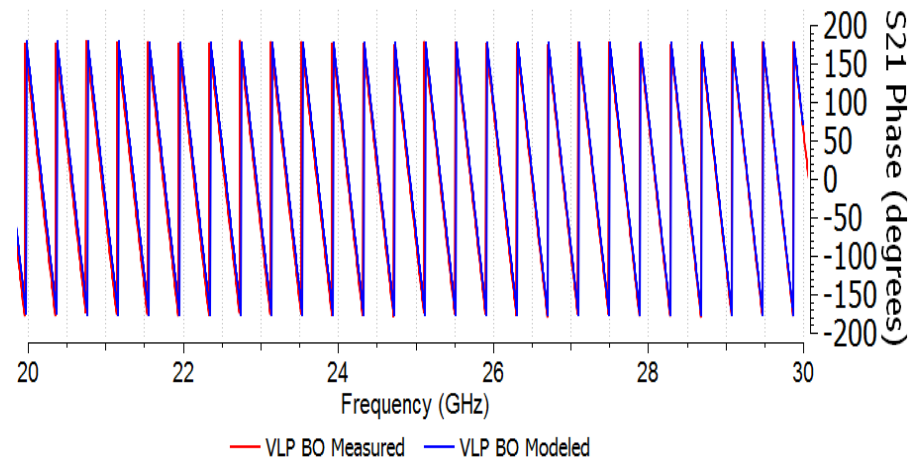
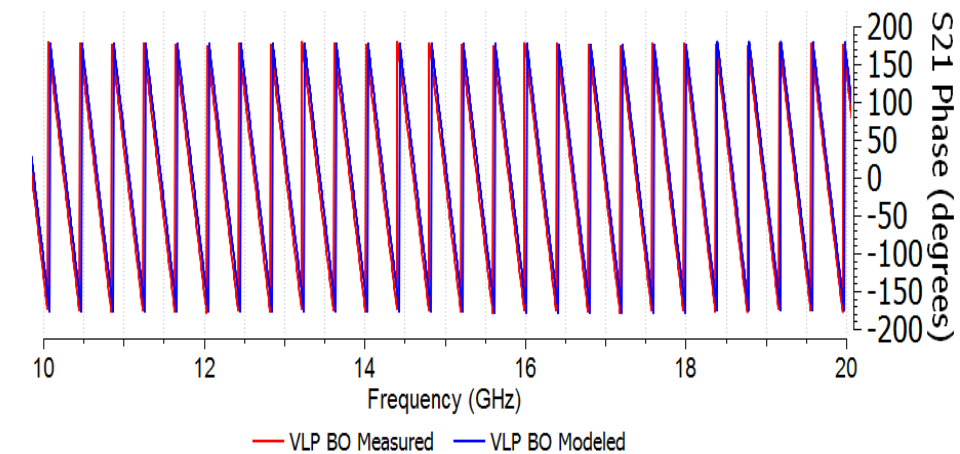
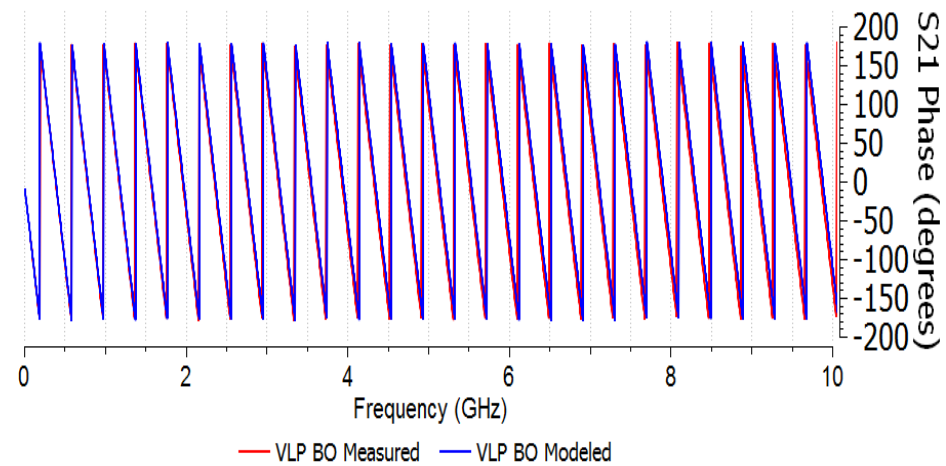
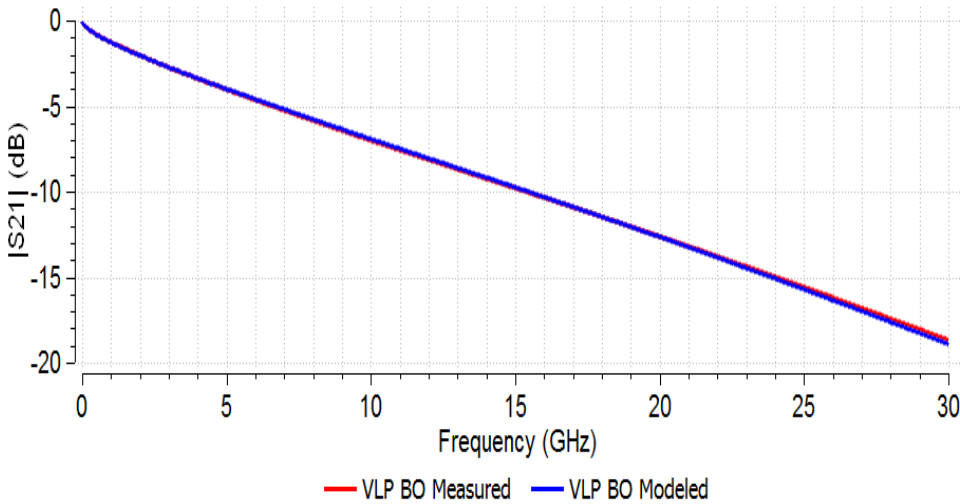
This model is used to extract parameters of Effective Roughness Dielectric (ERD): bright-green layers



# Modeled & Measured $S_{21}$ for Stripline with HVLP Foil (Q2D)

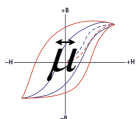
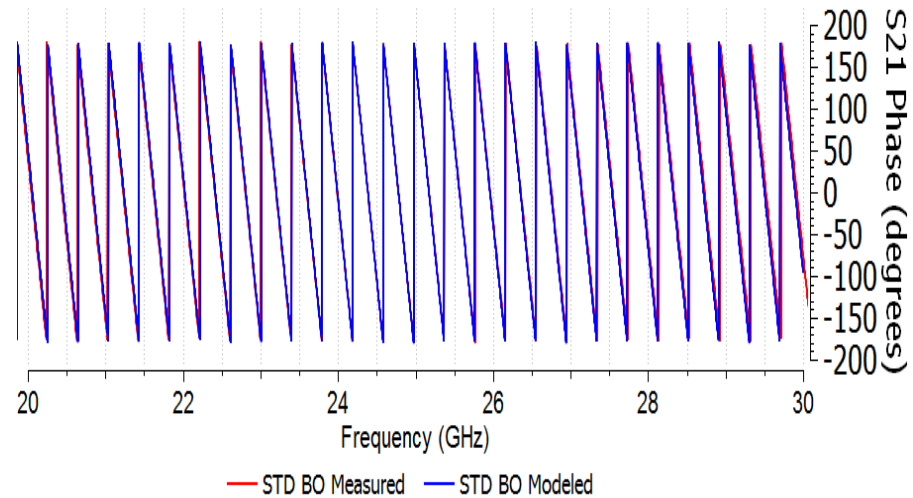
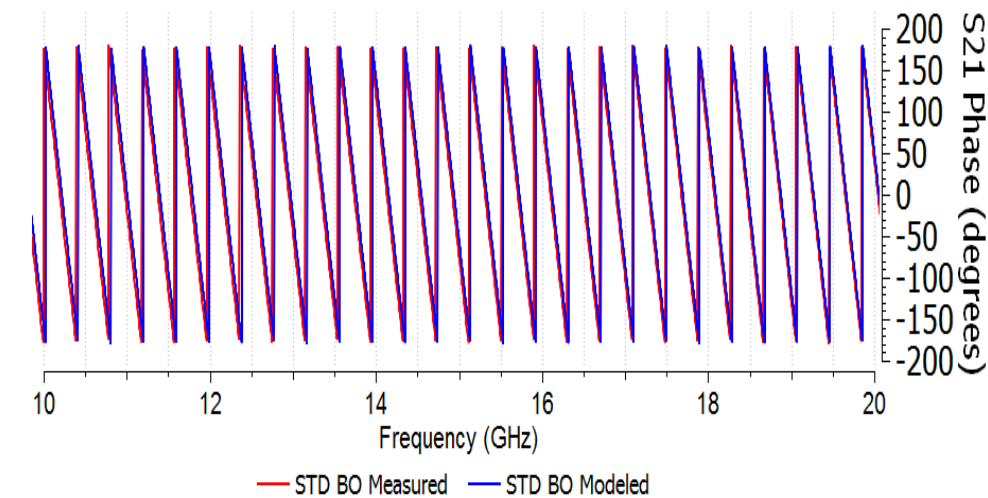
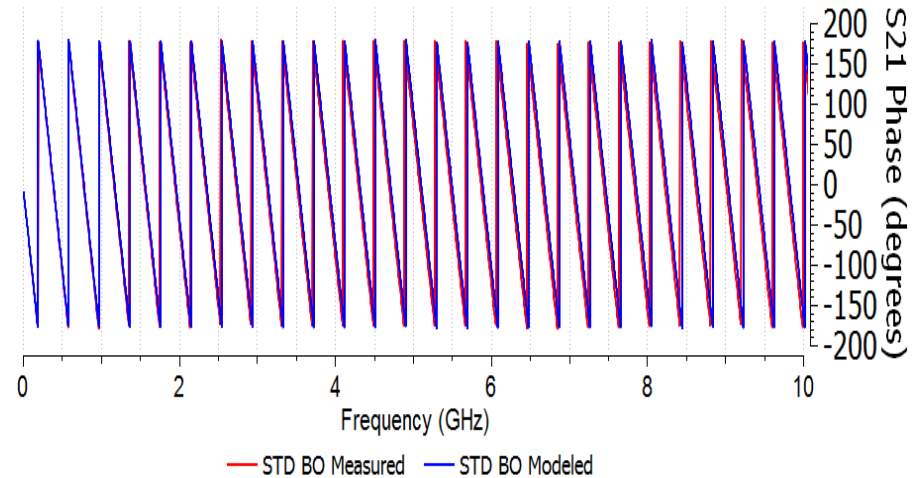
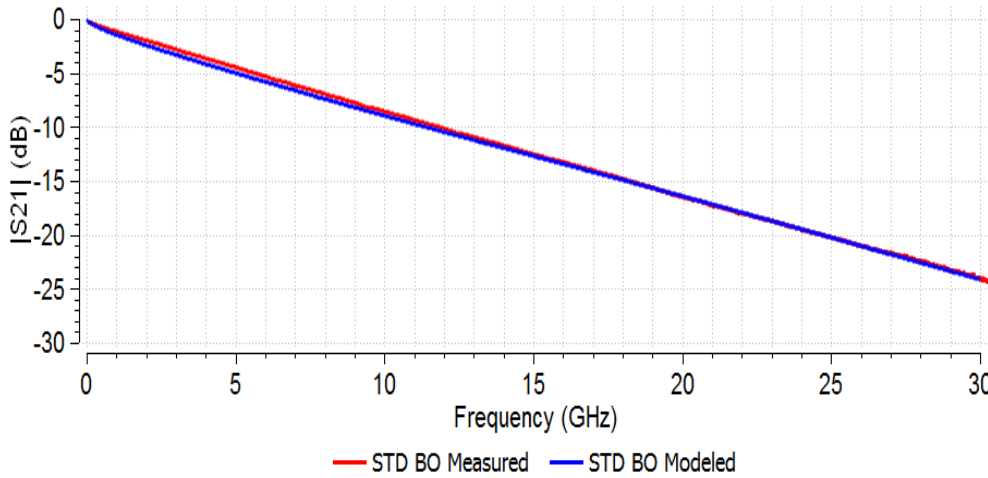


# Modeled & Measured $S_{21}$ for Stripline with VLP Foil (Q2D)





# Modeled & Measured $S_{21}$ for Stripline with STD Foil (Q2D)



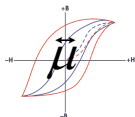
# Extracted Properties of Effective Roughness

## Dielectric

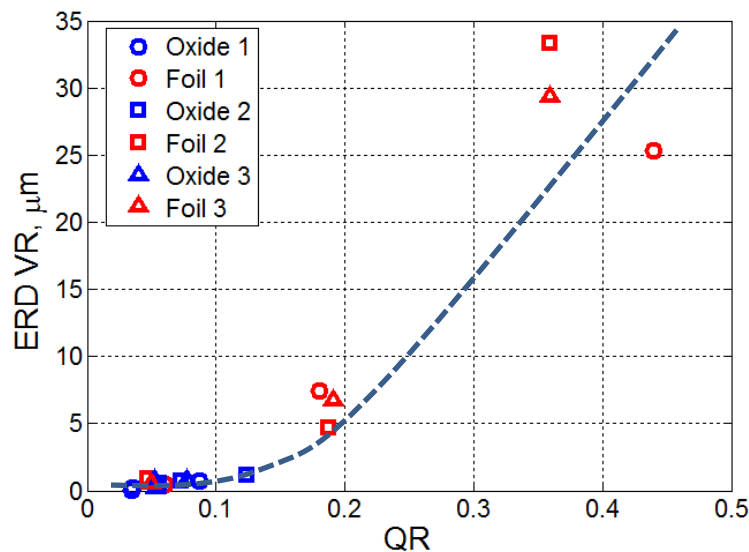
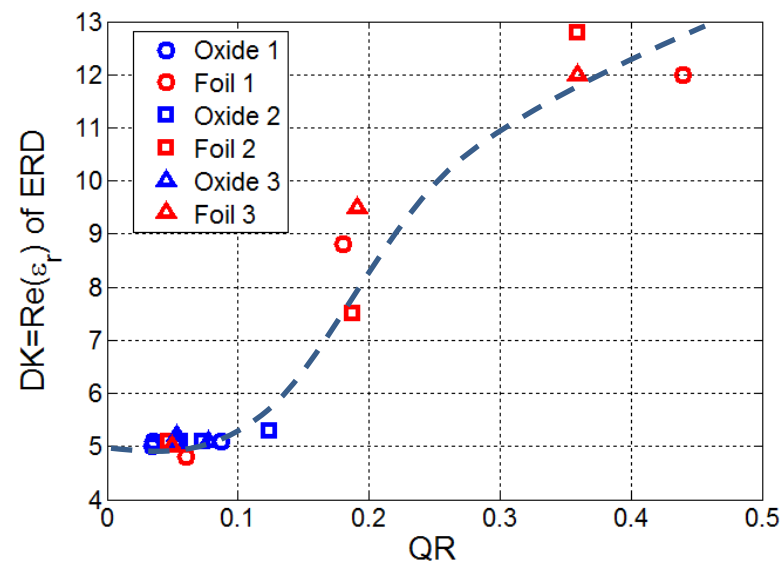
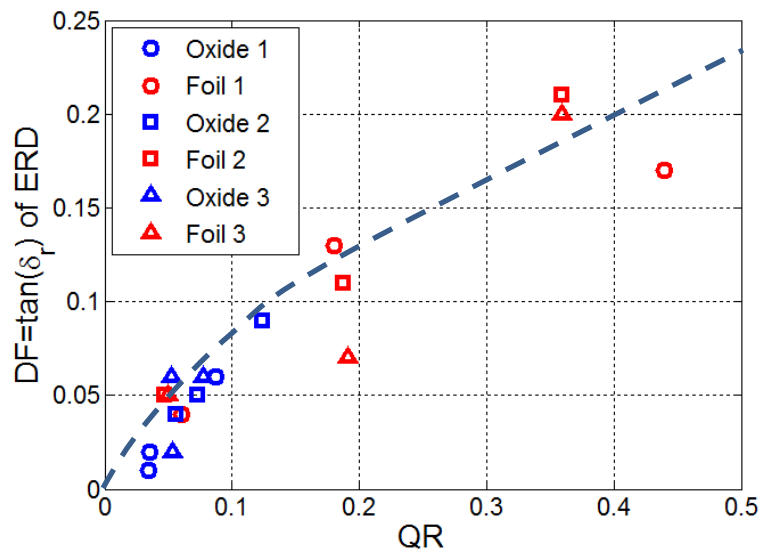
The refined dielectric data (DK and DF) for all the test vehicles is used in numerical electromagnetic modeling (2D-FEM)

### Set 1

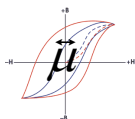
Foil Type	$T_{r1}$ (ox), $\mu\text{m}$	$T_{r2}$ (foil), $\mu\text{m}$	$\tan\delta_r$ (ox)	$\tan\delta_r$ (foil)	$\epsilon_r$ (ox)	$\epsilon_r$ (foil)	QR (ox)	QR (foil)	VR (ox), $\mu\text{m}$	VR (foil), $\mu\text{m}$
<b>STD</b>	<b>1.7</b>	<b>12.4</b>	<b>0.01</b>	<b>0.17</b>	<b>5.0</b>	<b>12.0</b>	<b>0.034</b>	<b>0.44</b>	<b>0.085</b>	<b>25.30</b>
<b>VLP</b>	<b>1.74</b>	<b>4.76</b>	<b>0.02</b>	<b>0.13</b>	<b>5.1</b>	<b>9.0</b>	<b>0.035</b>	<b>0.18</b>	<b>0.178</b>	<b>7.42</b>
<b>HVLP</b>	<b>2.50</b>	<b>2.26</b>	<b>0.06</b>	<b>0.04</b>	<b>5.1</b>	<b>4.8</b>	<b>0.087</b>	<b>0.06</b>	<b>0.765</b>	<b>0.433</b>



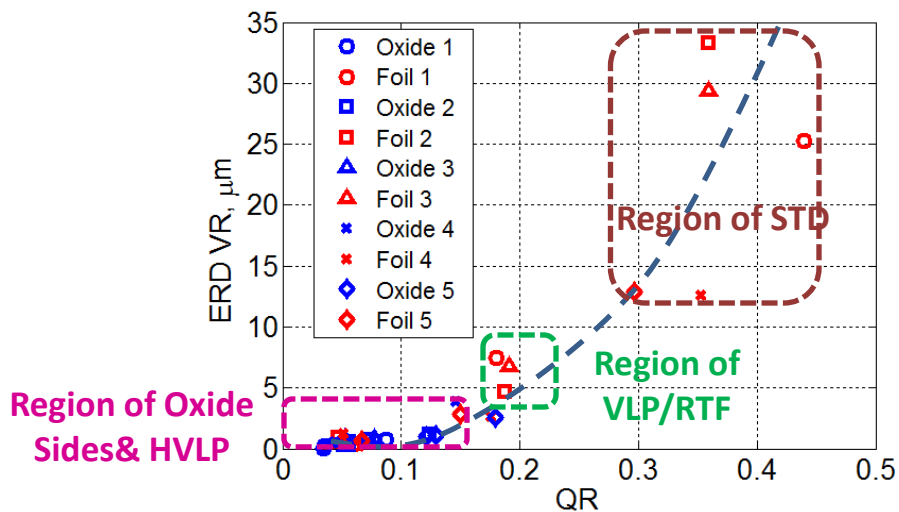
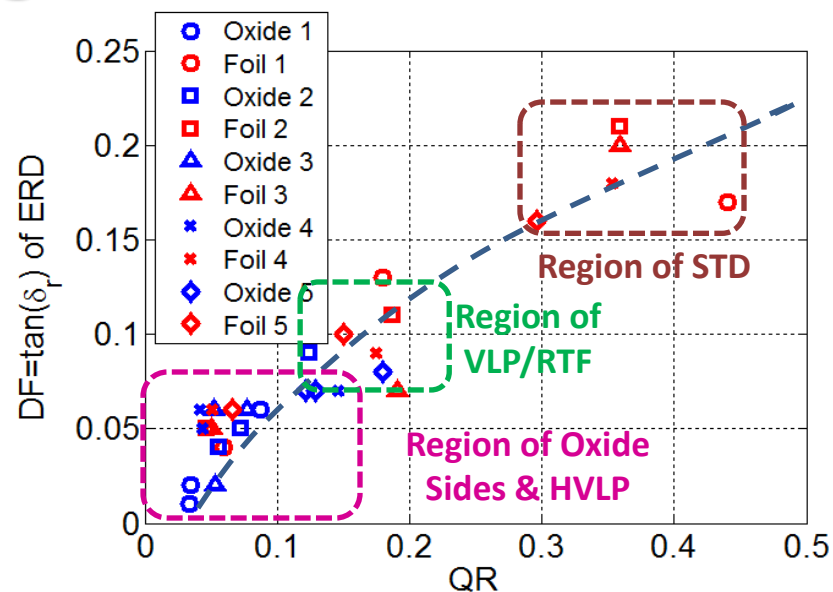
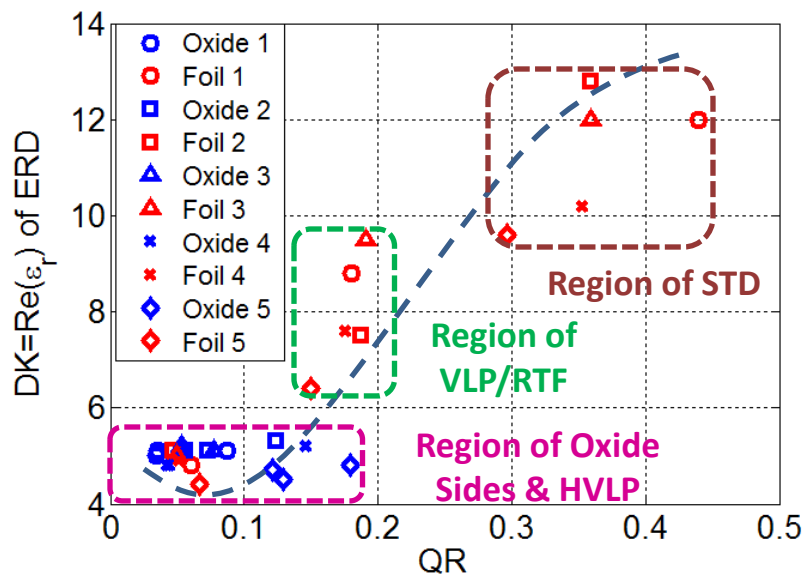
# Effective Roughness Dielectric Parameters as a Function of Roughness Factor



$$VR = \epsilon_r'' \times T_r = \epsilon_r' \times \tan \delta_r \times T_r$$



# Effective Roughness Dielectric Parameters as a Function of Roughness Factor



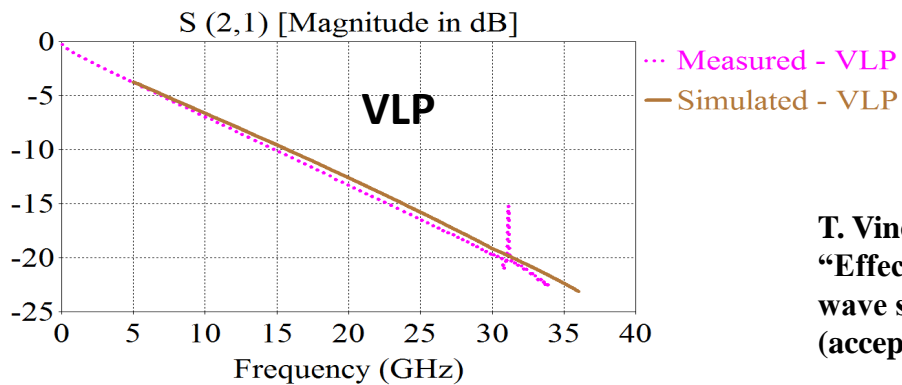
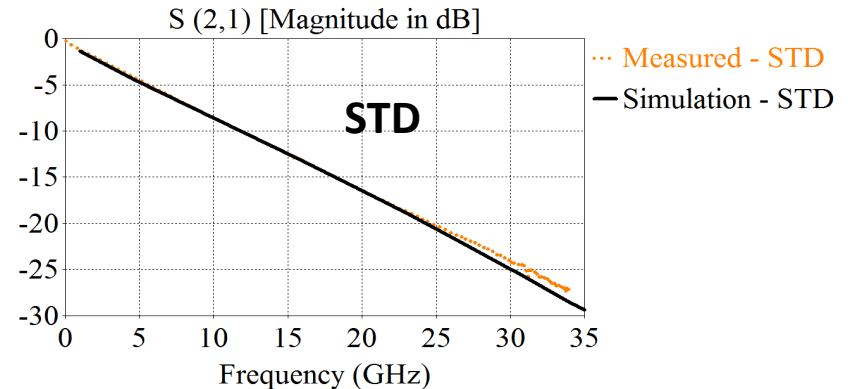
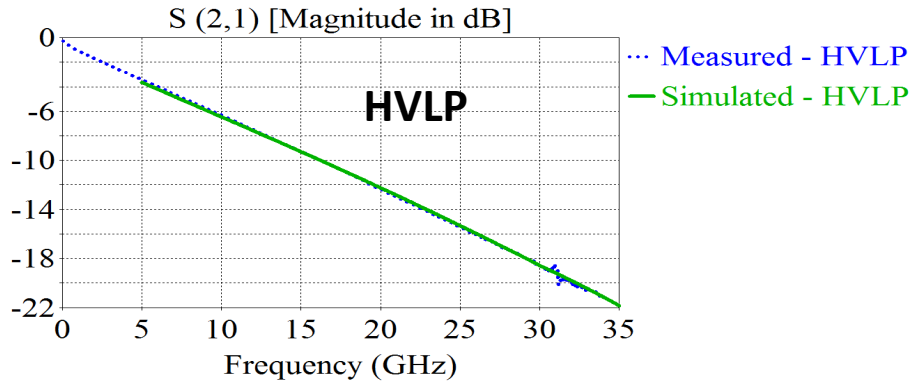
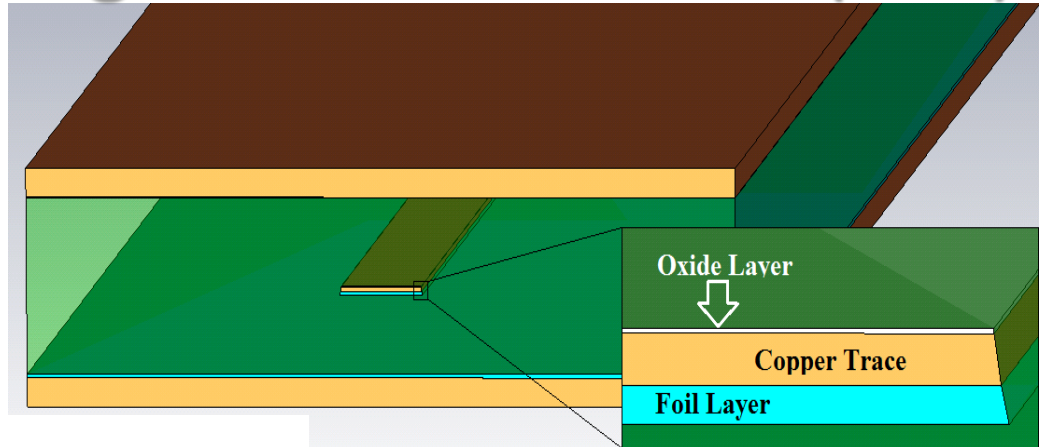
Sets 1,2,3 – **13mil**  
trace width

Sets 4, 5 – **7 mil**  
trace width

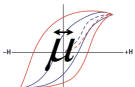
$$VR = \epsilon_r'' \times T_r = \epsilon_r' \times \tan \delta_r \times T_r$$

# Validation Using Full-wave Model (CST)

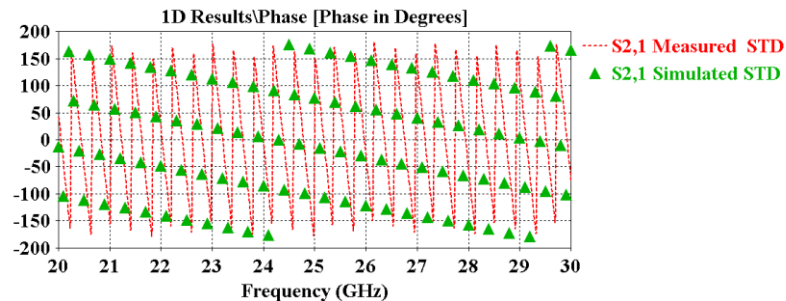
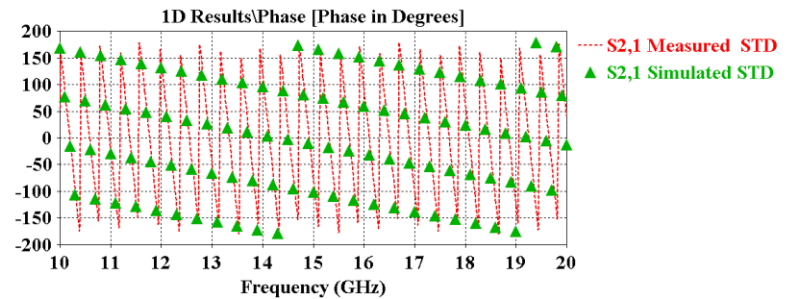
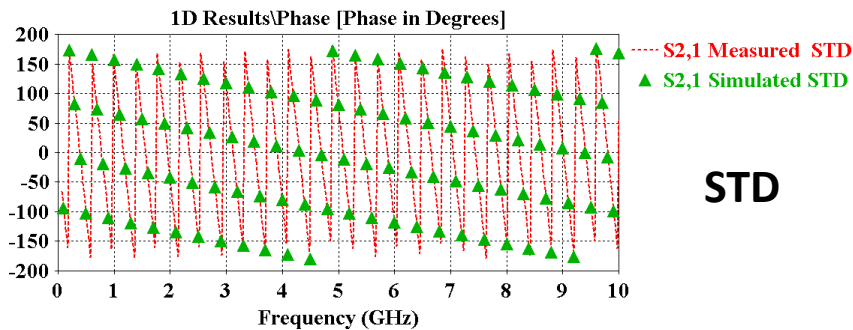
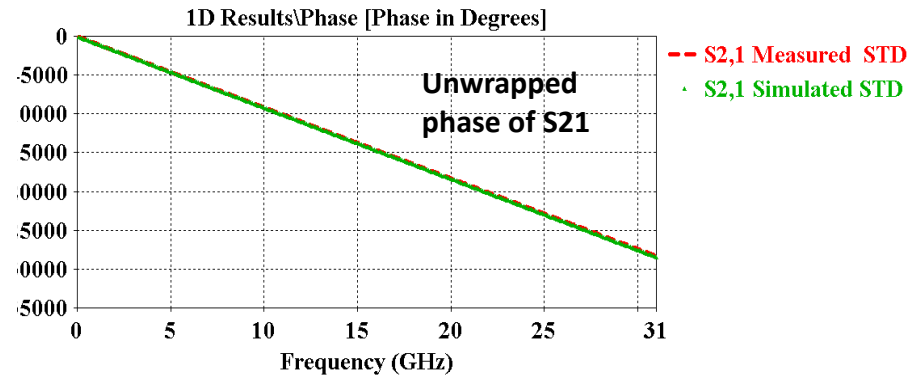
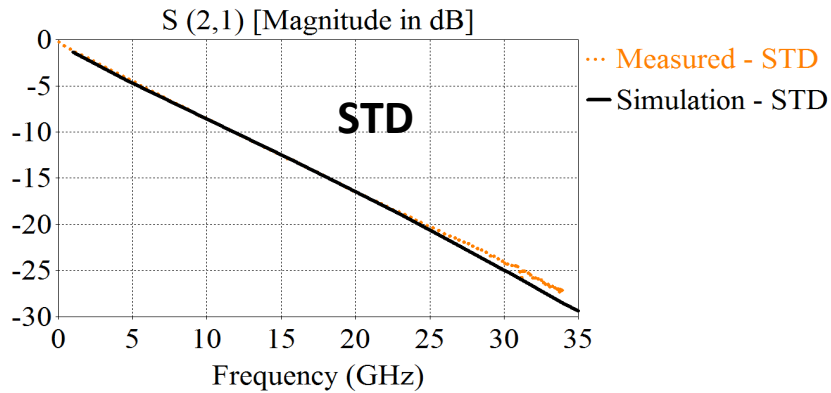
**Numerical model 2: CST Studio Suite 3D (Full-wave FD MoM) – this model is used for validation of the extracted ERD data**



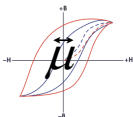
T. Vincent, M. Koledintseva, A. Ciccimancini, and S. Hinaga, "Effective roughness dielectric in a PCB: measurement and full-wave simulation verification", IEEE Symp. EMC, Aug. 2014 (accepted)



# S<sub>21</sub> CST Modeled vs. Measured



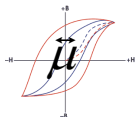
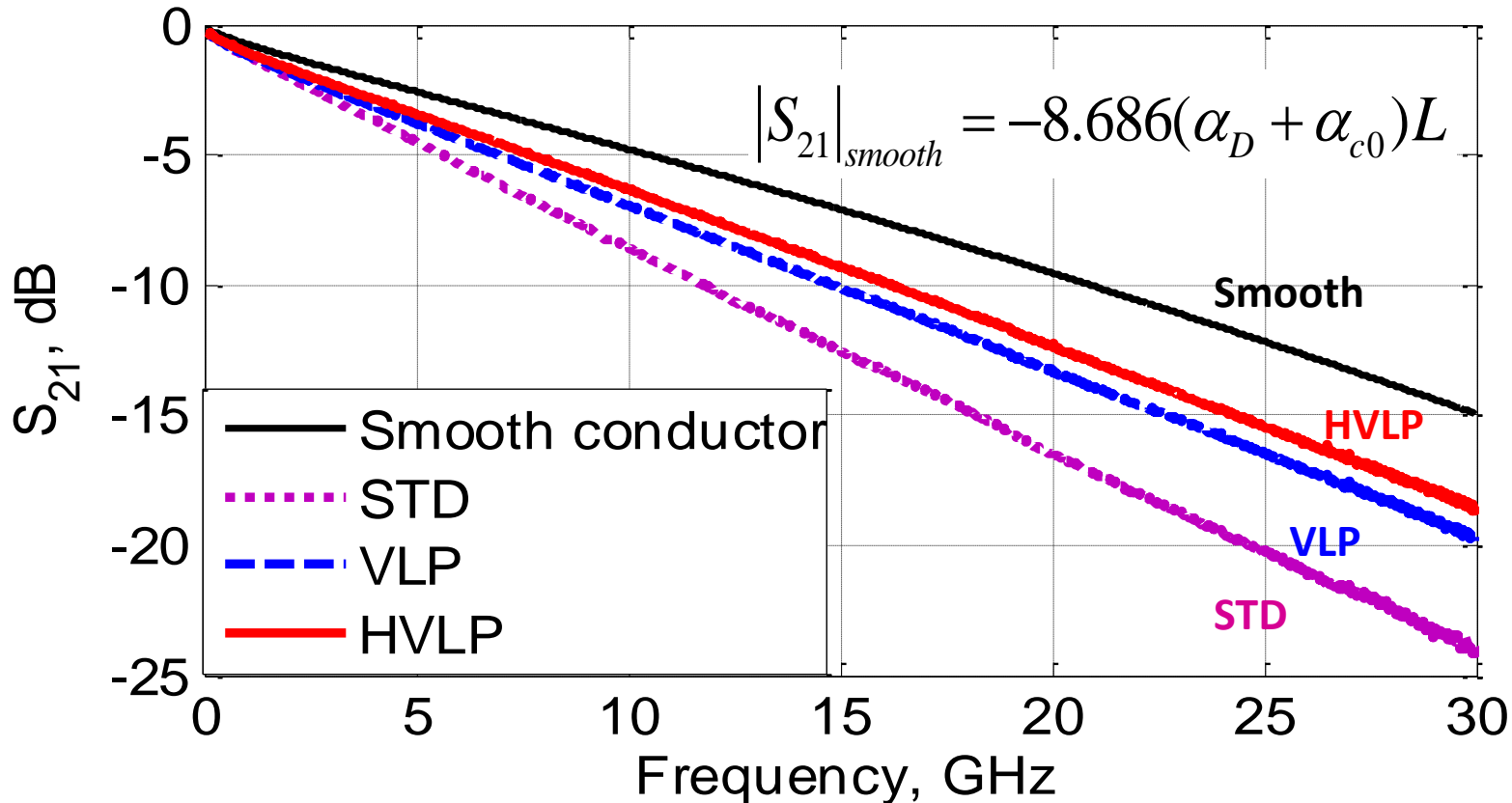
T. Vincent, M. Koledintseva, A. Ciccimancini, and S. Hinaga, “Effective roughness dielectric in a PCB: measurement and full-wave simulation verification”, IEEE Symp. EMC, Aug. 2014 (accepted)



# Modeled & Measured Magnitude of $S_{21}$ for Striplines with Different Foils

Slope of  $S_{21}$  as a function of frequency increases with the increase of surface roughness

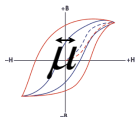
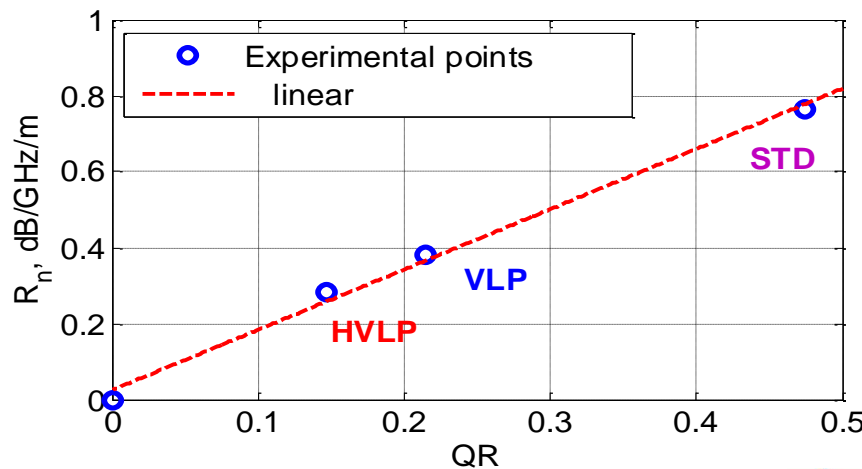
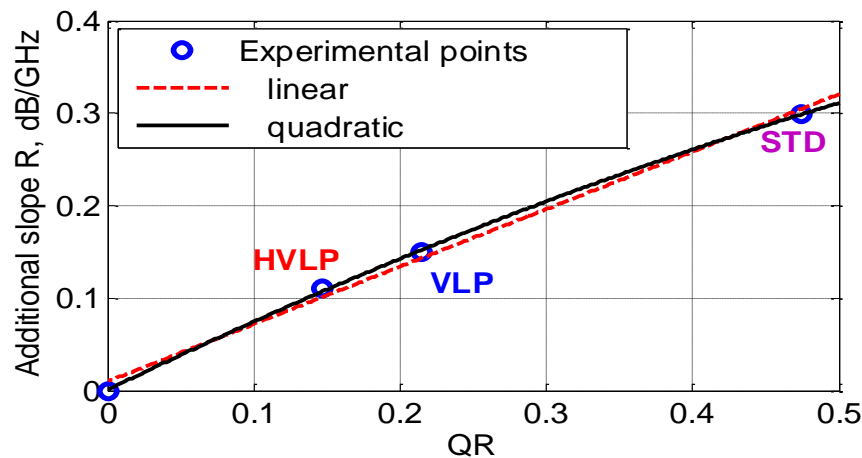
$$\alpha_c = \alpha_{c0}(1+r) \quad r = \frac{\Delta\alpha_r}{\alpha_{c0}} \quad \Delta\alpha_r = \alpha_c - \alpha_{c0}$$



# Additional Slope in $S_{21}$ as a Function of Roughness Factor

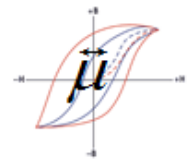
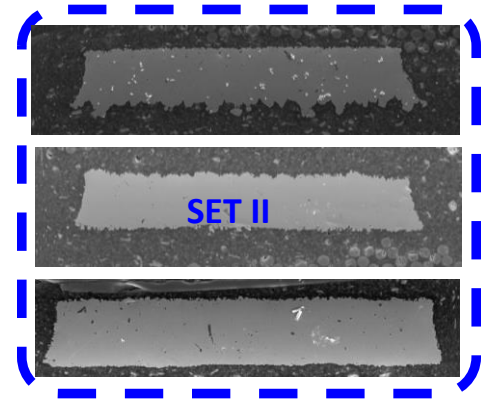
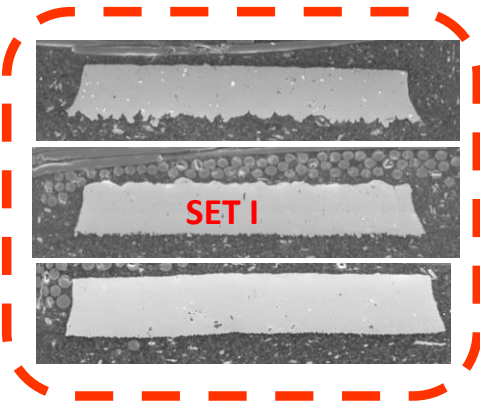
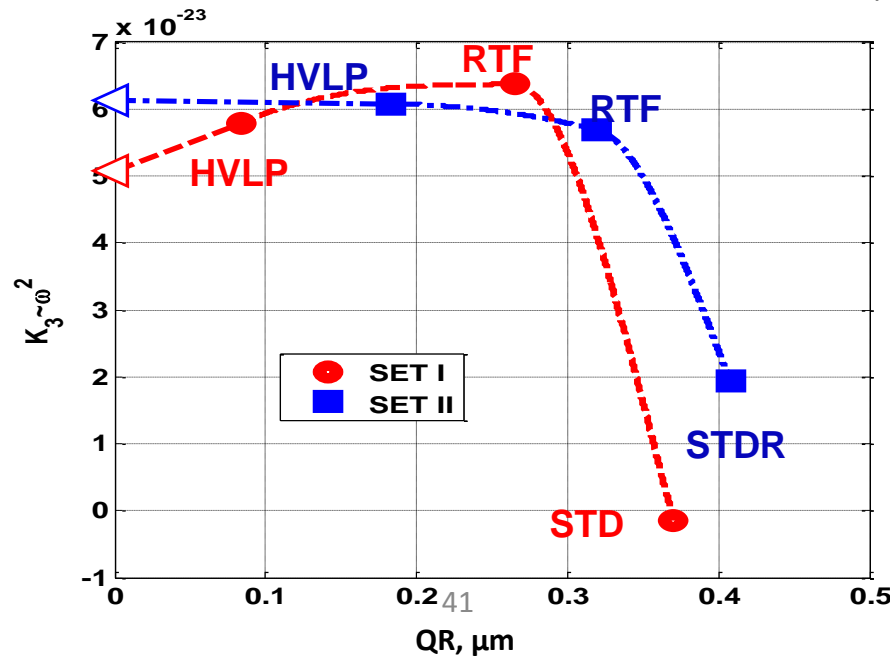
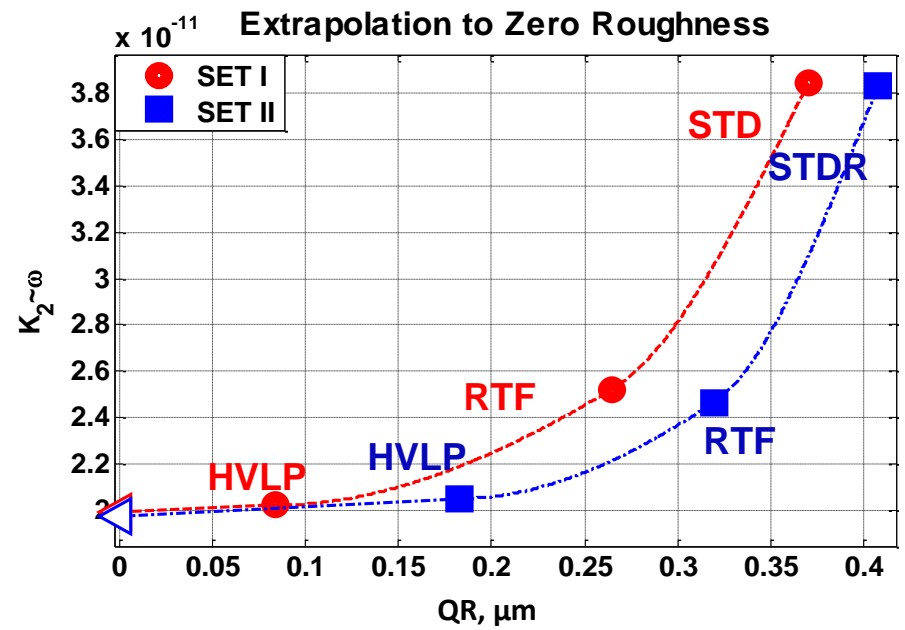
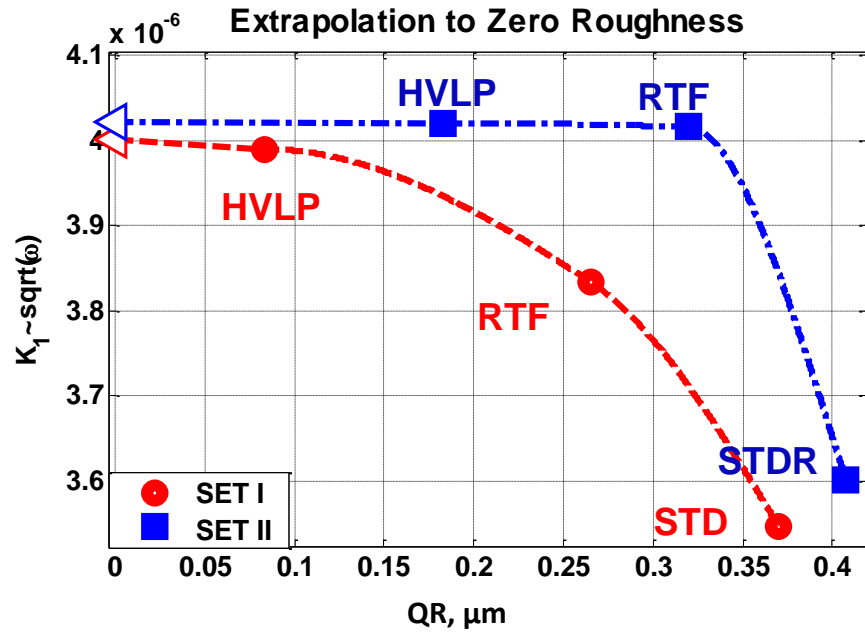
$$R = (\Delta S_{smooth} - \Delta S_{rough}) / \Delta f \quad [\text{dB/GHz}]$$

$$R_n = (\Delta S_{smooth} - \Delta S_{rough}) / \Delta f / L \quad [\text{dB/GHz/m}]$$

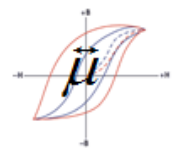
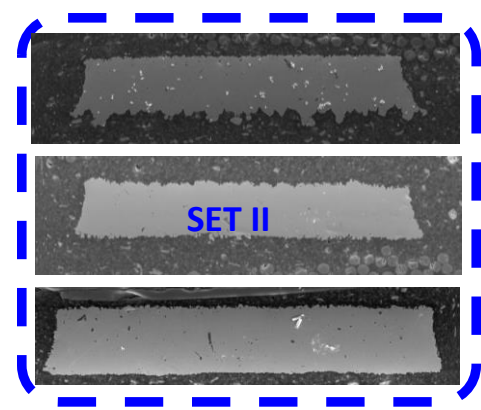
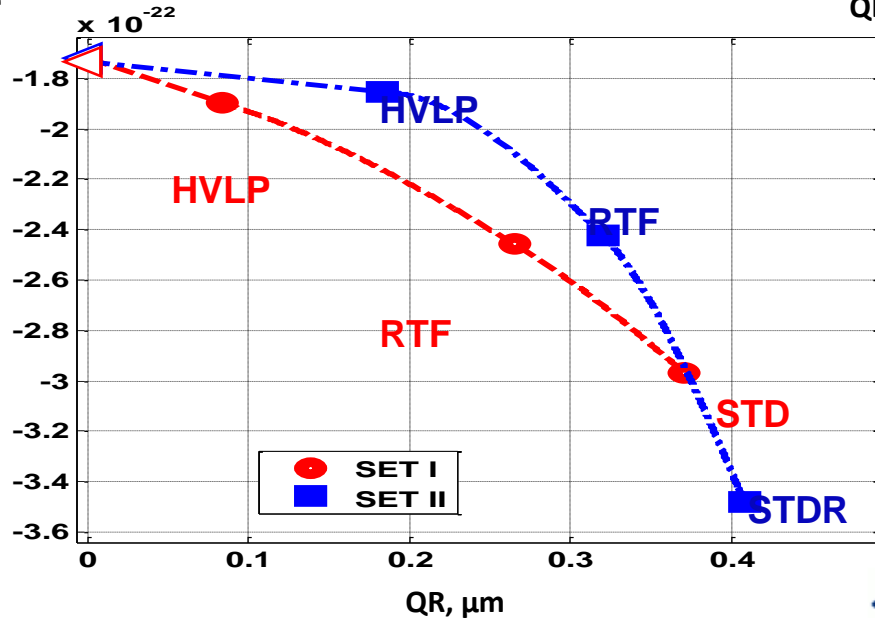
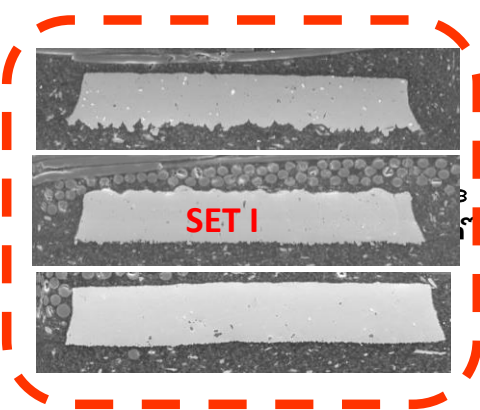
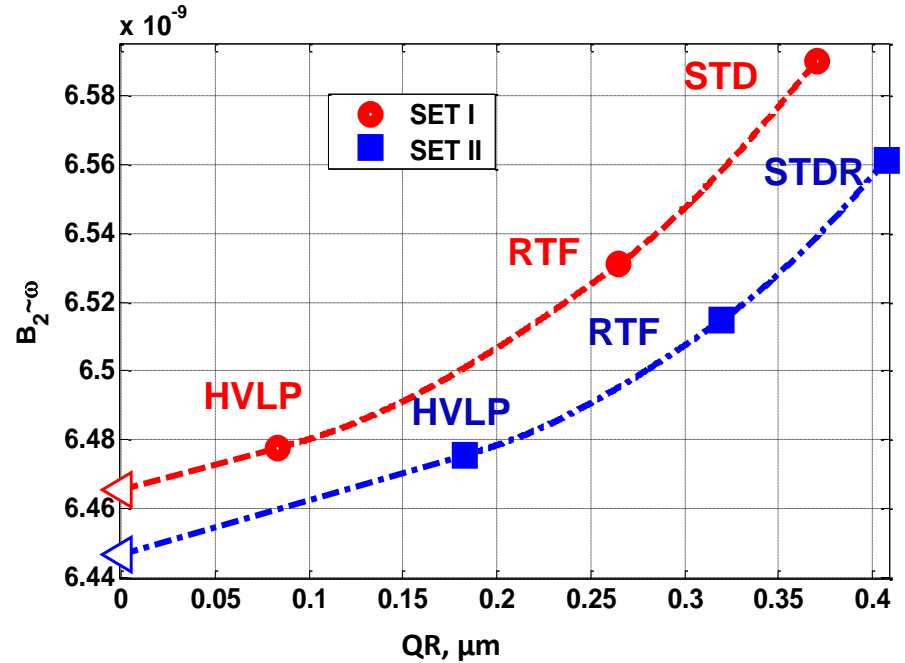
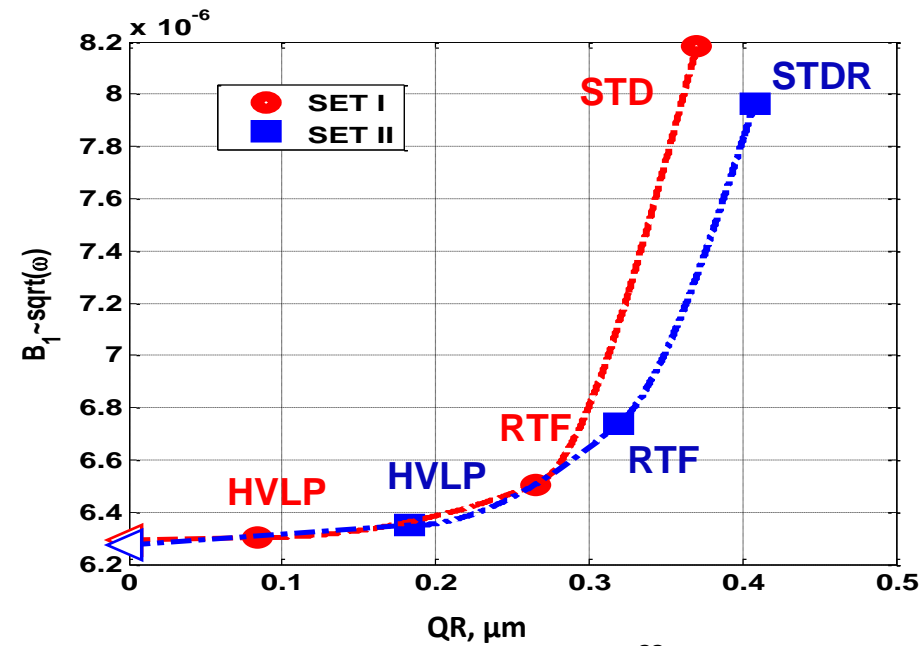




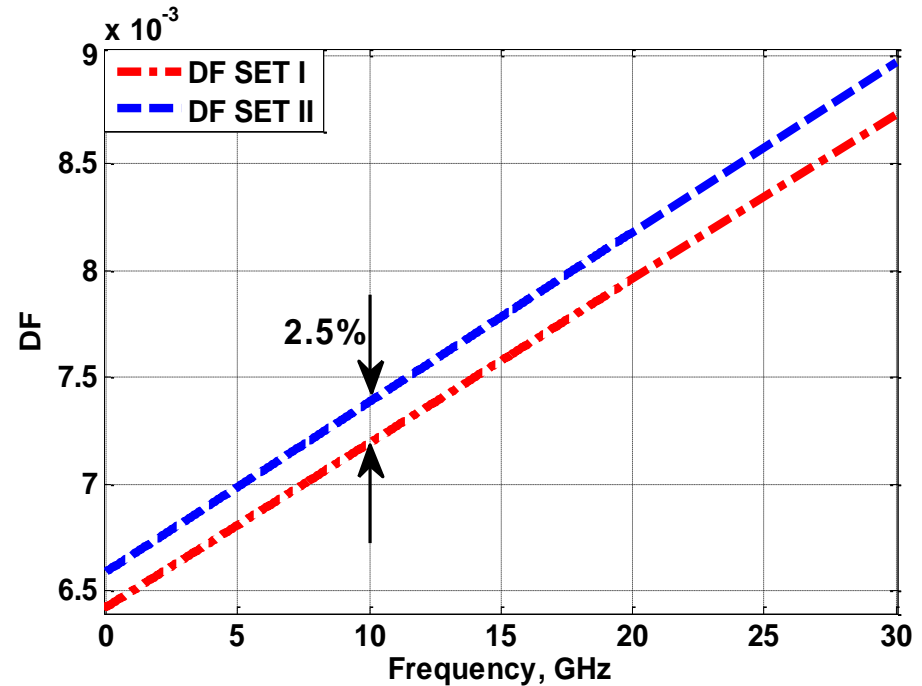
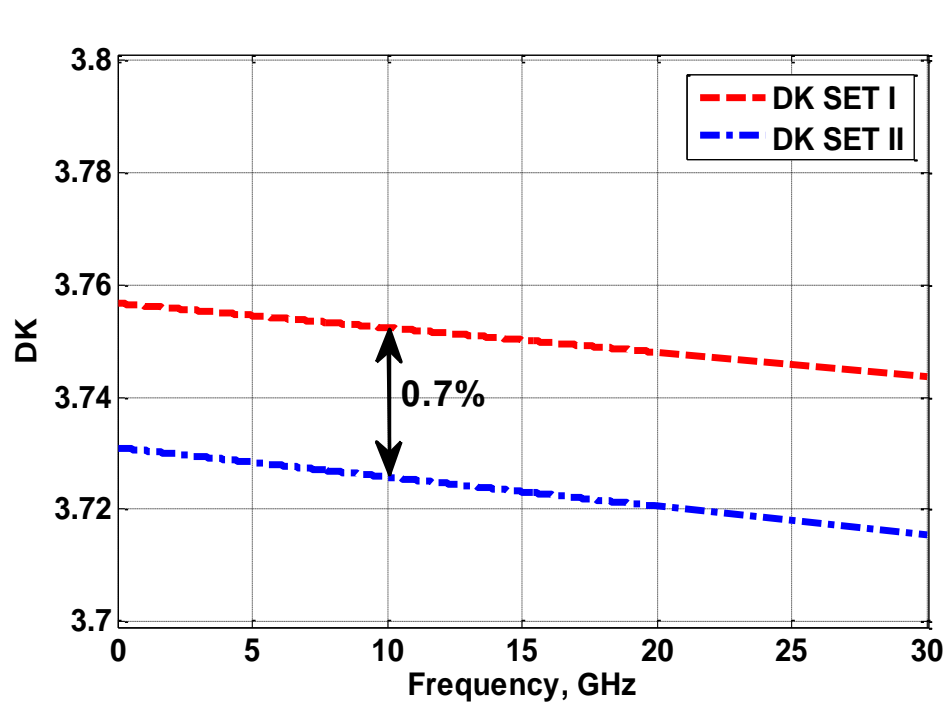
# Extrapolation to Zero Roughness in $\alpha$ (7-mil Lines)



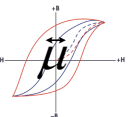
# Extrapolation to Zero Roughness in $\beta$



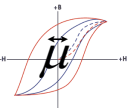
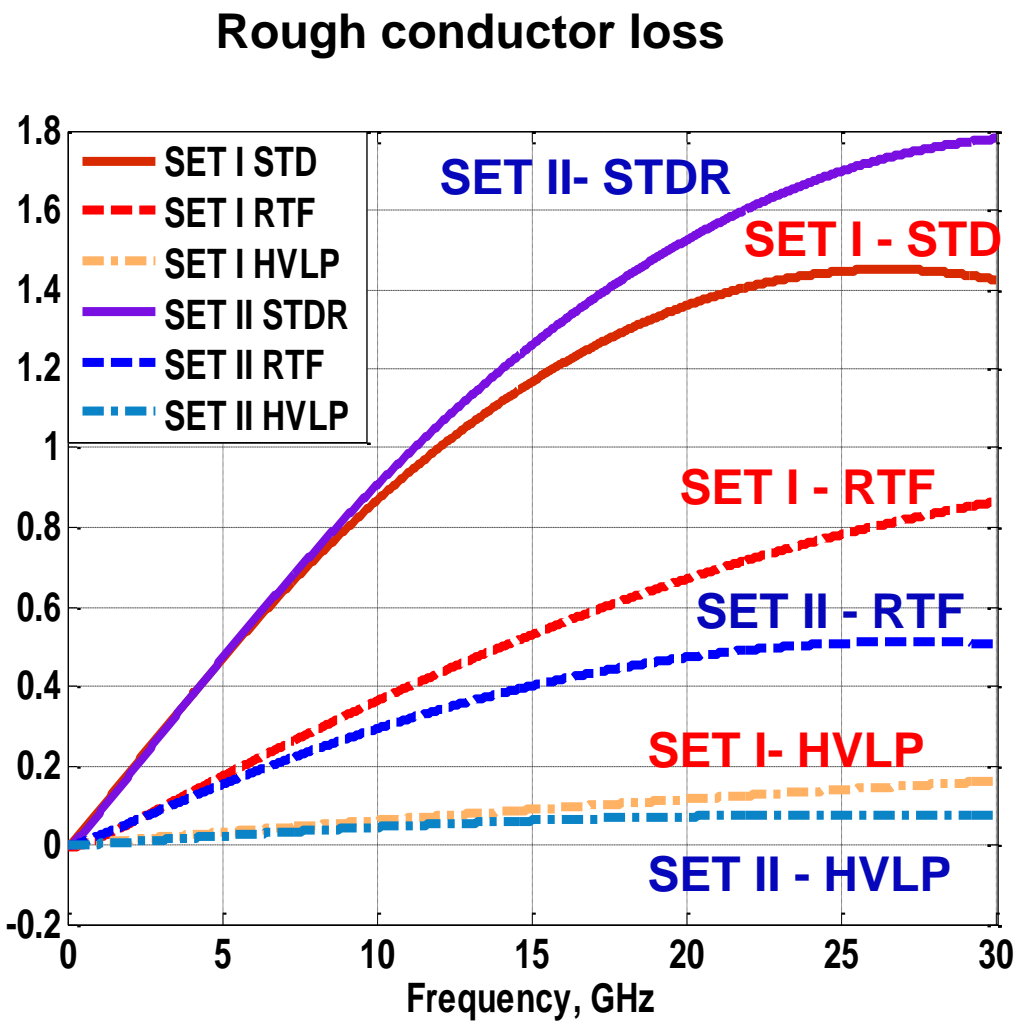
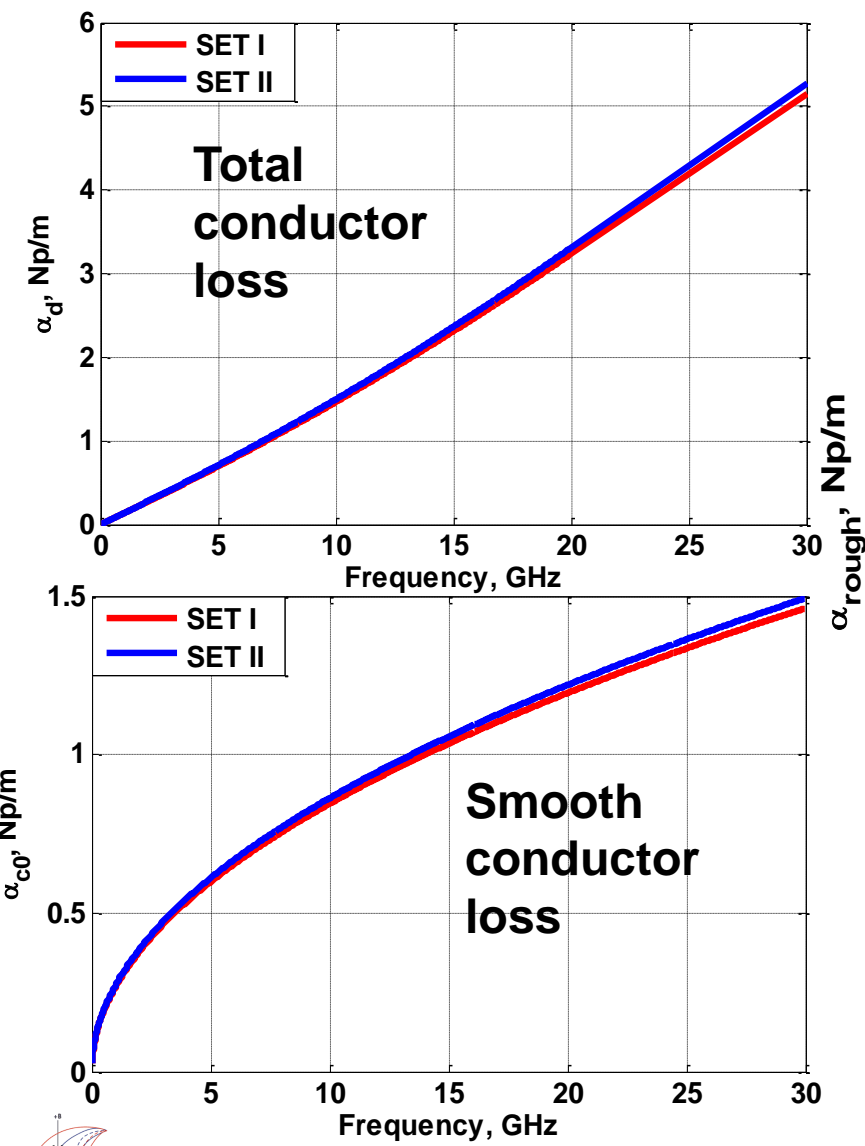
# Refined DK and DF



Excellent agreement between the results of extraction of dielectric parameters of two independent sets of boards (3+3 boards total) with the same dielectric and the same geometry, but different types of foil roughness has been obtained! Frequency range is from **10 MHz to 30 GHz**.

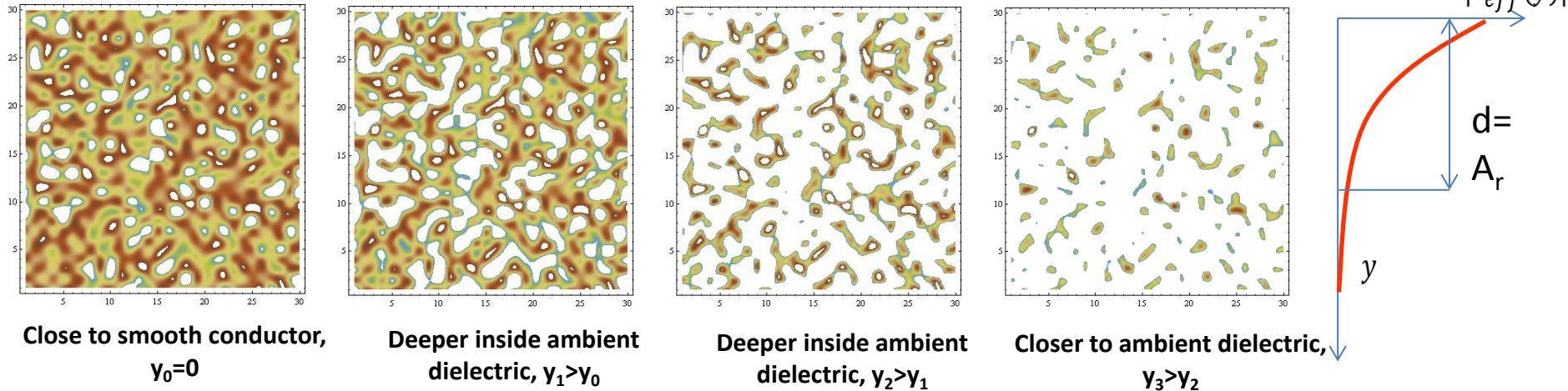


# Dielectric Loss and Smooth & Rough Conductor Losses



# Effective Roughness Dielectric Approximation

Concentration of “roughness inclusions” decreases with distance from zero-roughness plane



Maxwell Garnett mixing rule requires knowledge of volume concentration of “roughness inclusions”. This volume concentration  $\nu(y)$  varies as a function of the height  $y$ . *Hence the dielectric properties homogenized by Maxwell-Garnett in each incremental layer are also functions of  $y$ .*

$$\epsilon_{MG}(y) = \epsilon_{matrix} \left( 1 + \nu(y) \frac{\epsilon_{incl} - \epsilon_{matrix}}{\epsilon_{matrix} + (1 - \nu(y)) N_y (\epsilon_{incl} - \epsilon_{matrix})} \right)$$

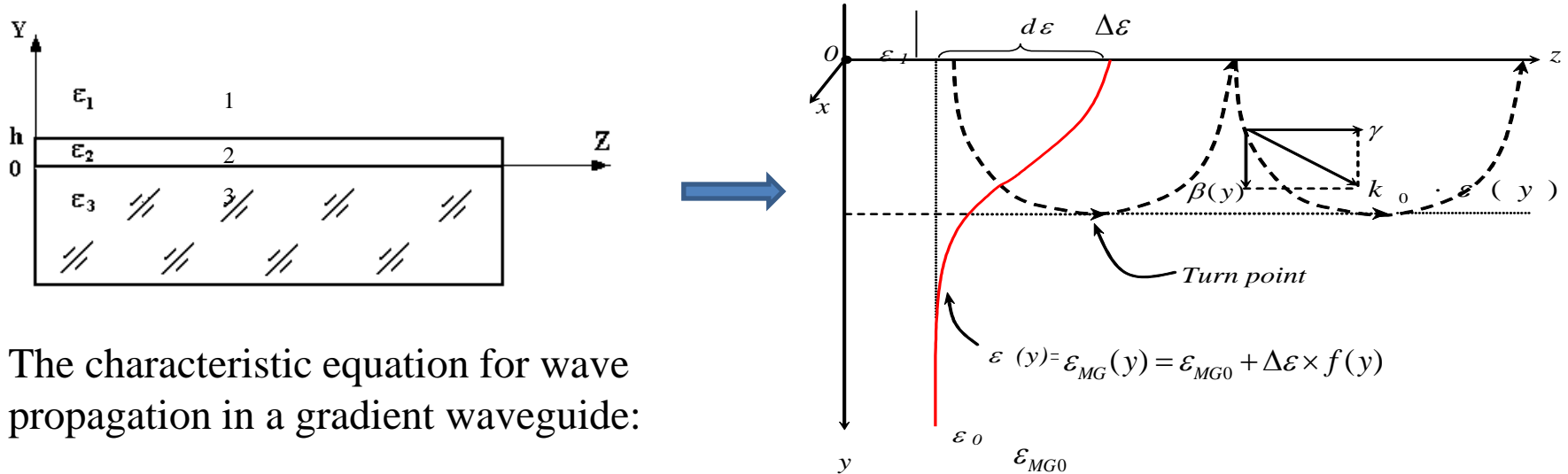
$N_y$  is the depolarization factor in  $y$ -direction.

$$\epsilon_{incl} = 1 - j \frac{\sigma}{\omega \epsilon_0} \quad \text{and} \quad \epsilon_{matrix} = 3.7 - j0.07$$

# Boundary Layer – Gradient Waveguide Model

Using Maxwell Garnett mixing rule the roughness could be described as gradient layer with exponential distribution  $\epsilon_{MG}(y) = \epsilon'_{MG}(y) - j\epsilon''_{MG}(y)$ .

Loss is due to non-propagating surface waves in the structure with variable permittivity.



The characteristic equation for wave propagation in a gradient waveguide:

$$k_0 \cdot \int_0^{y_l} \sqrt{\epsilon_{MG}(y) - \epsilon_{eff}^2} dy = \arctan \left( \frac{(\epsilon_{MG0} + \Delta\epsilon) \cdot \sqrt{\epsilon_{eff} - \epsilon_1}}{\epsilon_1 \cdot \sqrt{(\epsilon_{MG0} + \Delta\epsilon) - \epsilon_{eff}}} \right) + \pi \cdot (l-1) + \frac{\pi}{4}$$

**Resultant effective roughness dielectric**

$$\epsilon_{eff} = \epsilon'_{eff} - j\epsilon''_{eff}$$

Where  $\epsilon_1 = \epsilon_{incl} = 1 - j \frac{\sigma}{\omega \epsilon_0}$  and  $\Delta\epsilon$  is the difference of  $\epsilon_{MG} - \epsilon_{incl}$

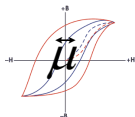
# Results for the Gradient Model: Set 1, Foil Side

Extracted from Gradient Model (on Foil Sides)						Extracted from Q2D		
		Solution #	Turning point= Ar	$\tan\delta_{\text{rough}}$	$\varepsilon'_{\text{rough eff}}$	Ar	$\tan\delta_{\text{rough}}$	$\varepsilon'_{\text{rough eff}}$
Set 1	STD	15	6.489	0.203	12.7	6.496	0.17	12.0
		13	5.05	0.124	5.02			
	VLP	6	2.739	0.130	8.08	2.752	0.13	9.0
		5	1.932	0.100	13.58			
	HVLP	2	1.083	0.048	5.01	1.086	0.04	4.8
		1	0.158	0.203	44.76			

There is a reasonable agreement; however, the results were obtained only for a limited number of samples.

# Conclusions

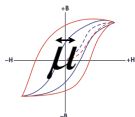
- A new improved technique DERM2 to extract dielectric properties of a laminate dielectric for a set of five test vehicles is demonstrated.
- A semi-automatic roughness profile extraction and quantification procedure has been applied to SEM or optical microscopy pictures of microsections of PCB stripline.
- A metric called “roughness factor” QR to quantify roughness profiles has been introduced.
- The correlation between the additional slope in insertion loss due to roughness and the roughness factor QR has been established. The effective roughness dielectric layer concept was applied to numerically model (in 2D FEM) all the five test vehicles.
- In the numerical models, the dielectric parameters of ambient dielectric were taken as those obtained using the DERM2 procedure; the boundary roughness layers were substituted by Effective Roughness Dielectric.
- This model and analysis lead to the development of the “design curves” (additional slopes of insertion loss, or additional conductor loss as a function of roughness parameter), which could be used by SI engineers in their designs.





# Acknowledgment

- I am very grateful to **Scott Hinaga** (Cisco) for collaboration, weekly discussions at conference calls, support of ideas, and sponsoring this research in 2008-2014.
- I would like to thank graduate and undergraduate students of Missouri S&T who contributed to this work: **Amendra Koul** (Cisco), **Praveen Annula** (Mentor Graphics), **Soumya De** (Cisco), **Fan Zhou** (Semtech), **Aleksandr Gafarov** (Mentor Graphics), **Aleksei Rakov** (Moscow Power Engineering Institute), **Oleg Kashurkin** (Missouri S&T), and **Alexei Koledintsev** (Missouri S&T).
- I would like to thank Prof. **James Drewniak** for an opportunity to work with EMC Lab of Missouri S&T in 2000-2014, motivation for this research, and useful discussions.
- I would like to thank Missouri S&T Materials Research Center colleagues – Dr. **Clarissa Wisner**, **Dr. Beth Culp**, Prof. **Matt O’Keefe**, and **Dr. Signo Reis** (Saint Gobain) for their help with SEM and optical micro photographs.
- This work was also partially supported by the **National Science Foundation** under **Grant No. 0855878** through *NSF IUCRC* Program.



# Thanks

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