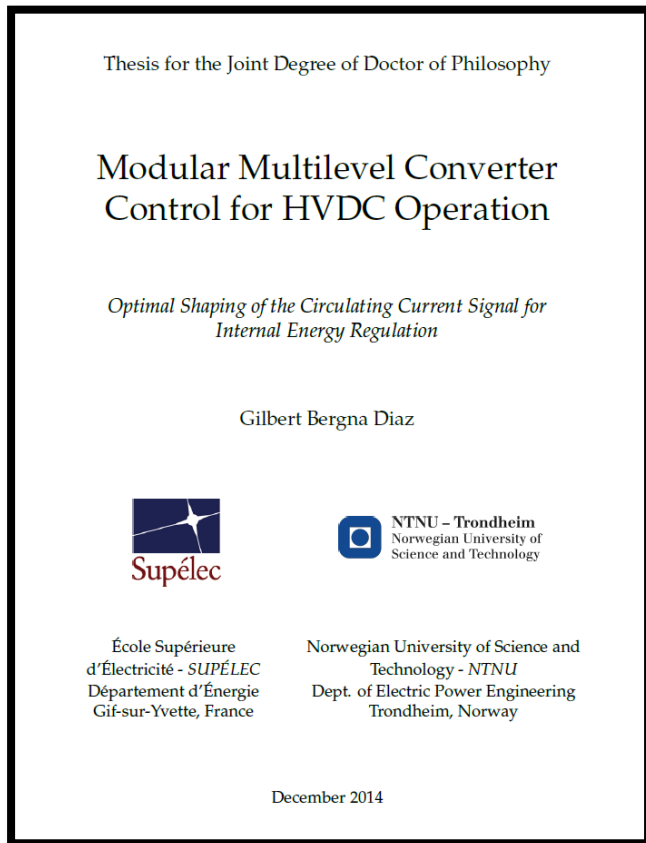


Modular Multilevel Converter Control for HVDC Operation

Optimal Shaping of the Circulating Current Signal for
Internal Energy Regulation

My PhD Thesis in 30 seconds



My PhD supervisors:



- Amir Arzandé
- Jean-Claude Vannier



NTNU • Marta Molinas



- Erik Berne
- Philippe Egrot

Thesis Outcomes:

- **Two** MMC control strategies:
 - Linear (Resonant controllers)
 - Non-linear (Passivity Theory)
- **One** lab-scale MMC

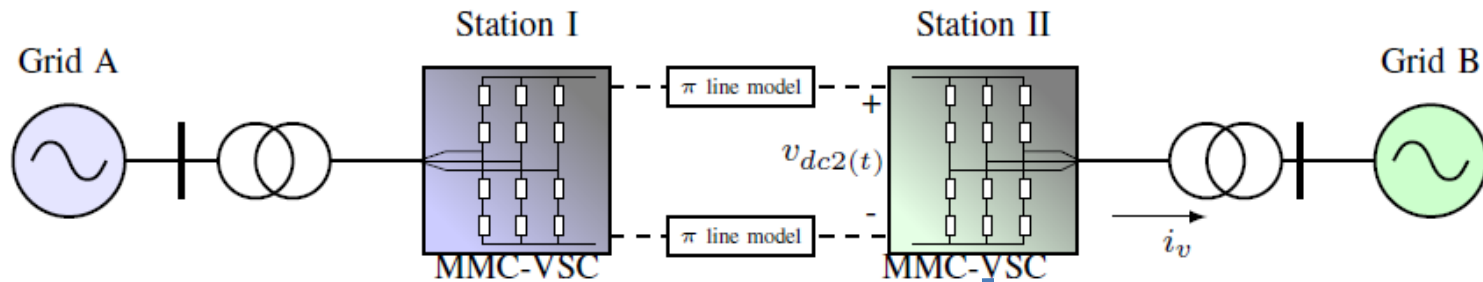
Overview

- Introduction
- Optimization of the circulating current.
- Circulating current signal for constant power under unbalanced grid conditions.
- Conclusions

Part I

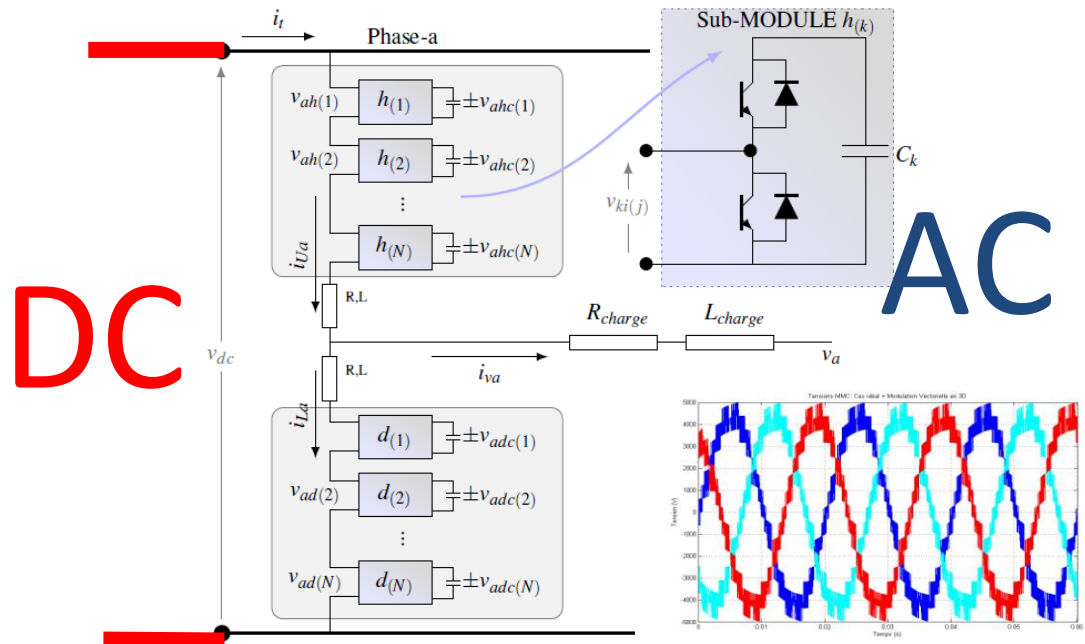
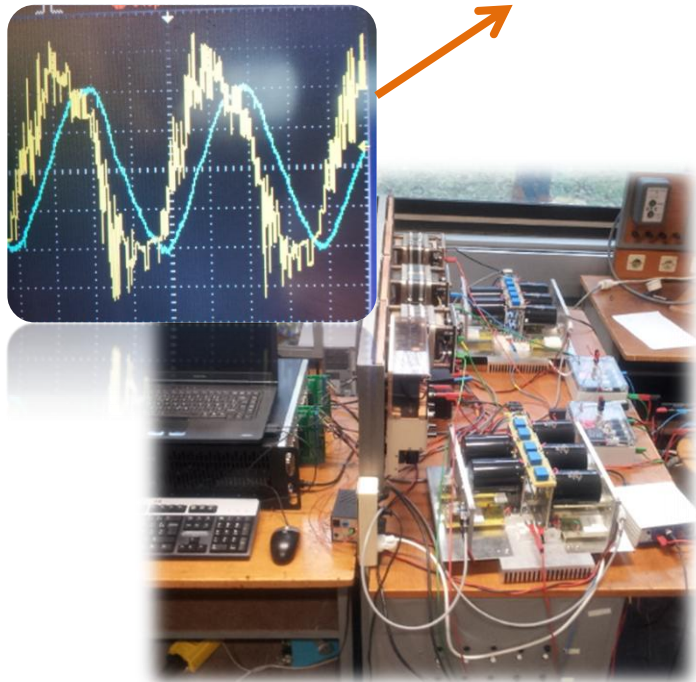
INTRODUCTION

The Modular Multilevel Converter

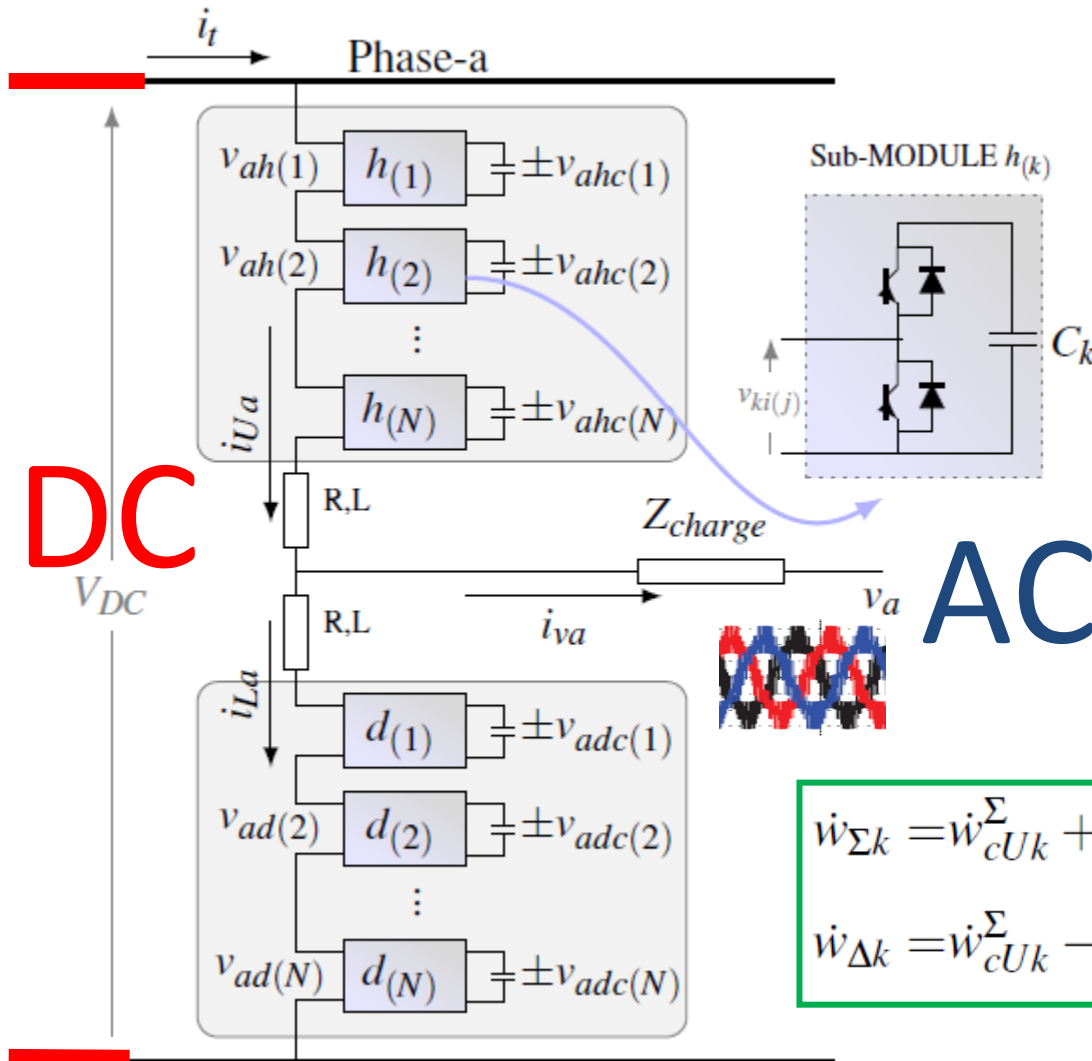


Lab Prototype:

MMC Voltage and Load Currents



MMC Basics



Two Current variables:

- 1) Circulating current (i_{circ})
- 2) Grid current (i_v)

$$i_{ck} = \frac{i_{Uk} + i_{Lk}}{2}$$

$$i_{vk} = i_{Uk} - i_{Lk}$$

Two Energy variables:

- 1) Energy Sum ($w_{\Sigma k}$)
- 2) Energy Difference ($w_{\Delta k}$)

$$\dot{w}_{\Sigma k} = \dot{w}_{cUk}^{\Sigma} + \dot{w}_{cLk}^{\Sigma} = -e_{vk} i_{vk} + (v_{dc} - 2u_{ck}) i_{ck}$$

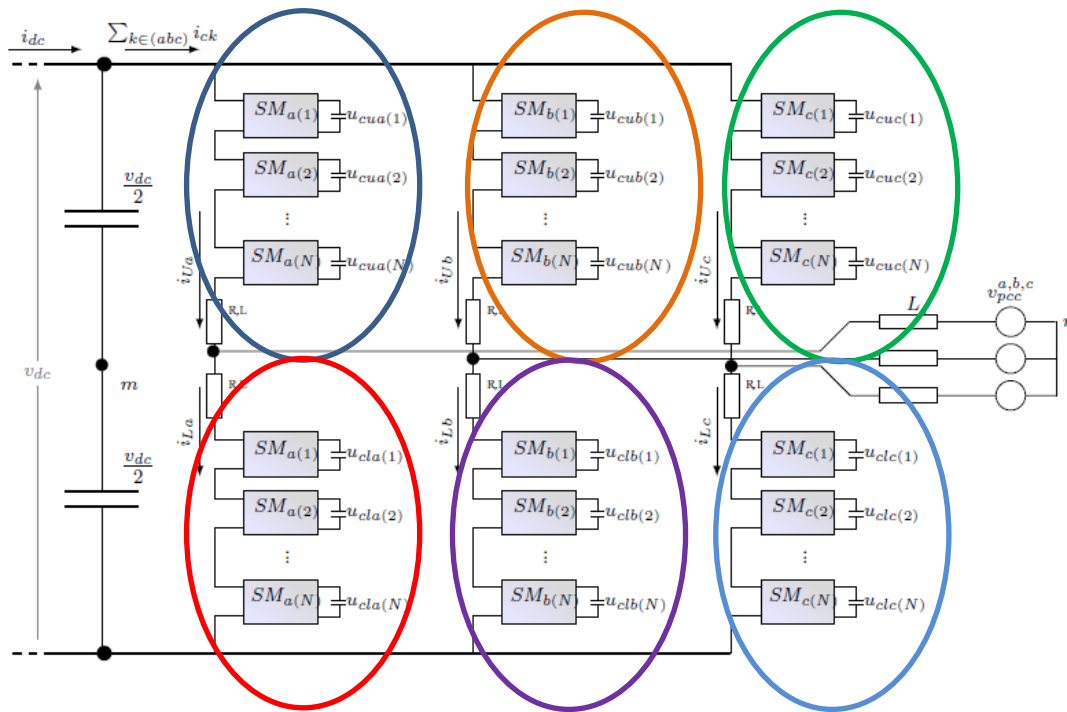
$$\dot{w}_{\Delta k} = \dot{w}_{cUk}^{\Sigma} - \dot{w}_{cLk}^{\Sigma} = \frac{i_{vk}}{2} (v_{dc} - 2u_{ck}) - 2e_{vk} i_{ck}$$

Motivation for a new "high-level" control strategy

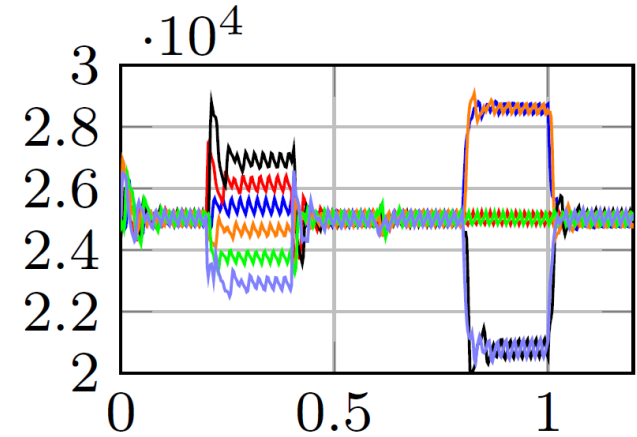


	Good Dynamic Performance	Robust / Parameter independent	Circulating Current Control	Capacitive Energy Control	SM Voltage Measurement Independence	Phase Independent Control
OLC	X	X	✓	✓	✓	✓
CLC	X	✓	X	✓	X	✓
CCSC	✓	✓	✓	X	✓	X
DDSRF	✓	✓	✓	✓	X	X
My PhD Controller	✓	✓	✓	✓	-	✓

Motivation: Need for a Robust and dynamically performant control scheme for phase / arm independent circulating current control and energy regulation.



Something like this...



p: Instantaneous
Active Power

q: Instantaneous
Imaginary Power
or reactive power

Akagi's instantaneous p-q theory

- In $\alpha\beta$ coordinates: $p(t) = (v_\alpha + jv_\beta) \cdot (i_\alpha + ji_\beta) = (v_\alpha i_\alpha + v_\beta i_\beta) + j(v_\alpha i_\beta - v_\beta i_\alpha)$
- In dqo coordinates: $p(t) = (v_d + jv_q) \cdot (i_d + ji_q) = (v_d i_d + v_q i_q) + j(v_d i_q - v_q i_d)$

Implementation of circulating current control strategies in dqo or $\alpha\beta$ can be challenging.

- Does not allow direct and explicit control of individual variables of each phase/arm.
- High number of reference frame transformations, filters and decoupling loops for detecting the various frequency components of circulating currents, sum arm energy and arm energy difference variables.

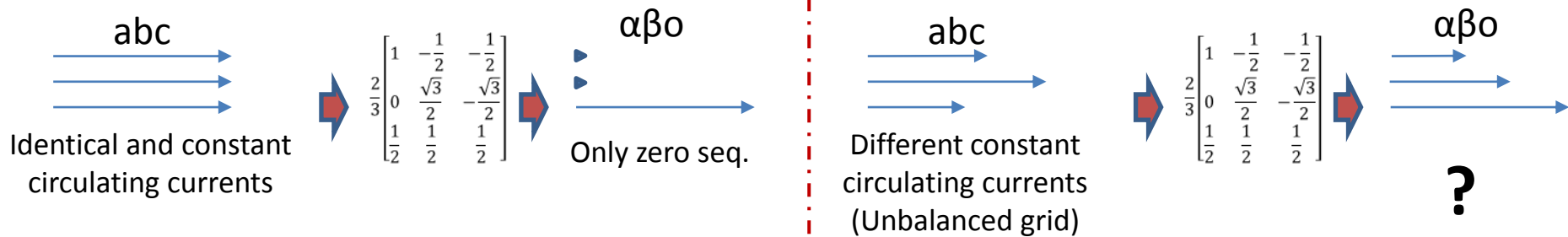
MMC: Several frequency components in steady state.

- Circulating current: DC , $+\omega$, -2ω ,.
- Grid current: $+\omega$.
- Capacitive Energy Sum: DC , -2ω .
- Capacitive Energy Difference: DC , $+\omega$.

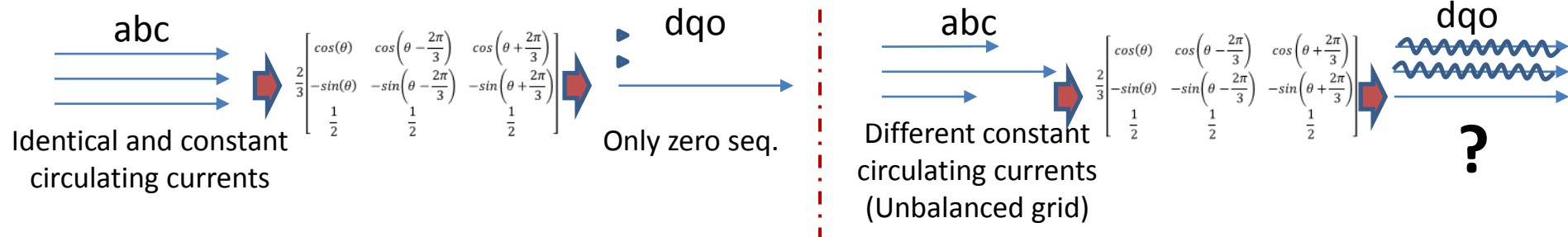
Conventional Synchronous Reference Frame Control (SRFC)

-> Requires advanced decoupling techniques.

Clarke's Transform (applied to three DC variables)



Park's Transform (applied to three DC variables)



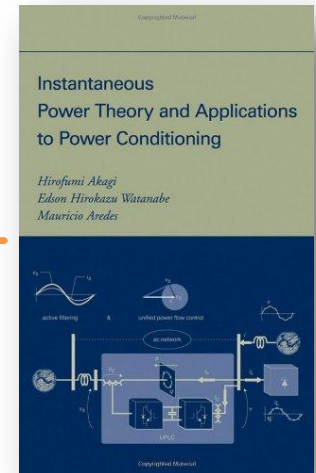
-> Controller will be designed in the MMC natural "abc" coordinates.

Part II: Arm-independent Energy Shaping and Regulation

OPTIMIZATION OF THE CIRCULATING CURRENT SIGNAL

Introduction to the instantaneous "abc" power theory

- Using the nomenclature proposed by H. Akagi, the instantaneous power theories can be classified into **two groups**:
 - The ***p-q theory***: defined using the $\alpha\beta$ coordinates.
 - The ***abc theory*** (or *vectorial theory*): defined directly using the natural *abc* coordinates from the start.
- His book was devoted to the *p-q* theory...
- ...however, there is a small section where he used the *abc theory* in combination with an optimization method to determine the active currents in phase coordinates.



Active current calculation by means of a minimization method (1/2)

Calculate the minimum currents of a three phase system:

$$\min \rightarrow f(i_k) = (i_k)^2, k \in (abc)$$

...subject to the constraint of transferring the desired instantaneous power:

$$p_{3\varphi} = \sum_{k \in (abc)} v_k i_k$$

The above is an optimization problem, that can be solved using the Lagrange methodology.

$$\mathcal{L}(i_k, \lambda) = (i_k)^2 + \lambda \left(\sum_{k \in (abc)} v_k i_k - p_{3\varphi} \right)$$

Active current calculation by means of a minimization method (2/2)

$$\nabla_{i_k, \lambda} \mathcal{L}(i_k, \lambda) = 0 \quad \left\{ \begin{array}{l} \frac{\partial \mathcal{L}(i_k, \lambda)}{\partial i_k} = 2i_k + \lambda v_k = 0 \\ \frac{\partial \mathcal{L}(i_k, \lambda)}{\partial \lambda} = \sum_{k \in (abc)} (v_k i_k) - p_{3\varphi} = 0 \end{array} \right.$$

$$i_k = \frac{p_{3\varphi}}{\sum_{k \in (abc)} v_k^2} v_k$$

- The resulting current can be referred to as the *instantaneous active current*.
- This is the minimum current required to transfer the desired active power.

Generalized compensation theory for active filters

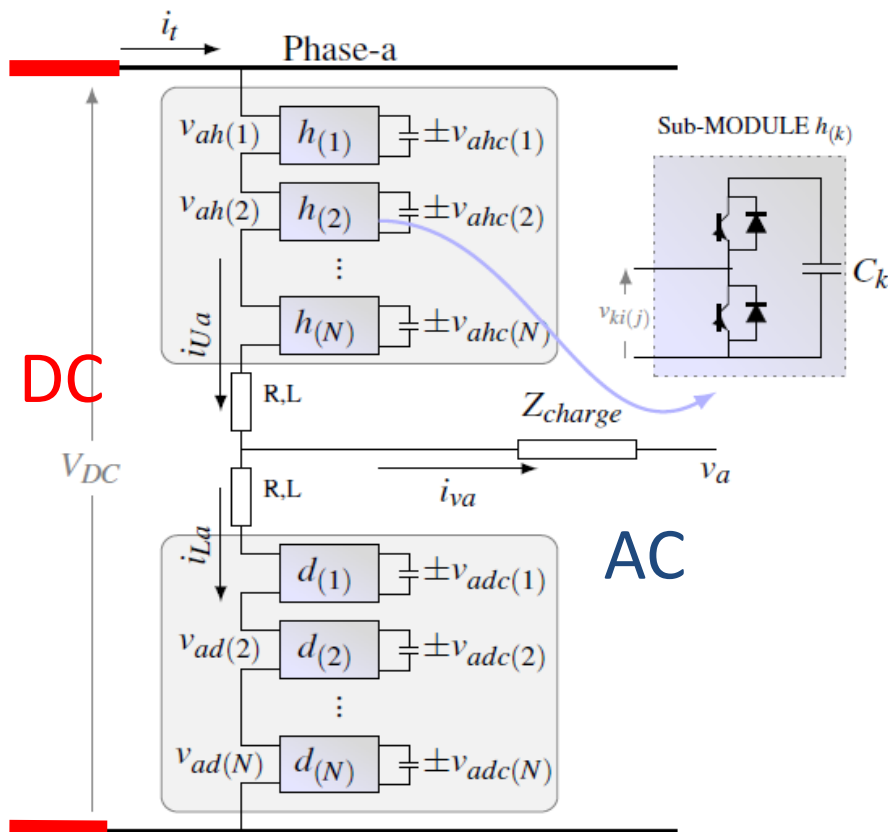
In 2012, A. Garcés *et al* **extended the previous results** by taking advantage of the inherent versatility of the optimization technique, applied to the case of a two level VSC active filtering.

For instance, cancelation of the zero-sequence current in four wire –three phase systems:

$$\mathcal{L}(i_k, \lambda_P, \lambda_0) = (i_k)^2 + \underbrace{\lambda_P \left(\sum_{k \in (abc)} v_k i_k - p_{3\varphi} \right)}_{\text{Same formulation problem as before}} + \underbrace{\lambda_0 \left(\sum_{k \in (abc)} i_k \right)}_{\text{Additional Constraint}}$$

$$i_k = \frac{p_{3\varphi}}{\sum_{k \in (abc)} v_k^2 - 3(v_o)^2} \cdot (v_k - v_o)$$

Applying the power theory to the MMC Circulating Current



Circulating current (i_{ck})

$$i_{ck} = \frac{i_{Uk} + i_{Lk}}{2}$$

IDEA:

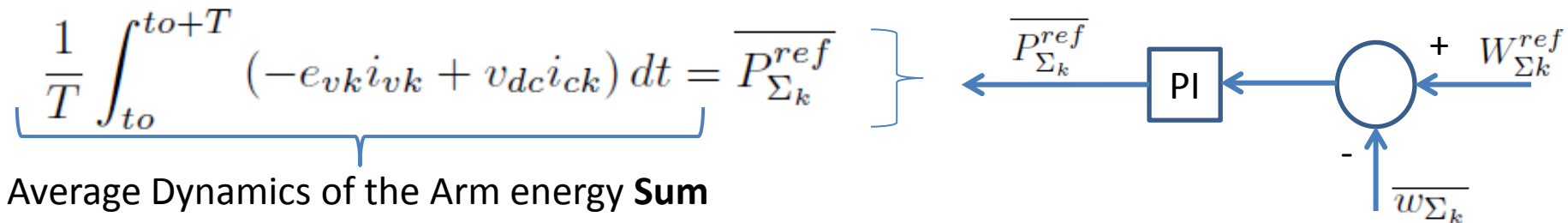
- Apply the Lagrange methodology to the MMC circulating current.
- Minimize energy and current fluctuations.
- Use constraints to regulate the average energy.

MMC circulating current calculation for phase independent control

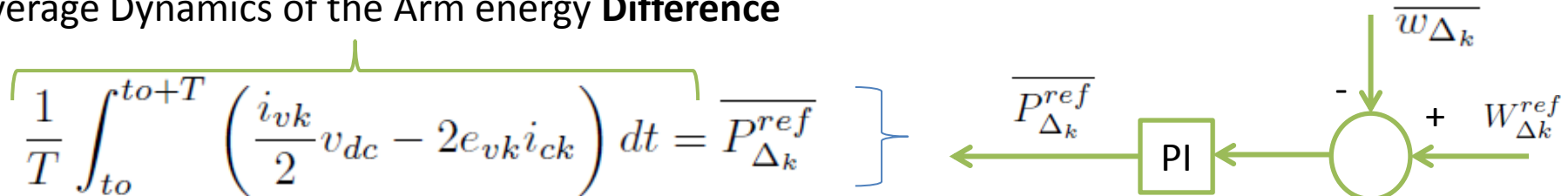
Objective function: Minimize the capacitive energy fluctuations & circulating current oscillations

$$\min \rightarrow \frac{1}{T} \int_{t_0}^{t_0+T} \left[\alpha (\dot{w}_{\Sigma k})^2 + (1 - \alpha) (v_{dc} i_{ck})^2 \right] dt$$

Constraints: The capacitive energy distribution (sum and difference) is being imposed.



Average Dynamics of the Arm energy **Difference**



MMC circulating current calculation for phase independent control (1/2)

Weighting factor

Objective function: Minimize the capacitive energy fluctuations & differential current oscillations

Lagrange

Equation:

$$\mathcal{L}(i_{ck}, \lambda_{\Sigma}, \lambda_{\Delta}) = \frac{1}{T} \int_{t_0}^{t_0+T} \left[\alpha (\dot{w}_{\Sigma k})^2 + (1 - \alpha) (v_{dc} i_{diffk})^2 \right] dt$$

$$+ \lambda_{\Sigma} \left(\overline{\dot{w}_{\Sigma k}}(t) - \overline{P_{\Sigma k}^{ref}} \right) + \lambda_{\Delta} \left(\overline{\dot{w}_{\Delta k}}(t) - \overline{P_{\Delta k}^{ref}} \right)$$

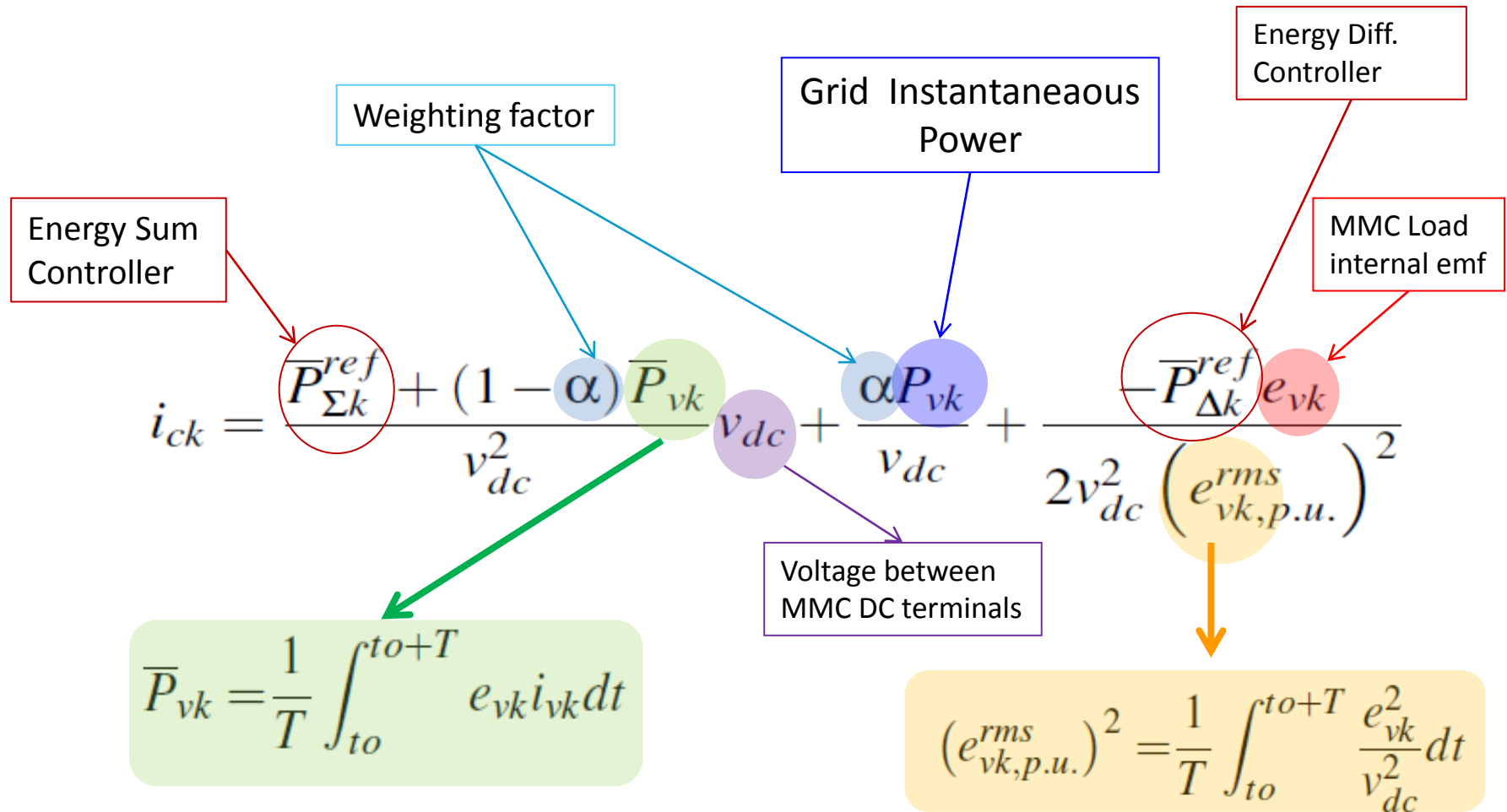
Lagrange's
Multipliers

Constraints: The capacitive energy distribution (sum and difference) is being imposed.

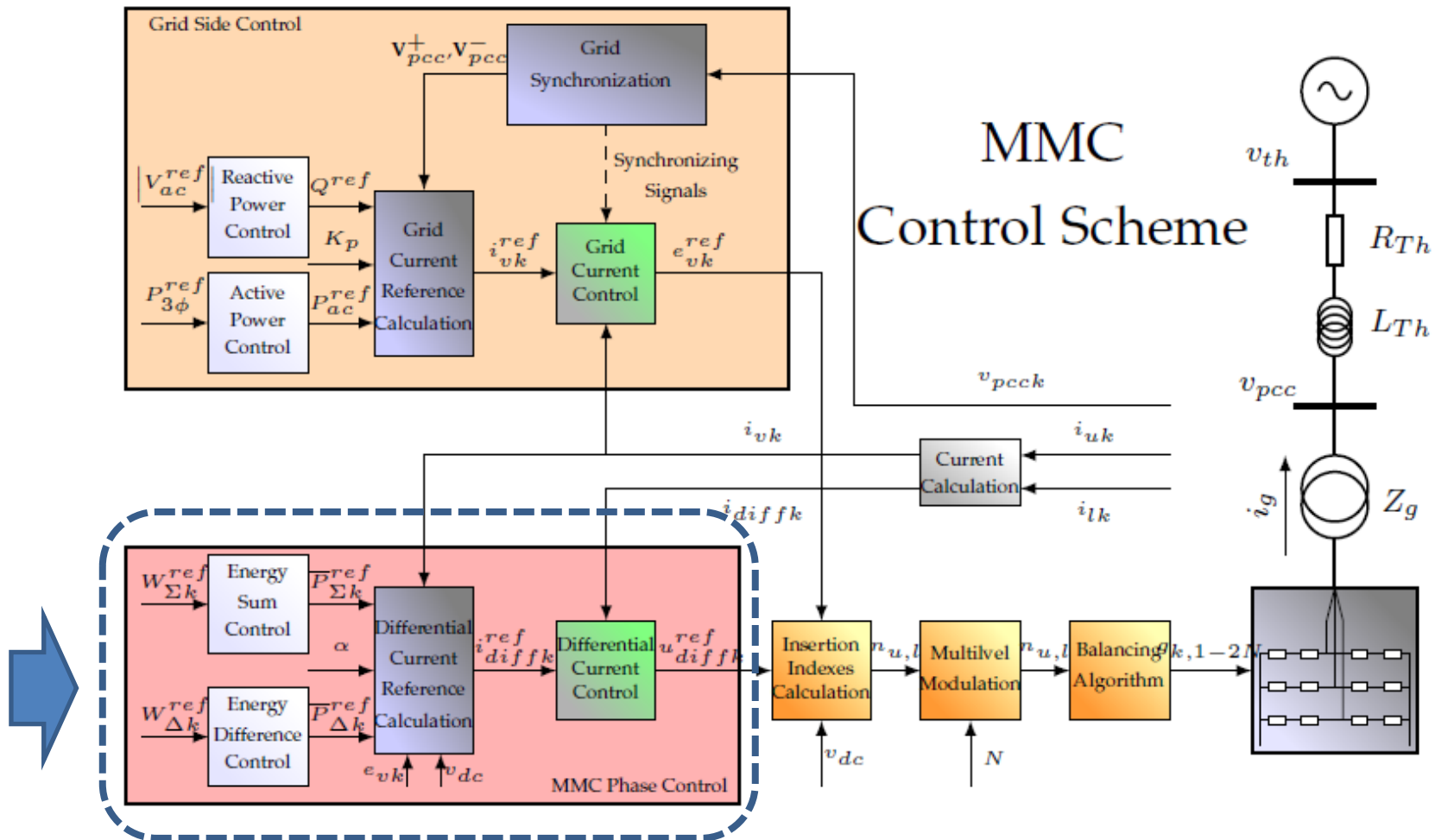
By solving:

$$\nabla_{(i_{ck}, \lambda_{\Sigma}, \lambda_{\Delta})} \mathcal{L}(i_{ck}, \lambda_{\Sigma}, \lambda_{\Delta}) = 0$$

MMC circulating current calculation for phase independent control (2/2)



Control Scheme – Phase Independent Control of the MMC based on Mathematical Optimization

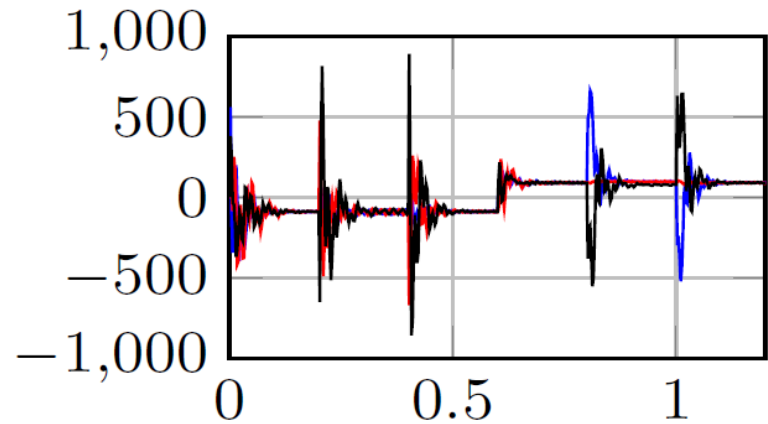
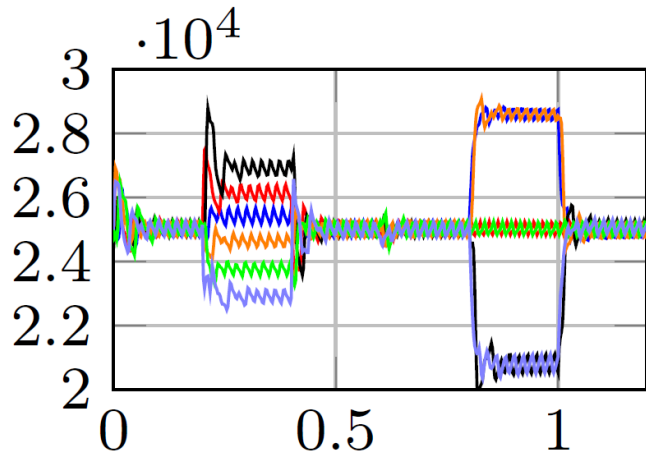


Some Simulation Results:

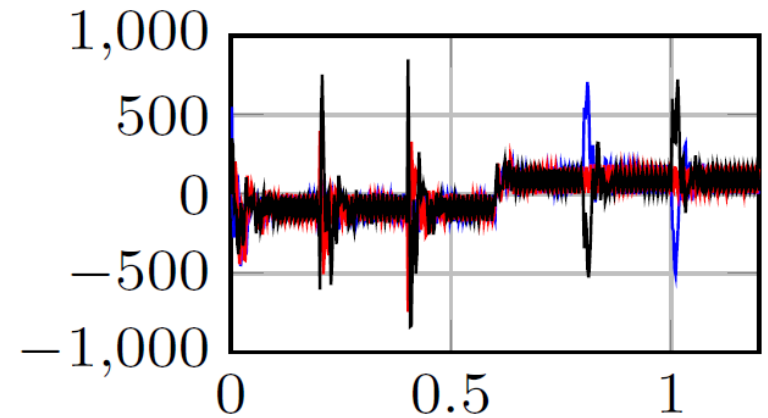
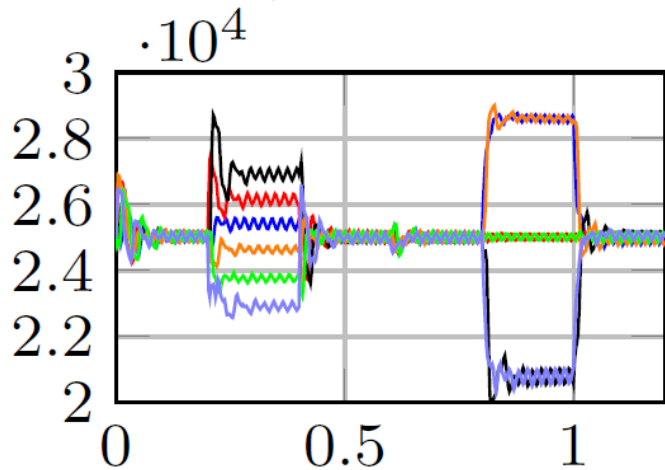
Capacitor Voltages (V)

Differential Currents (A)

$\alpha=0$



$\alpha=1$

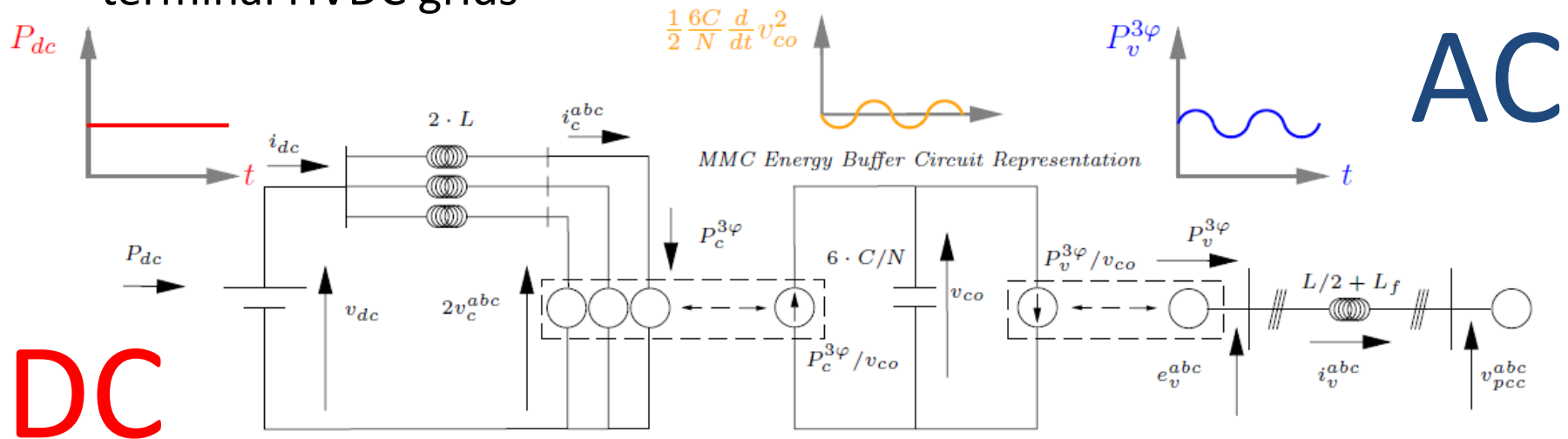


Part III: The MMC Energy Buffer

CIRCULATING CURRENT SIGNAL FOR CONSTANT POWER UNDER UNBALANCED GRID CONDITIONS

DC

- # AC



Circulating current reference calculation suited for unbalances.

- Limitations of the circulating current reference equation:
 - The optimization procedure used considered each phase of the MMC completely independent!
 - This implies that it did not include the possibility for optimizing the operation of a 3-phase converter under an unbalanced condition in the AC grid.
- A new optimization is therefore required!
 - The goal is to always ensure constant power at the DC terminals of the converter.

New Optimization Problem, suitable for unbalanced grid conditions:

Reduce the difference between the NEW circulating current and the one previously calculated.

$$\mathcal{L}(i_{ck}, \lambda) = \left(i_{ck} - \mathbf{I}_{ck}^{*Eq.} \right)^2 + \lambda \left(v_{dc} \sum_{k \in (abc)} i_{ck} - P_{dc}^{ref} \right)$$

Constant Power at the DC terminals of the MMC

Former circulating current equation

$$\frac{\bar{P}_{\Sigma k}^{ref} + (1 - \alpha) \bar{P}_{vk}}{v_{dc}^2} v_{dc} + \frac{\alpha P_{vk}}{v_{dc}} + \frac{-\bar{P}_{\Delta k}^{ref} e_{vk}}{2v_{dc}^2 \left(e_{vk, p.u.}^{rms} \right)^2}$$

Solving: $\nabla_{(i_{diffk}, \lambda)} \mathcal{L}(i_{diffk}, \lambda)$, we obtain:

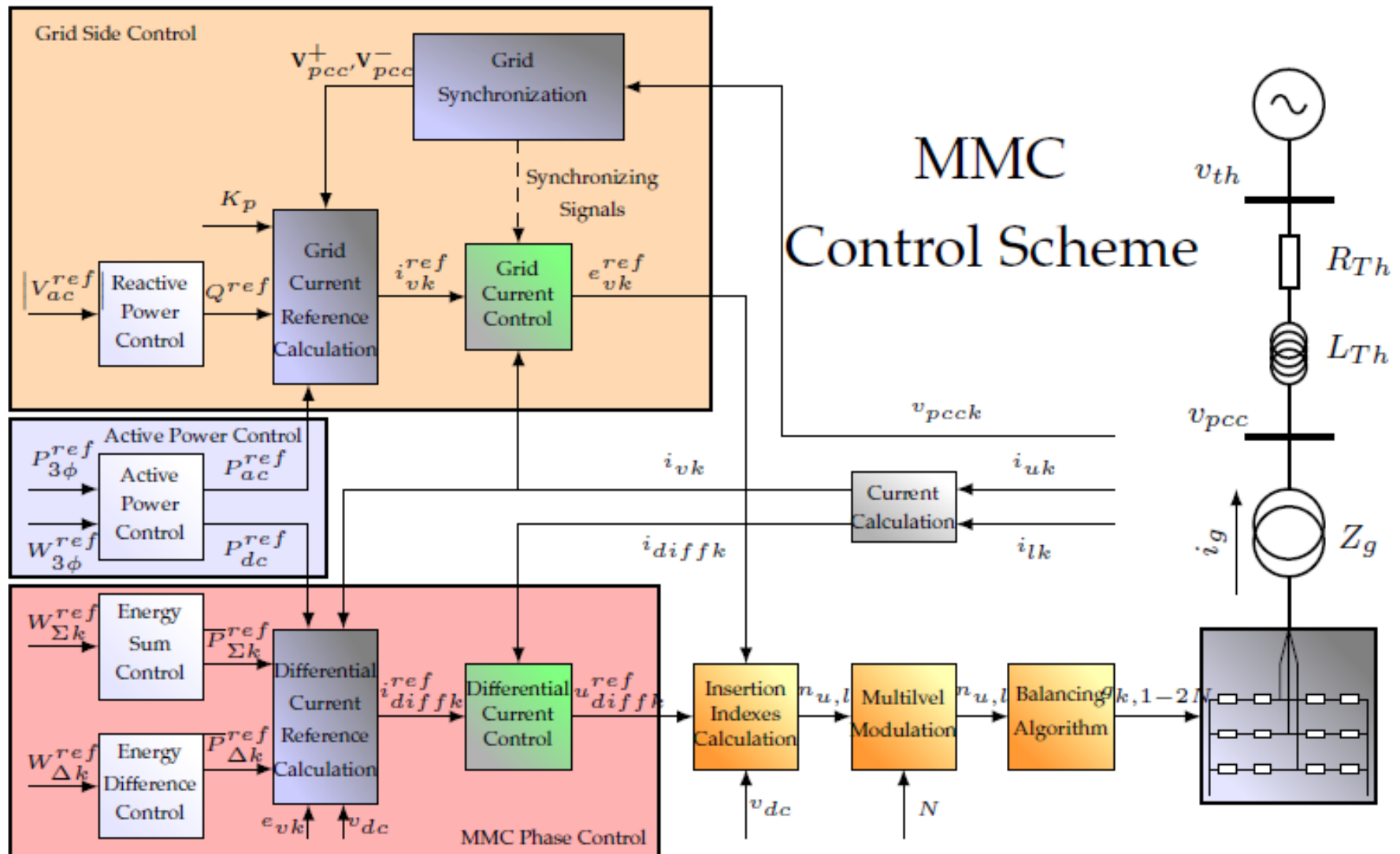
$$i_{ck} = \textcircled{\mathbf{I}_{ck}^*} + \underbrace{\frac{1}{3} \frac{P_{dc}^{ref}}{v_{dc}} - \frac{1}{3} \sum_{k \in (abc)} \textcircled{\mathbf{I}_{ck}^*}}_{\text{Possibility to control the DC power through the circulating current}}$$

Possibility to control the
DC power through the
circulating current

Or the more extended version:

$$i_{ck} = \frac{\bar{P}_{\Sigma k}^{ref} + (1 - \alpha) \bar{P}_{vk}}{v_{dc}^2} v_{dc} + \frac{\alpha P_{vk}}{v_{dc}} + \frac{-\bar{P}_{\Delta k}^{ref} e_{vk}}{2v_{dc}^2 \left(e_{vk, p.u.}^{rms} \right)^2} - \sum_{k \in (abc)} \left(\frac{\bar{P}_{\Sigma k}^{ref} + (1 - \alpha) \bar{P}_{vk}}{v_{dc}^2} v_{dc} + \frac{\alpha P_{vk}}{v_{dc}} + \frac{-\bar{P}_{\Delta k}^{ref} e_{vk}}{2v_{dc}^2 \left(e_{vk, p.u.}^{rms} \right)^2} \right) + \frac{1}{3} \frac{P_{dc}^{ref}}{v_{dc}}$$

MMC Control Scheme suitable for balanced and unbalanced grid operation

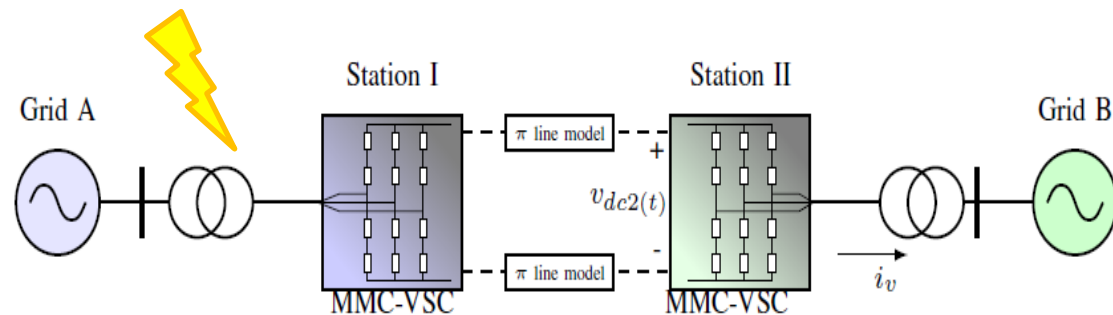


Simulation Results

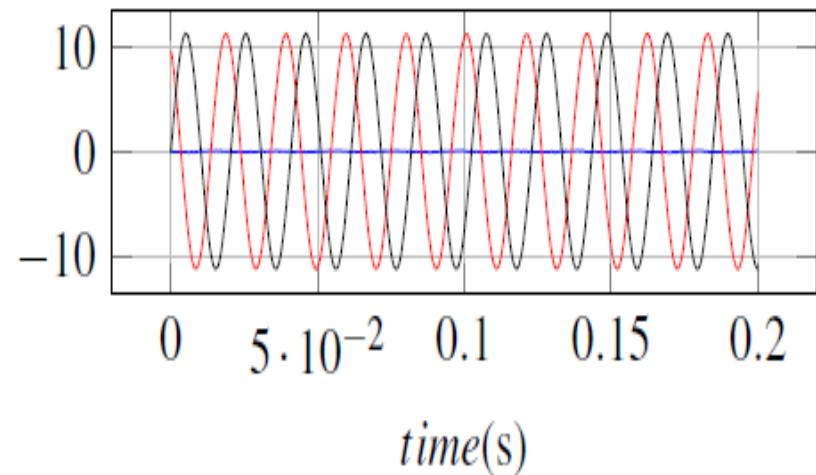
Unbalanced fault

AC/DC

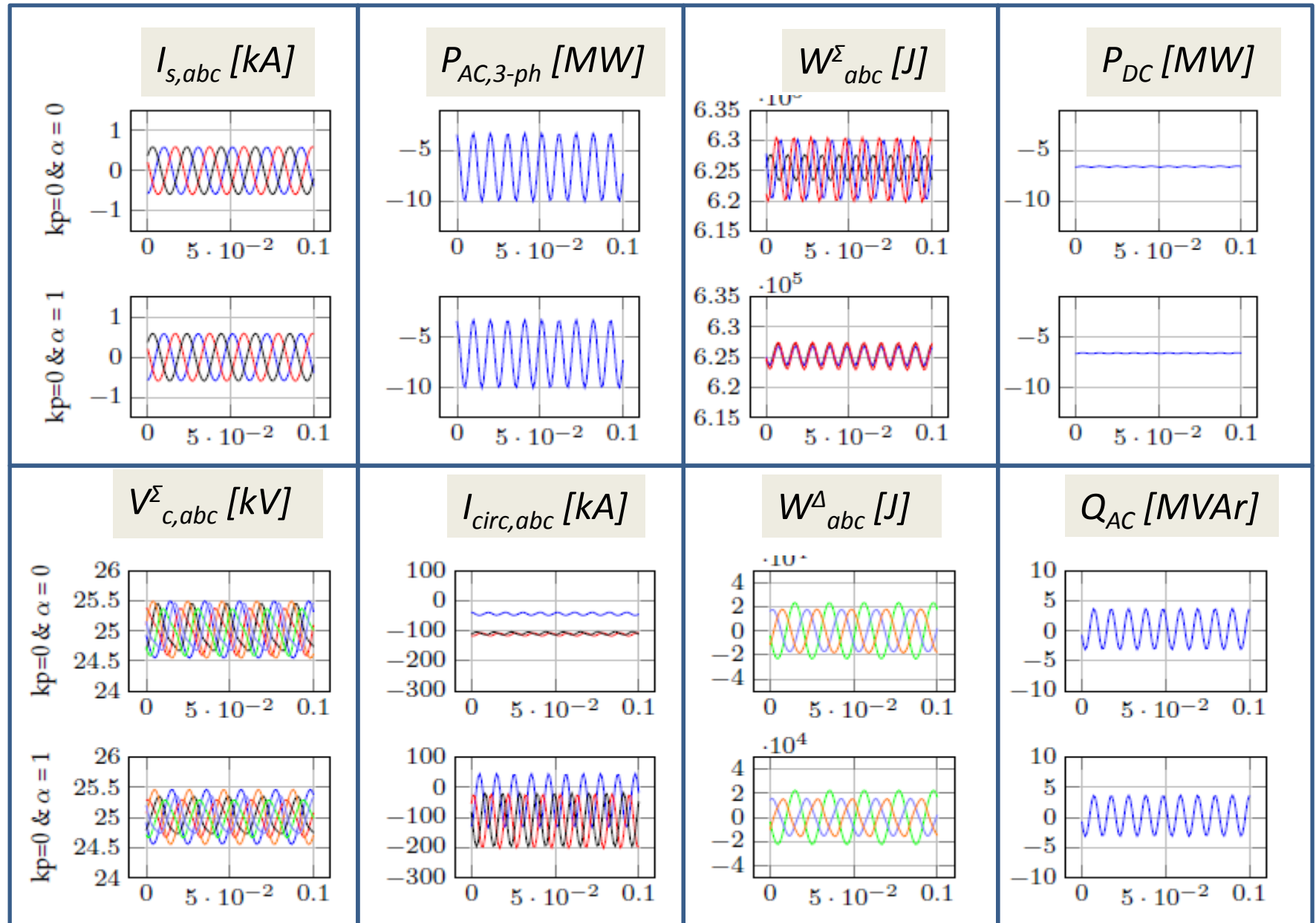
DC/AC



Parameter	Value
Number of SM per arm	100
SM Nominal Voltage	5kV
SM Capacitance	5mF
Arm Inductance	3mH
Arm Resistance	0.1Ω



Proposed Control scheme suited for unbalances



Operation with $\alpha=0$: Constant differential current

Operation with $\alpha=1$: Minimized sum energy oscillations for all phases

Almost done!

CONCLUSIONS

- An control scheme in the "abc" frame, based on mathematical optimization is presented.
 - Using the Lagrange multipliers method, it is posible to calculate a minimized circulating current equation used as reference for the control action.
 - The control is able to ensure constant, non-oscillatory power flow at the DC side of the converter, even under unbalanced grid conditions.
- Such operation can be especially relevant for (multi-terminal) HVDC systems, where power fluctuations, and thus DC voltage fluctuations must be avoided because they negatively influence other converters connected to the same DC grid.

Merci!