

# Passive Intermodulation Distortion, Part 2

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with

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and Josh Wetherington

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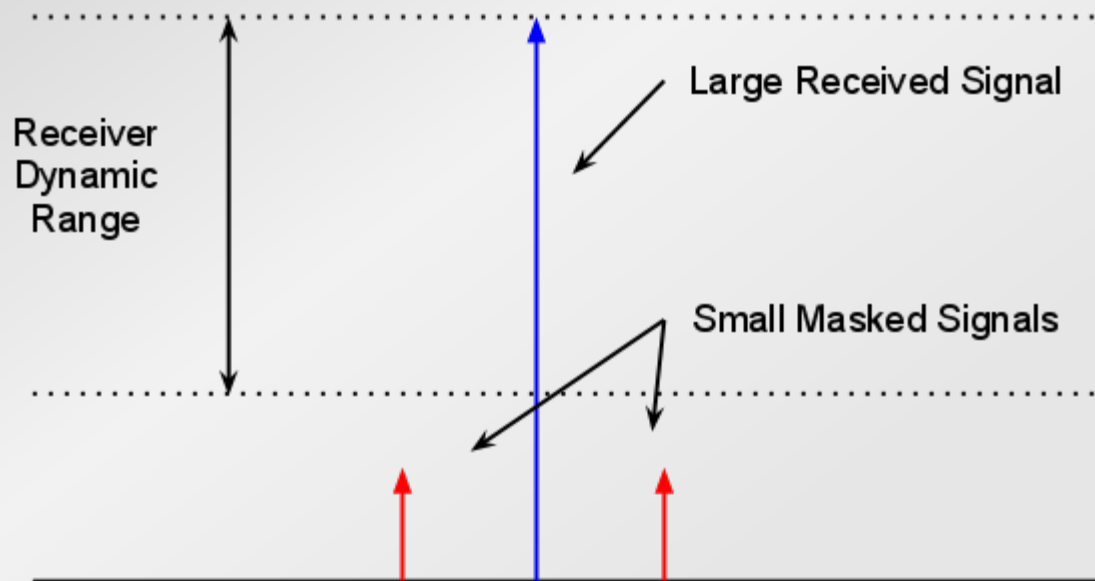
# Outline

- Background
- Passive Intermodulation Distortion (2 parts)
  - Part 1, PIM effects, Electro-Thermal PIM
    - Test Equipment, Microwave Circuits / Antennas
  - Part 2, PIM effects
    - Non Electro-Thermal PIM, Filter PIM
- Behavioral Modeling
  - Behavioral model
  - Measurement Equipment
- Simulation and Modeling of Large Systems
  - Part 1, New circuit concepts
  - Part 2, fREEDA

# **PIM Measurement System (Analog Canceller)**

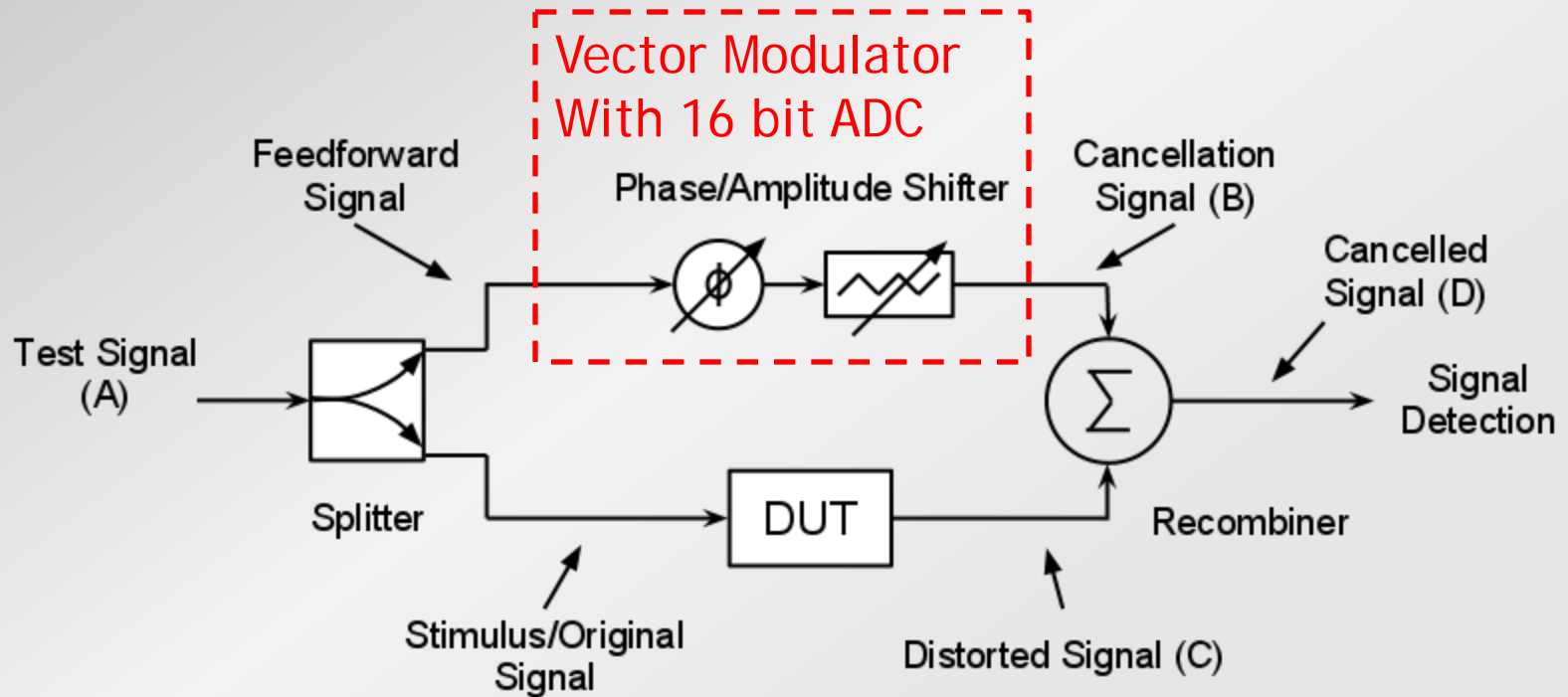
# Problem

- Need to measure small signals in the presence of large signals.
  - E.g. GPS receiver, radar, distortion measurement



# Cancellation Theory

- Sum with equal amplitude/anti-phase signal of original signal



# Cancellation Theory

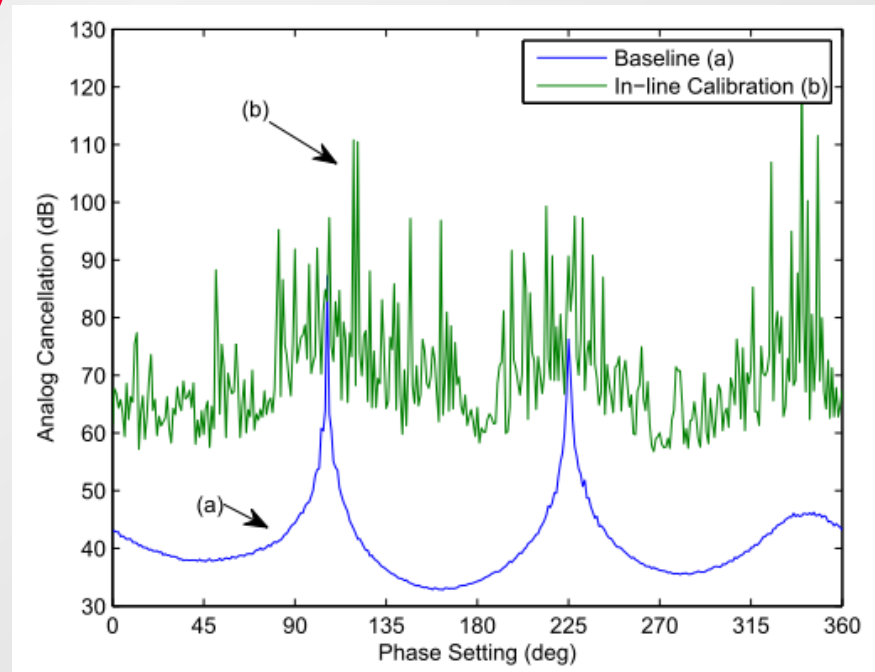
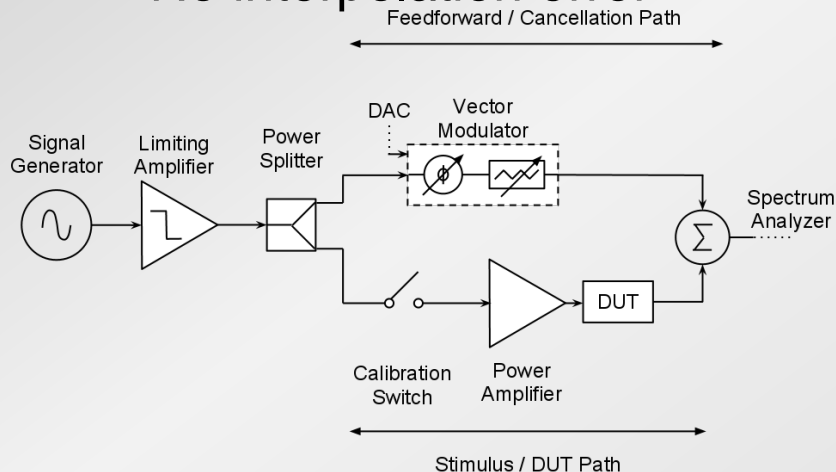
- Amplitude Measurements Only
- Non Newton-Based Iteration

## Cancellation Errors

- Phase error:
  - Mostly result of errors in  $\beta$  and  $\alpha$  in  $\theta_s$  equation
  - Dependent on phase separation of signals
  - Can be minimized in iteration
- Amplitude error:
  - Results from path non-linearities
  - Dependent on phase, frequency, time
  - More sensitive than phase errors due to sole reliance on amplitude measurement
  - Minimized through path amplitude calibration

# Amplitude Calibration

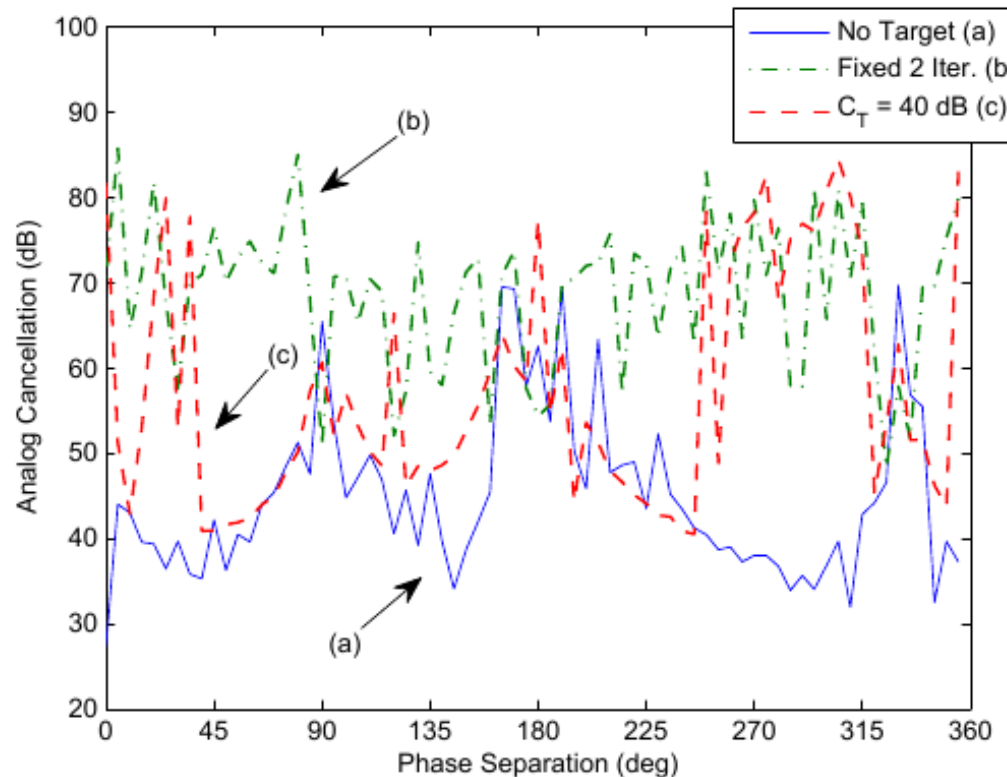
- **Standard (baseline): Generate calibration matrix: Ampl. vs. Freq.**
  - Occurs pre-test
  - Does not capture time-dependent or phase-dependent effects
  - Only needs to be done once (ideally)
  - Speed depends on density of matrix
  - Inherent interpolation error
- **In-line: Perform calibration on-the-fly**
  - Occurs during cancellation
  - Minimizes time-dependency
  - Very fast: single measurement
  - No interpolation error



# Analog Cancellation

- Initial cancellation is statistical
  - Cancellation converges to 70-90 dB

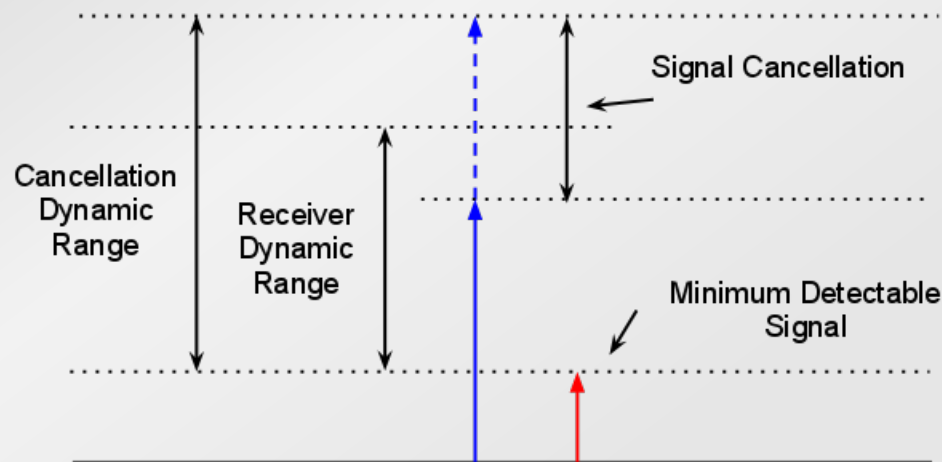
Target $C_T$ (dB)	Iterations				Meas. analog cancellation (dB)			
	Av.	Max	Md.	$\sigma$	Av.	Max	Min	$\sigma$
0	1.00	1	1	0.00	45.0	69.7	27.3	9.5
30	1.01	2	1	0.12	46.4	79.3	31.2	10.4
40	1.31	2	1	0.46	56.9	84.5	40.5	13.3
50	1.72	3	2	0.48	67.0	84.5	50.3	10.0
60	2.01	4	2	0.49	73.5	87.6	62.5	4.9
70	2.63	11	2	1.24	75.3	90.0	70.3	4.0
-	Forced 2 Iter.				68.6	85.8	48.3	8.7





# High Dynamic Range Measurement

- **Cancellation Dynamic Range ( $DR_C$ ):**
  - Ratio of the highest-power signal that can be cancelled to the minimum detectable signal (MDS) after cancellation
  - Not simple combination of  $C_A$  and  $DR_R$

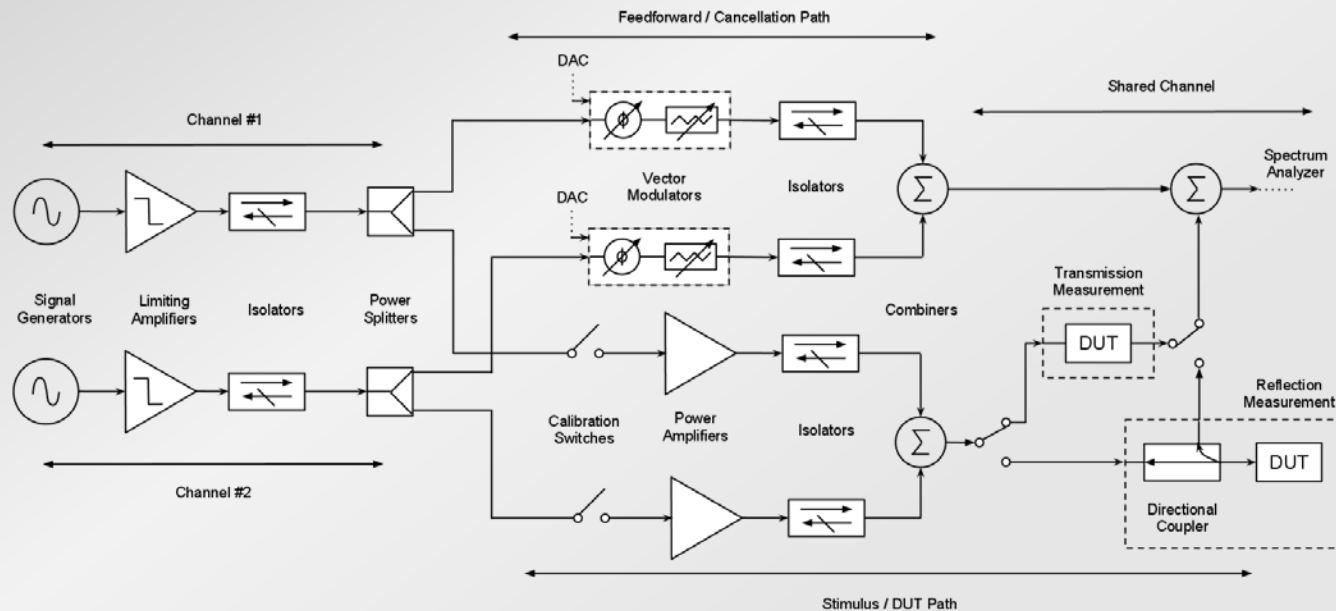


# High Dynamic Range Measurement

- **Limits on Dynamic Range:**
  - RF signal source spurious leakage
    - Suppressed inherently through cancellation
  - Coupling of external RF emissions
    - Suppressed through RF shielding/isolation
  - AC power supply leakage
    - Eliminate by using DC power (i.e. batteries)
  - System thermal noise
- **Ultimate limit on cancellation: quantization error**
  - Quantization in DAC leads to finite resolution for VM output step
    - Can be improved with attenuation at a cost to dynamic range
  - Quantization in receiver leads to finite resolution for measurement
    - Calibration accuracy cannot exceed measurement accuracy

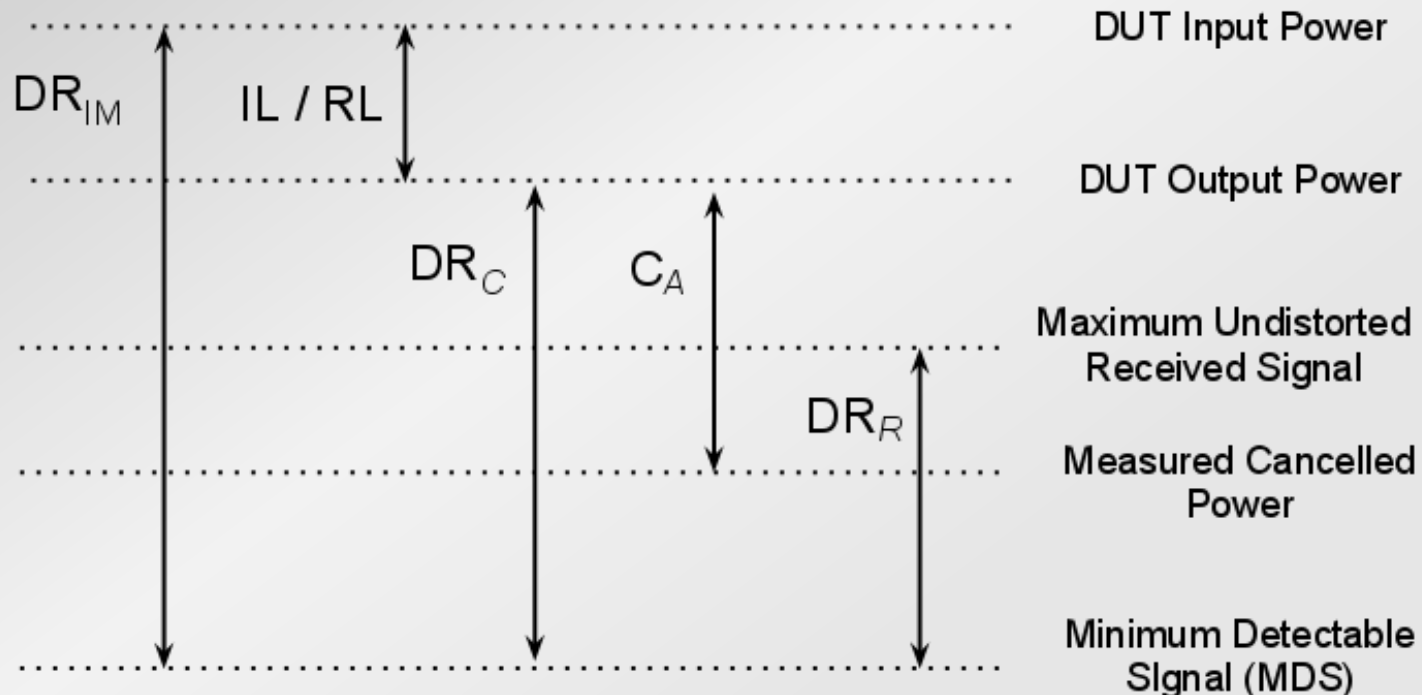
# Two-Tone IMD Measurement

- Two-tone IMD measurement system built using separate cancellers for each channel
- Can be used for transmission or reflection



# Intermodulation Dynamic Range, $DR_{IM}$

- The change in reference makes  $DR_{IM}$  theoretically independent of DUT characteristics and system configuration.

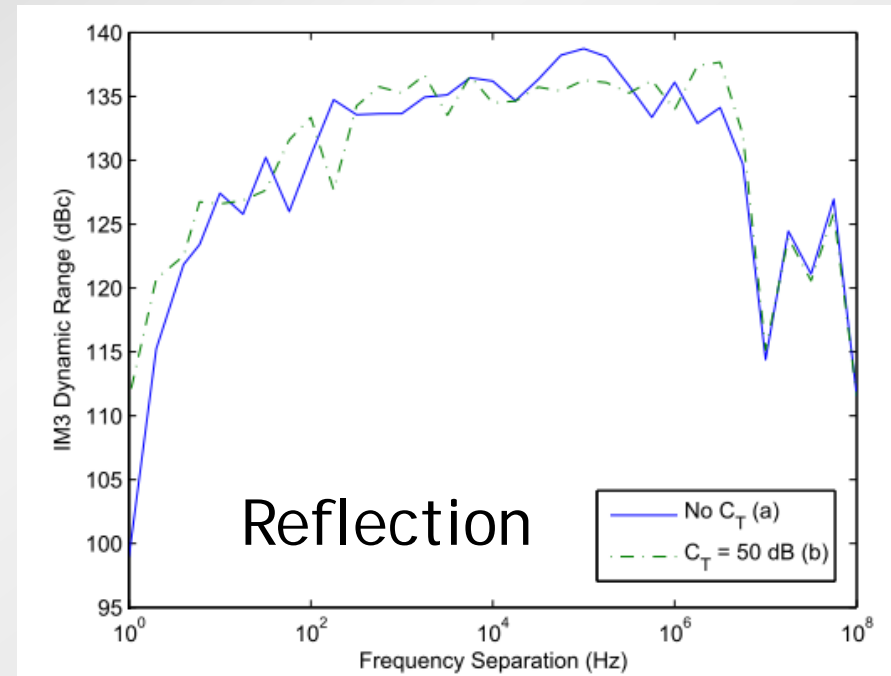
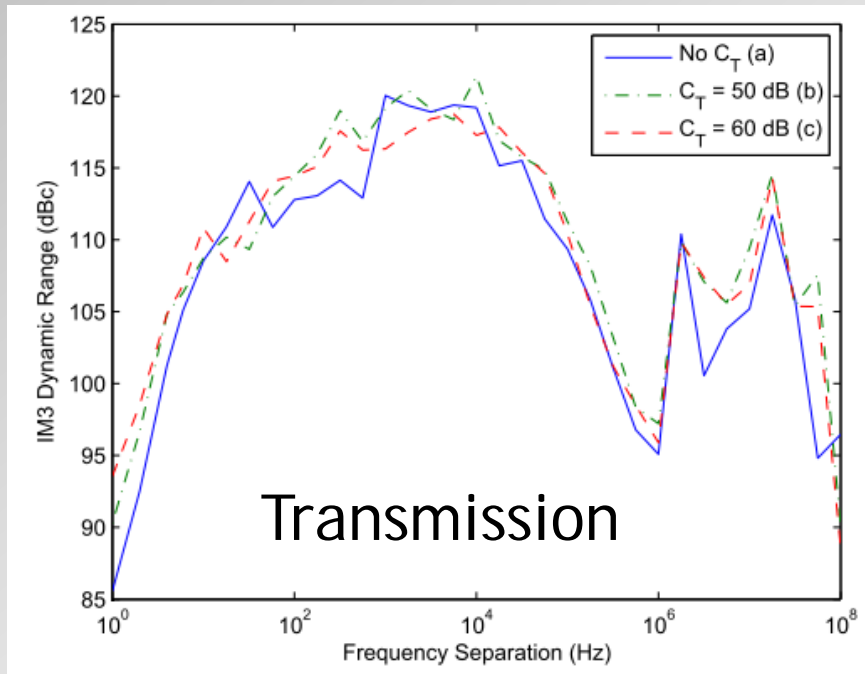


# Two-Tone IMD Measurement

- **Key to high dynamic range: linearity**
  - Isolators reduce undesired mixing of channels through reverse path
  - Minimize external spurious content
    - External RF coupling, AC supply leakage
  - Low-PIM components:
    - Silver-plated
    - Physically large
    - Distributed implementations
- **Bandwidth Limitations:**
  - Isolators (typically half-octave):
    - Narrowest bandwidth in system, but only limits frequency range of a single channel
  - Shared channel components
    - Wider bandwidth than isolators but must include entire frequency range from lower IM product to upper IM product
  - Bandwidth limitations only affect maximum tone separation; system emphasis is on very small tone separation (to 1 Hz)

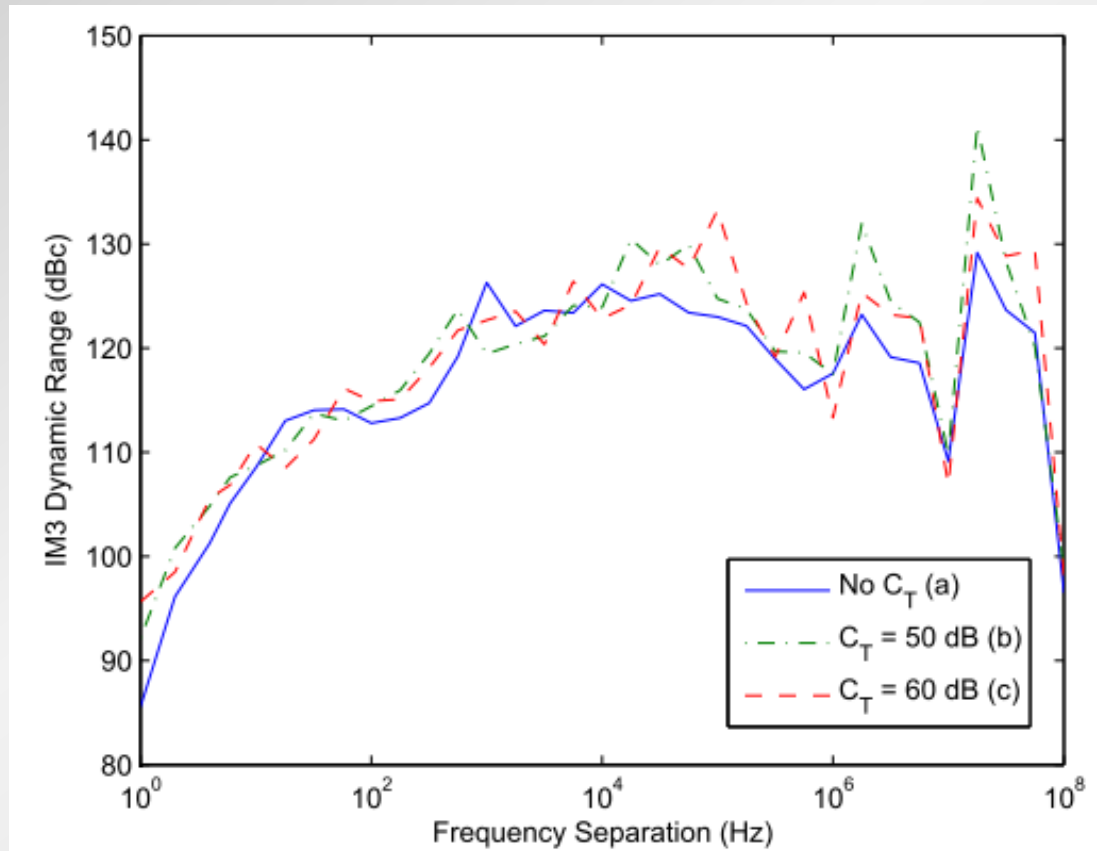
# Measured Results ( $DR_{IM3}$ )

- 460 MHz with an input power of 26 dBm.



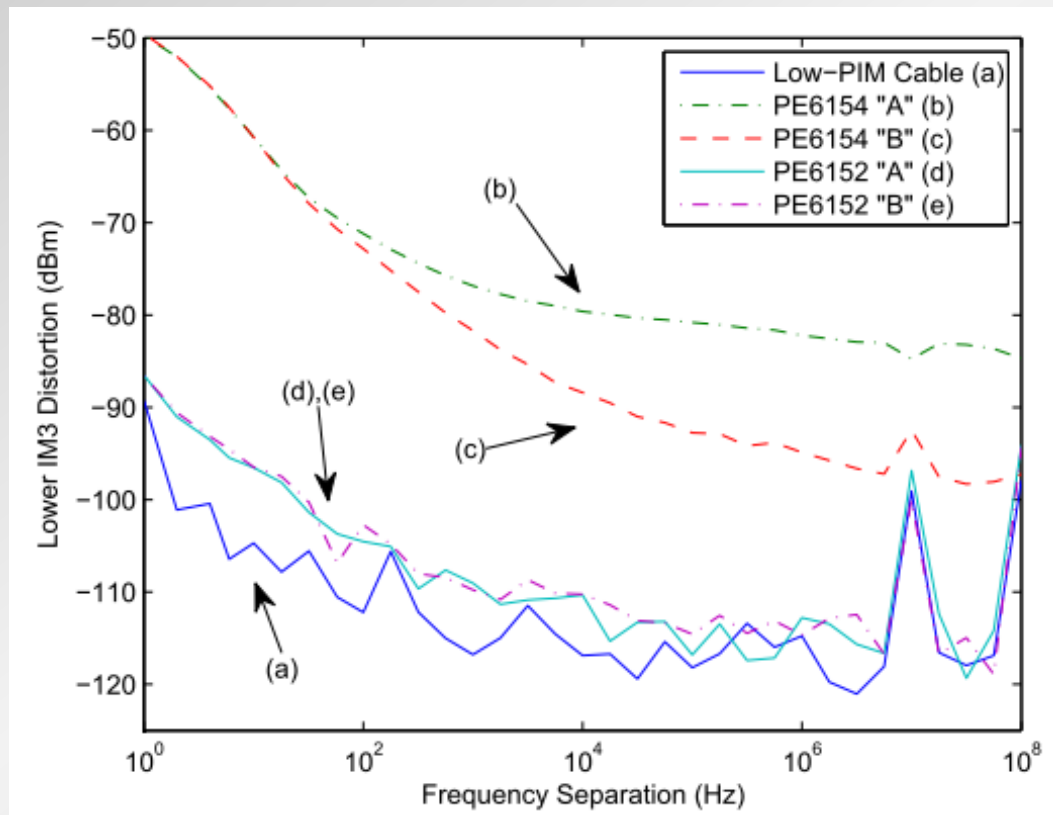
# Measured Results ( $DR_{IM3}$ )

- Spurious tone at 1 MHz only shows up in upper IM3 in transmission
  - Source currently unknown



# Measured Results (PIM)

- Pasternack PE6154, PE6152
  - Standard 2W terminations, similar form-factor

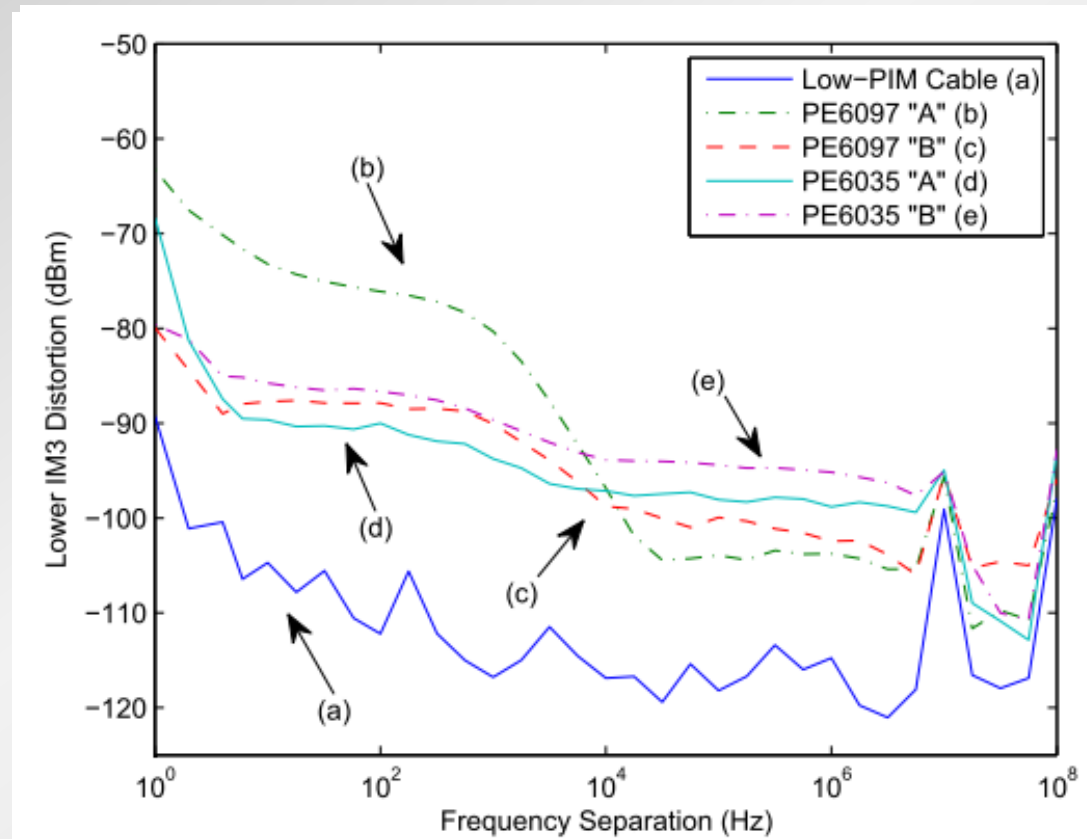


Lower IM3



# Measured Results (PIM)

- Pasternack PE6097 (5W), PE6035 (10W)
  - High power, terminations with large “finned” aluminum heatsinks



Lower IM3

# Summary PIM Measurement

- **Analog Canceller**

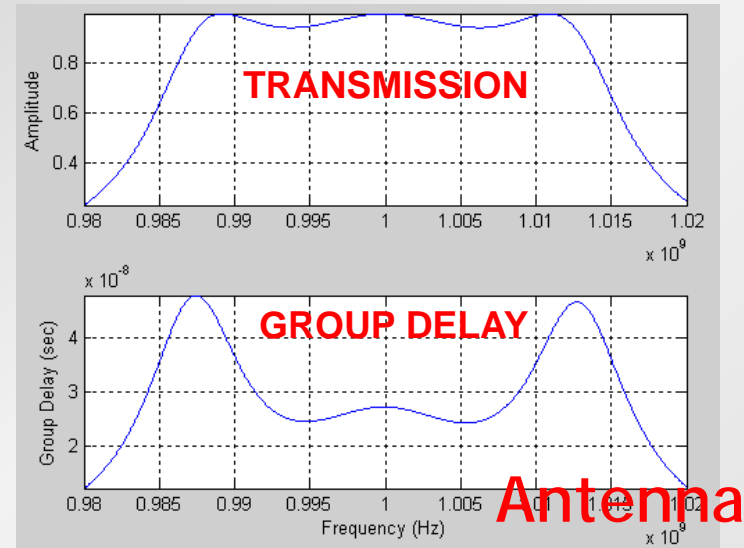
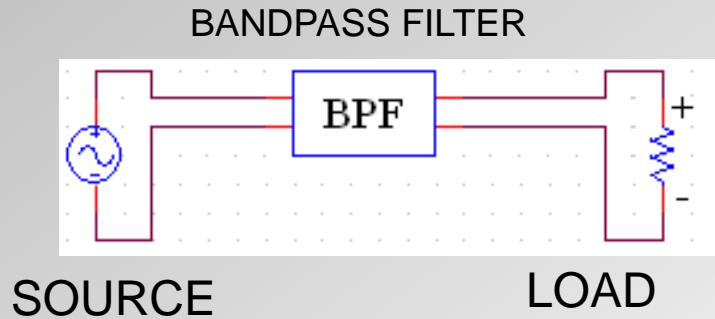
- Minimum  $DR_{IM3}$  :
  - Transmission: 94 dBc at 1 Hz ( $C_T = 60$  dB)
  - Reflection: 111 dBc at 1 Hz ( $C_T = 50$  dB)
- Minimum  $DR_{IM3}$  between 100 Hz – 30 kHz:
  - Transmission: 113 dBc ( $C_T = 60$  dB)
  - Reflection: 130 dBc ( $C_T = 50$  dB)
- Limited improvement with additional cancellation except at  $\Delta f < 10$  Hz
  - At these tone separations, the MDS is the phase noise off the carrier signals: extra cancellation directly reduces the MDS, improving  $DR_{IM3}$
- Spurious tones reduce performance at 10 MHz, and 100 MHz
  - Sources currently unknown

# References

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- J. R. Wilkerson, K. G. Gard, and M. B. Steer, "Automated broadband high-dynamic-range nonlinear distortion measurement system," *IEEE Trans. Microwave Theory and Techniques*, vol. 58, no. 5, pp. 1273-1282, May 2010.
- J. Henrie, A. Christianson, W. J. Chappell, "Prediction of passive intermodulation from coaxial connectors in microwave networks," *IEEE Trans. Microwave Theory and Techniques*, vol. 56, no. 1, pp. 209-216, Jan. 2008.
- J. R. Wilkerson, K. G. Gard, A. G. Schuchinsky, and M.B. Steer, "Electro-thermal theory of intermodulation distortion in lossy microwave components," *IEEE Trans. Microwave Theory and Techniques*, vol. 56, no. 12, pp. 2717-2725, Dec. 2008.
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- J. R. Wilkerson, K. G. Gard, and M.B. Steer, "Electro-thermal passive intermodulation distortion in microwave attenuators," *Proc. 36th Eur. Microwave Conf.*, 10-15 Sept. 2006, pp. 157-160

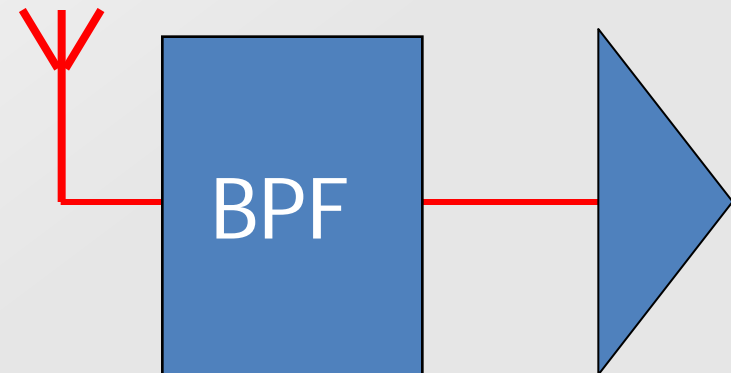
# Time-Frequency Effect Filter PIM

# Delay Effects in Filters

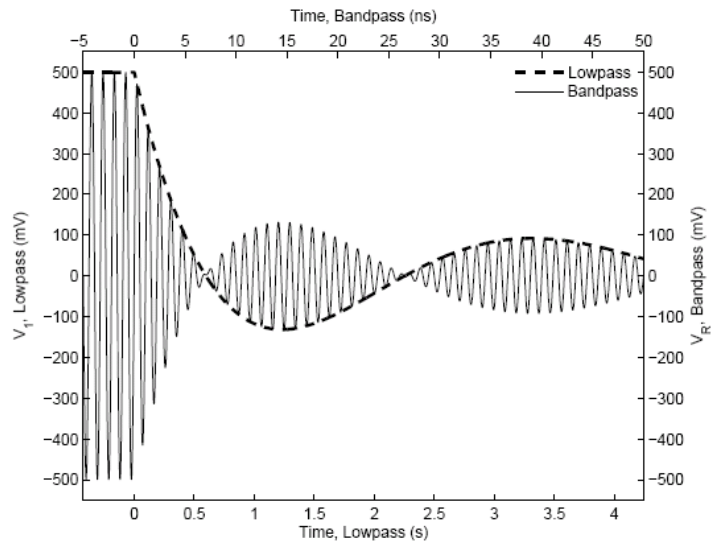
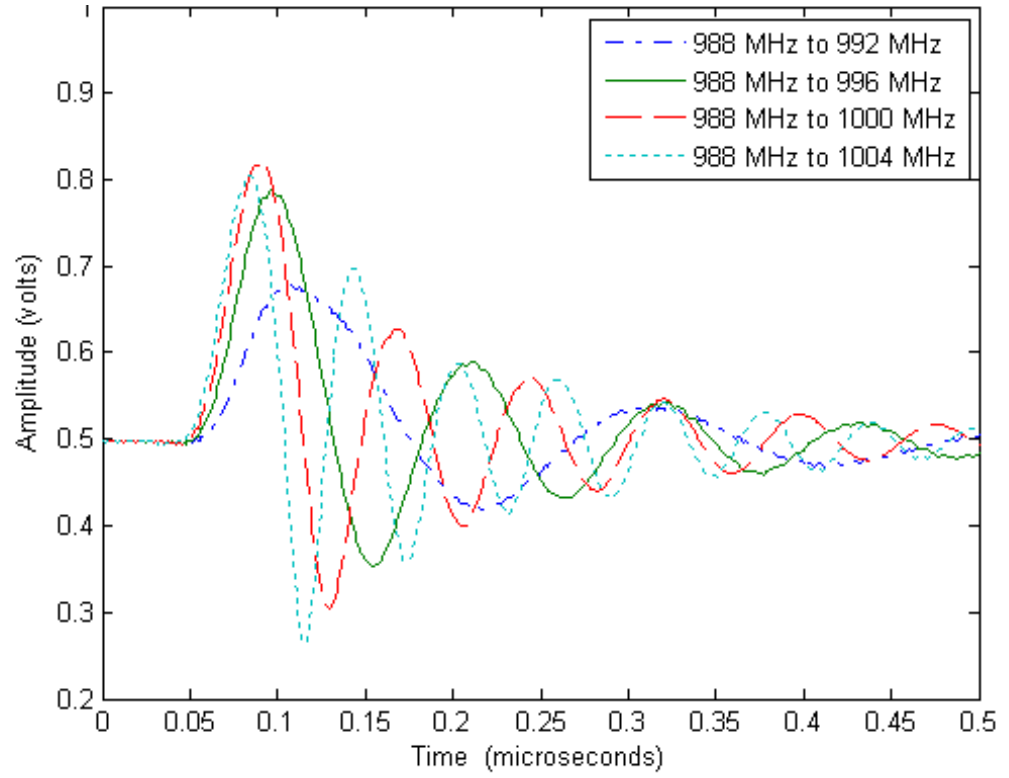
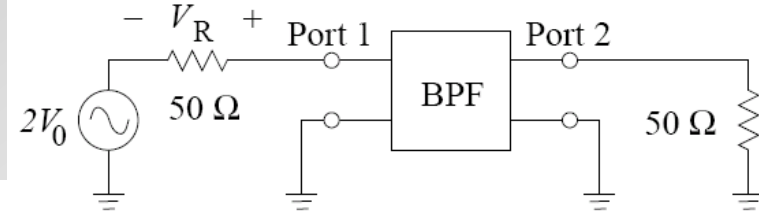
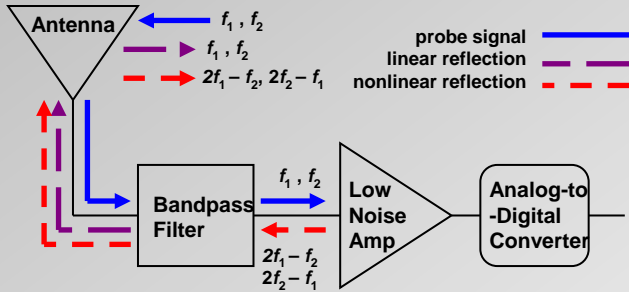


## Thesis:

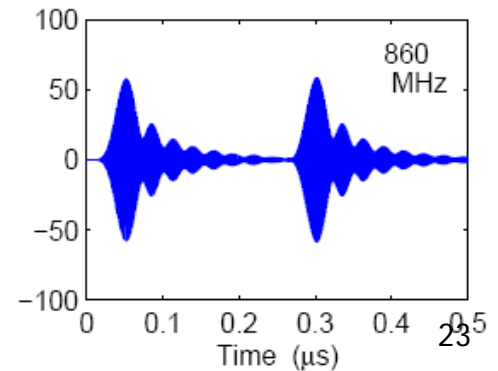
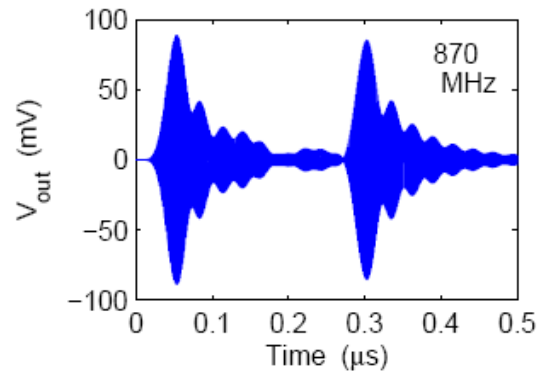
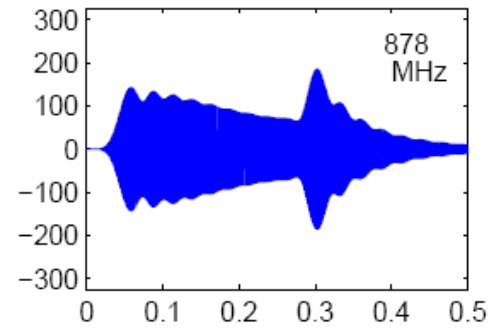
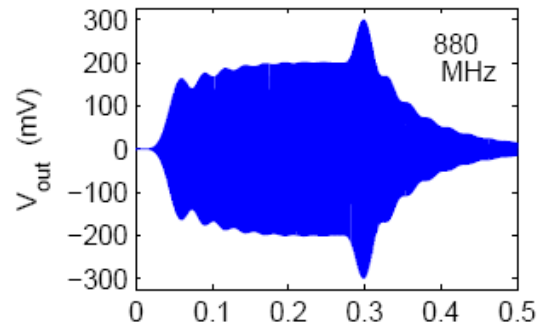
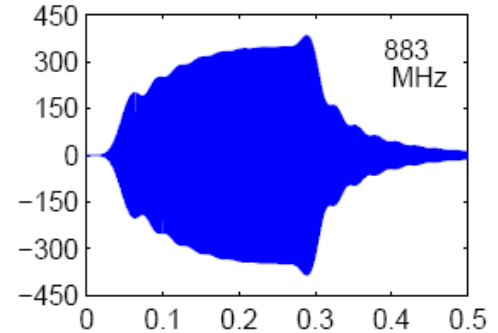
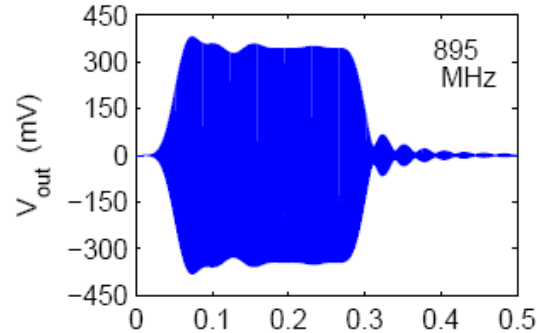
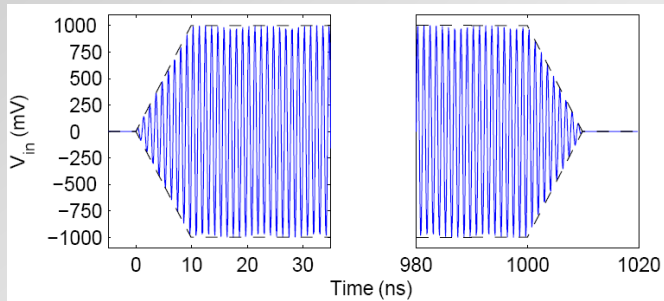
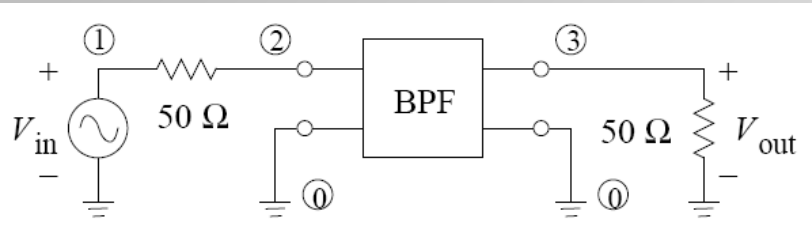
Can we use variation in group delay to develop an optimum waveform to create large nonlinear effects.



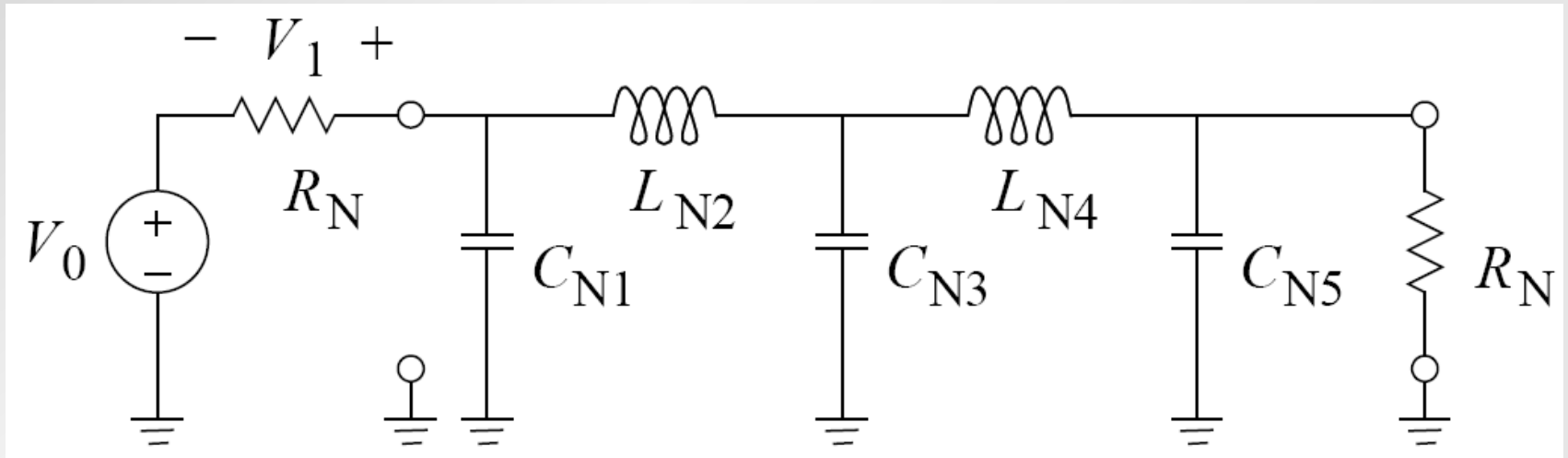
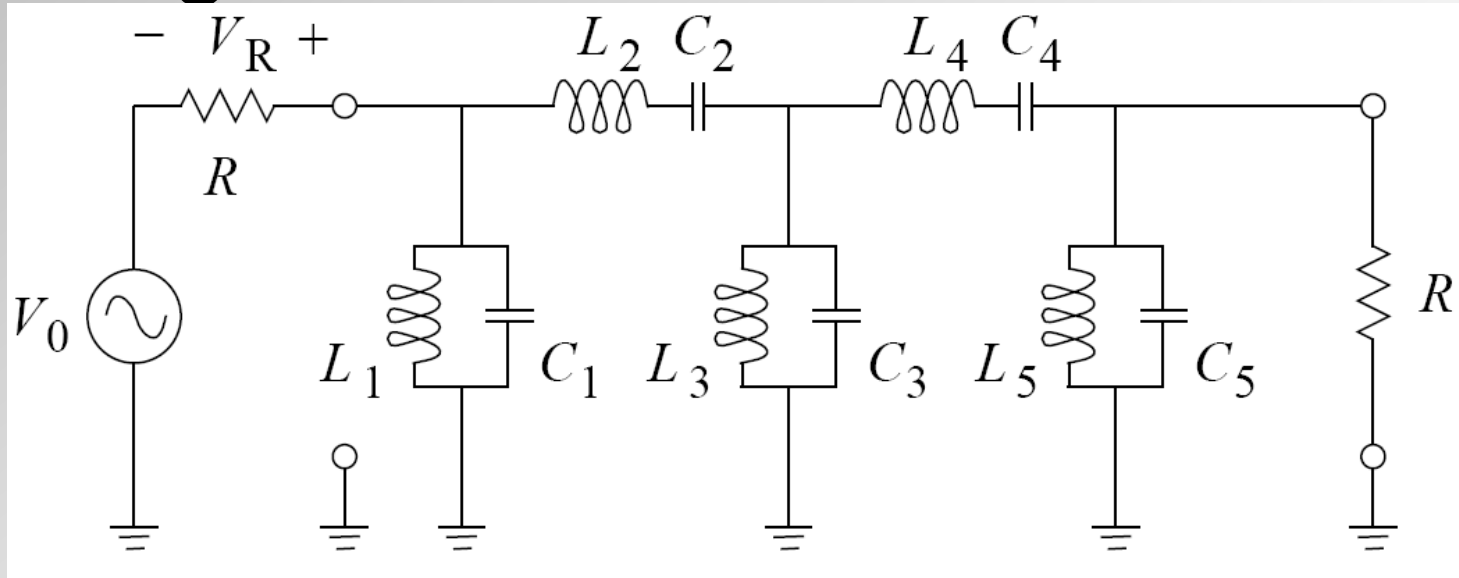
# Switched Tone Response of a Filter



# Time-Frequency Response of a Filter

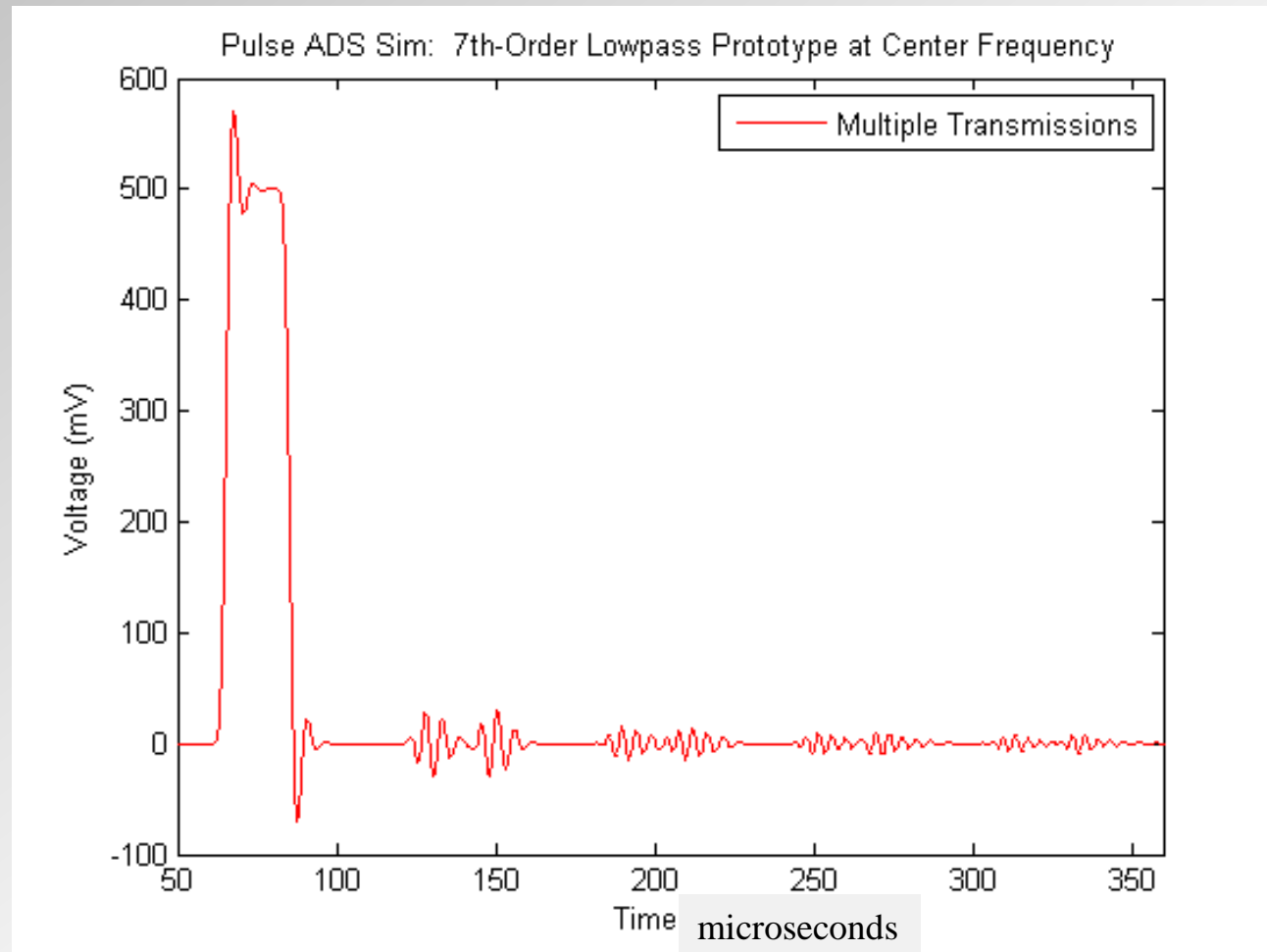


# Modeling

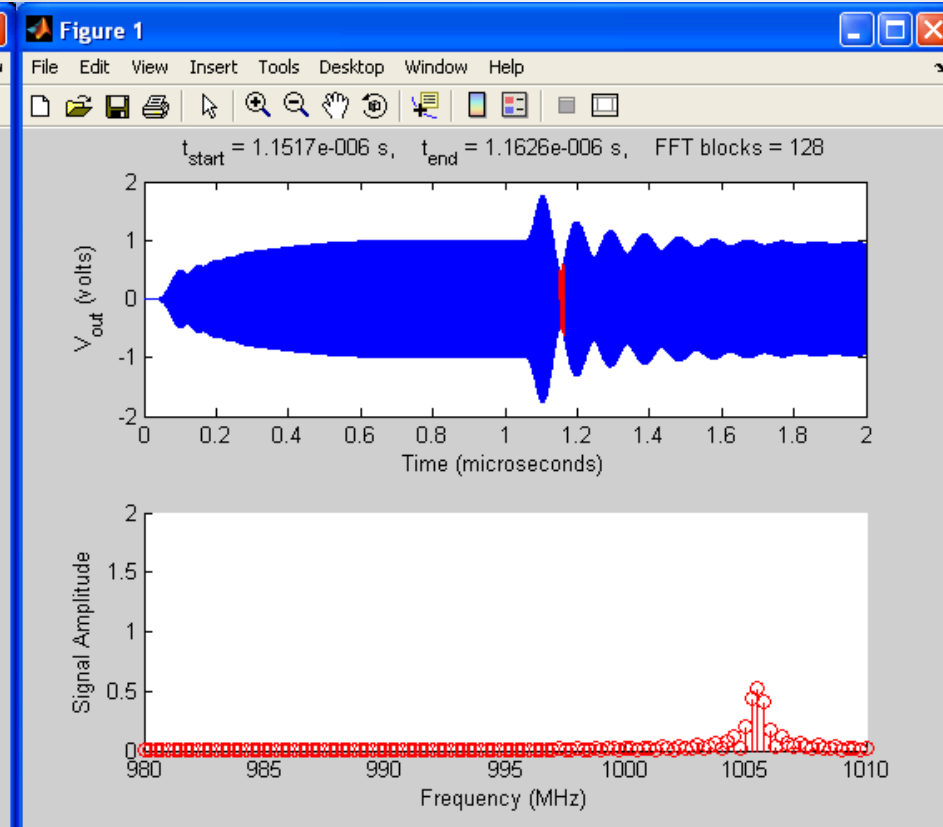
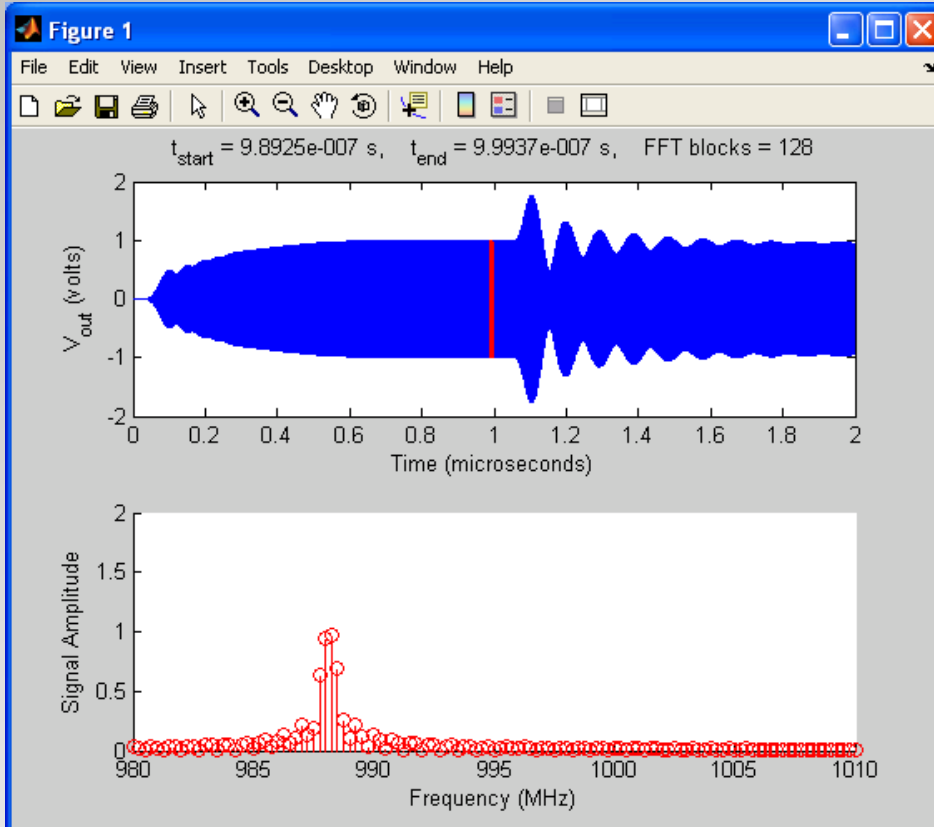




# Memory Effect

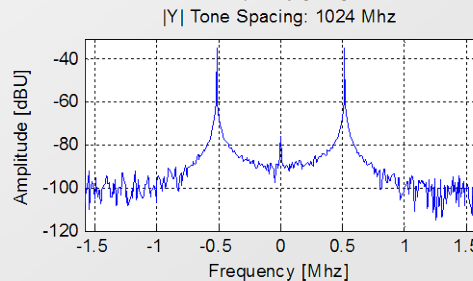
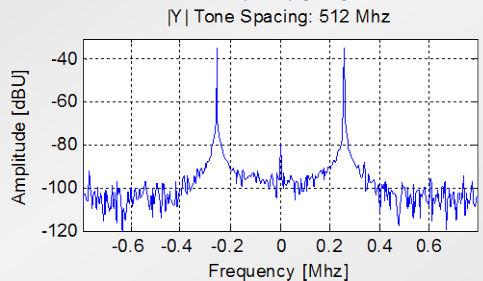
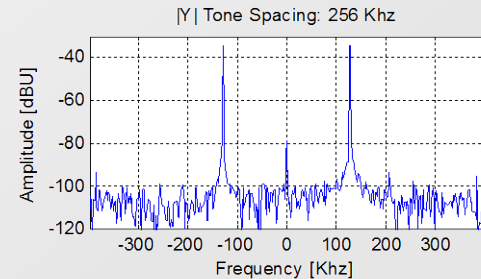
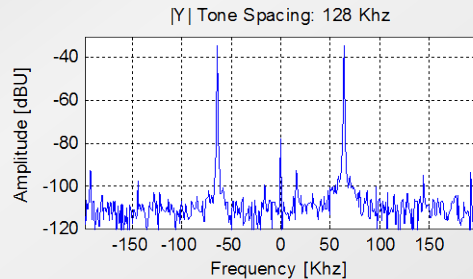
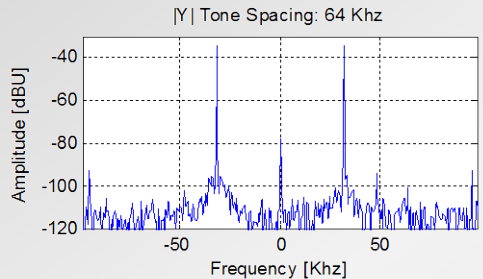
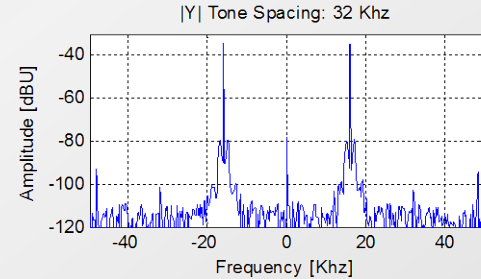
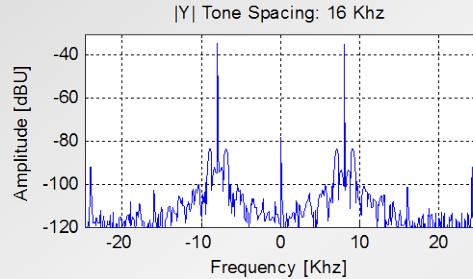
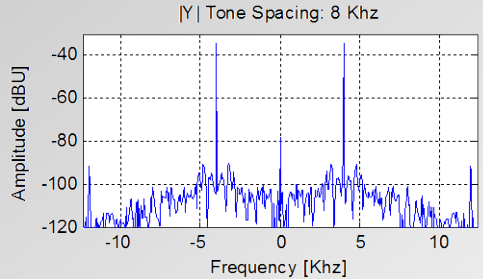
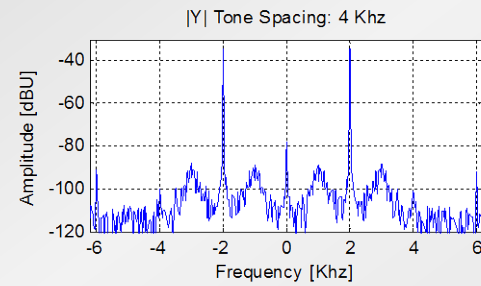
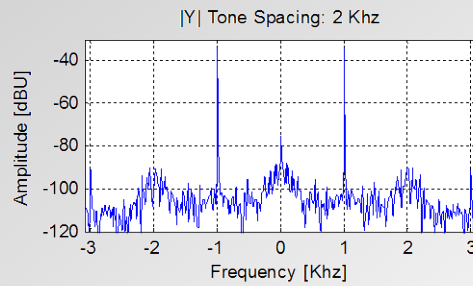
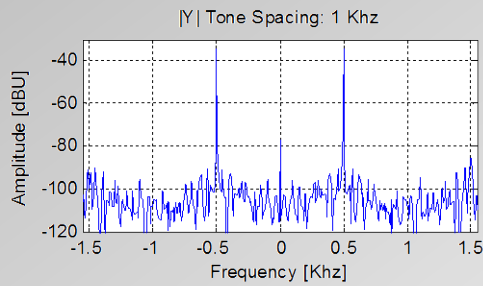


# Linear PIM



# Stepped Two-tone Signals

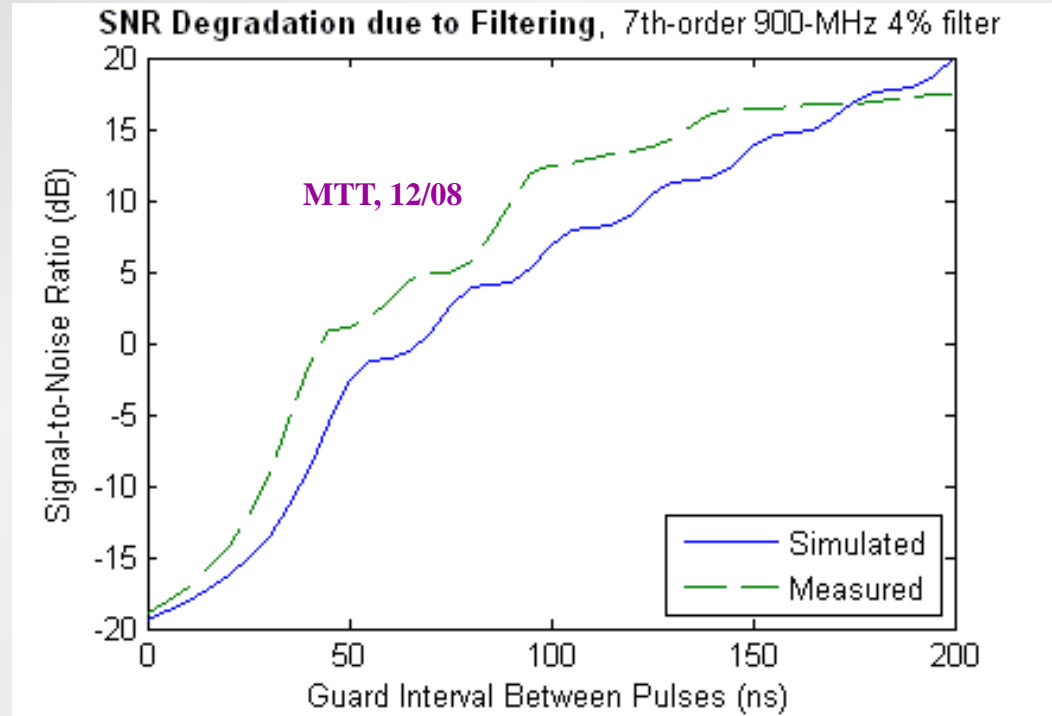
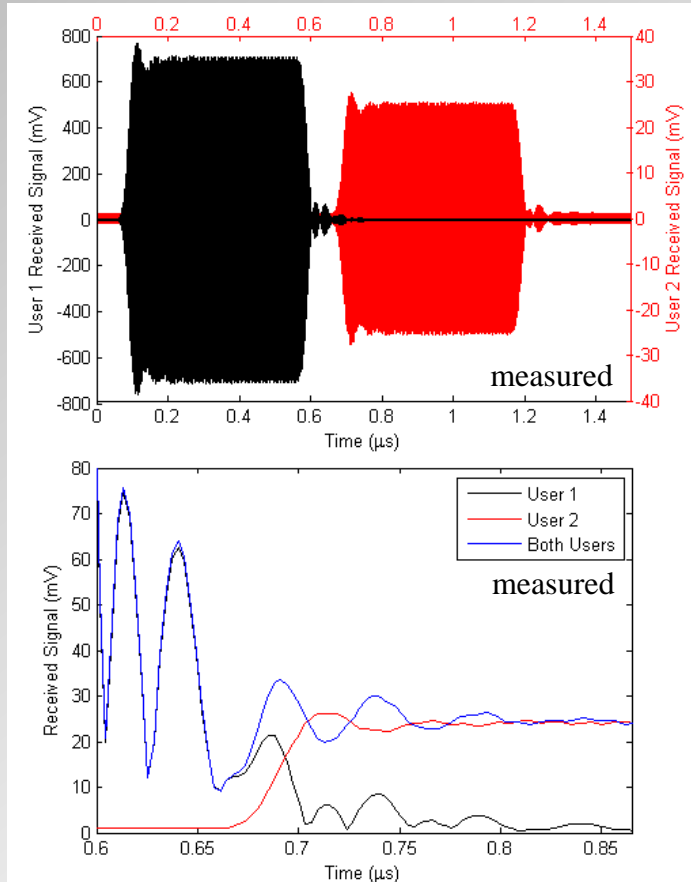
Frequency separation stepped logarithmically from 1 kHz to 1 MHz



# Time-Frequency Effects: Linear Transient Distortion

- What are the effects of these transients on wireless communications?

➤ sharp filtering can degrade received signal-to-noise ratio



**Filtered frequency-hopping pulses, 900-MHz 4% filter**  
 User 1 at 10 dBm, User 2 at -20 dBm  
 900 MHz, 100 ns guard interval

Nearest work:

**Chohan/Fidler (1973)** -- impact on FSK & PSK, no metric

# Time-Frequency Effects: Linear Metrology

• How do we measure parameters of coupled resonator circuits?

- the  $Q$  factor of the outer resonators in a chain may be determined with time-domain analysis

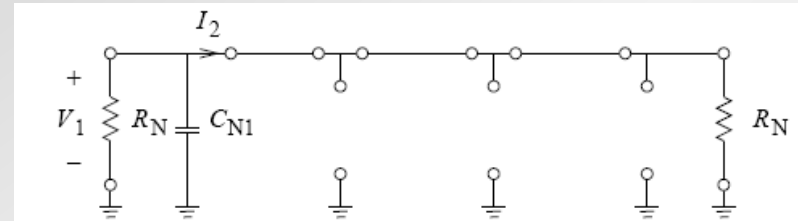
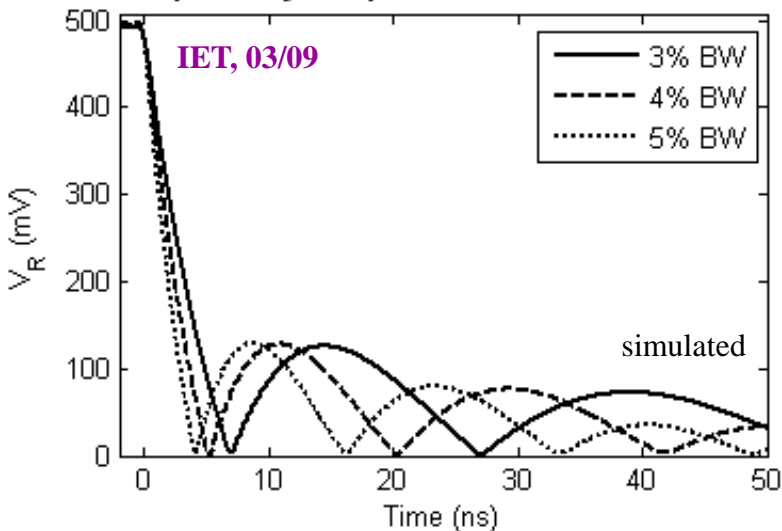


Figure 5: Equivalent lowpass circuit after source is zeroed

$$\frac{dV_1(0)}{dt_N} = -\frac{V_1(0)}{R_N C_{N1}} - \frac{I_2(0)}{C_{N1}} = -\frac{2}{R_N C_{N1}} V_1(0)$$

$$\tau = \frac{t}{\ln(V_0^2) - \ln(V_R^2(t))}$$

Envelope Decay at Input Port, 7th-order 900-MHz filters



900-MHz stimulus tone turned off at  $t = 0$  ns

Table 2: Measured Q-Value Estimation, 900 MHz Chebyshev Design

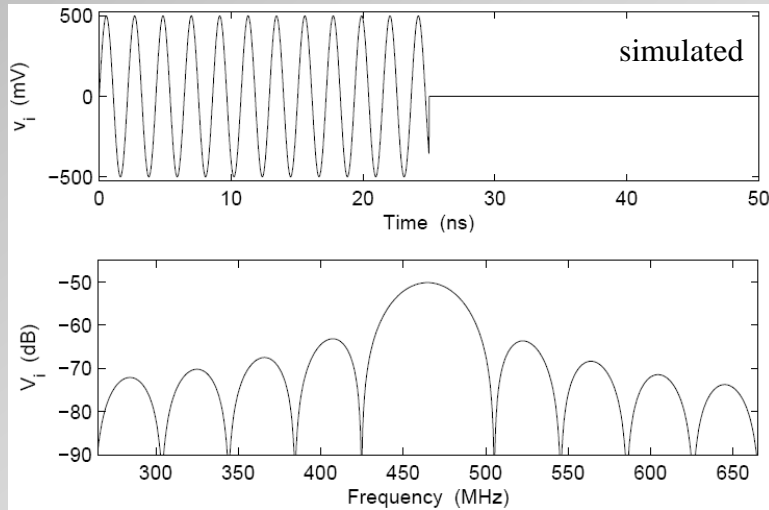
Filter Order	BW	Passband Ripple (dB)	2-Port Q Value	1-Port Q Value
7	4%	0.01	23.3	24.6
	5%	0.01	18.4	20.1

Nearest prior work:

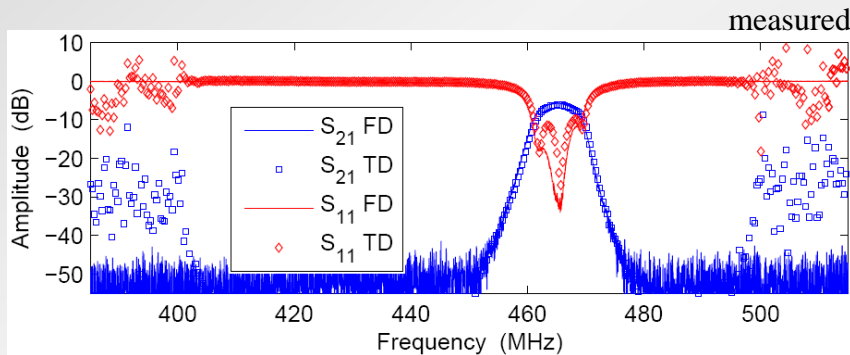
**Pereda (1992)** -- Prony analysis, dielectric resonators, not a ‘coupled’ structure

# Time-Frequency Effects: Linear Metrology

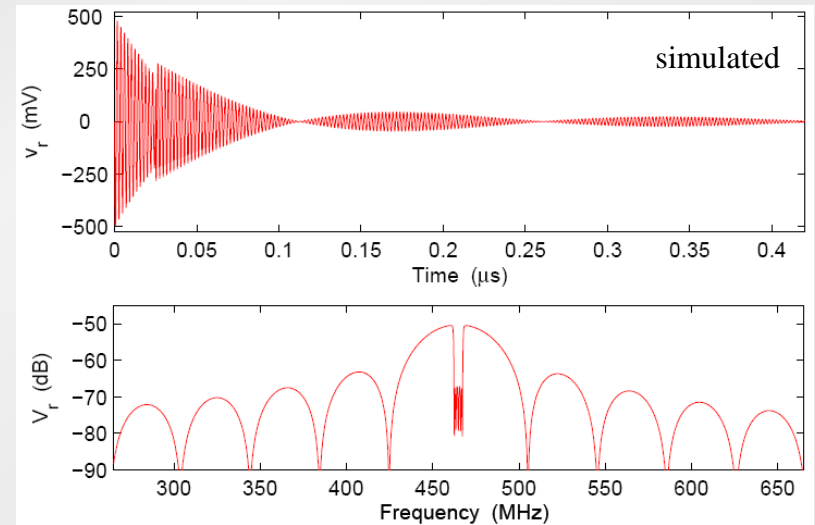
- How else can we exploit transients for metrology?



Time- & frequency-domain views, short pulses  
465-MHz 1% Chebyshev filters



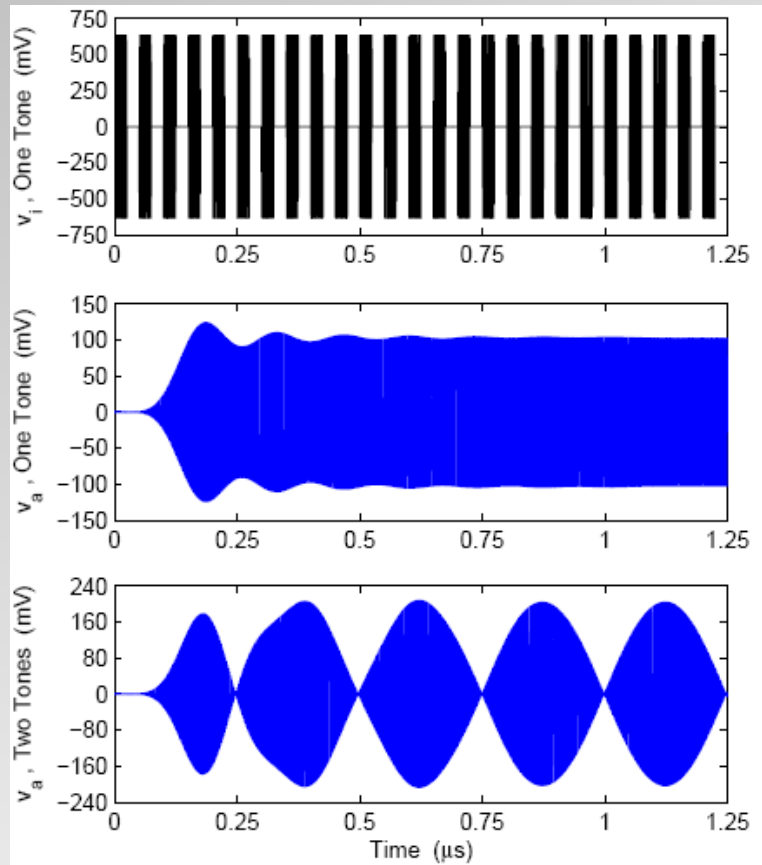
- 2-port  $S$ -parameters can be extracted from short-pulse time-domain responses



Nearest prior work:  
**Courtney (1999)** –  
permittivity measurements,  
nanosecond impulses

# Time-Frequency Effects: Nonlinear Metrology

- Can we exploit filter properties for nonlinear measurements?

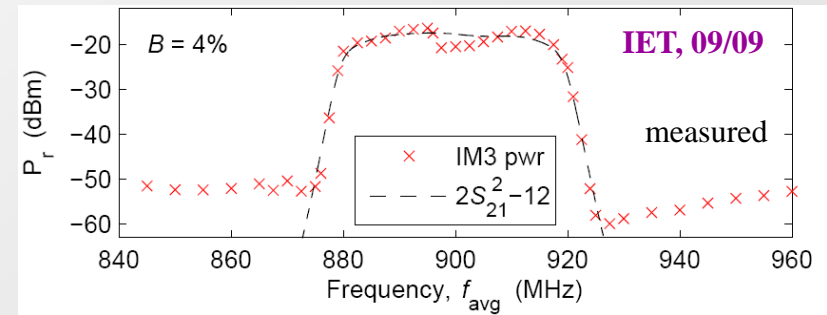
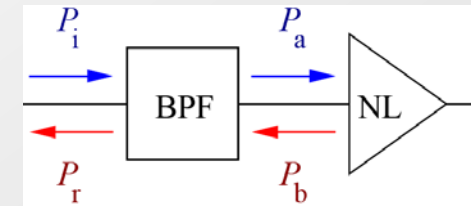


**Simulated fast-switching filter response**

7<sup>th</sup>-order 465-MHz Chebyshev design

(a) input, 1 tone, (b) output, 1 tone, (c) output, 2 tones

- IP3 of an amplifier can be measured using a filter & switched-tone source
- a device's passband can be extracted from 1 port

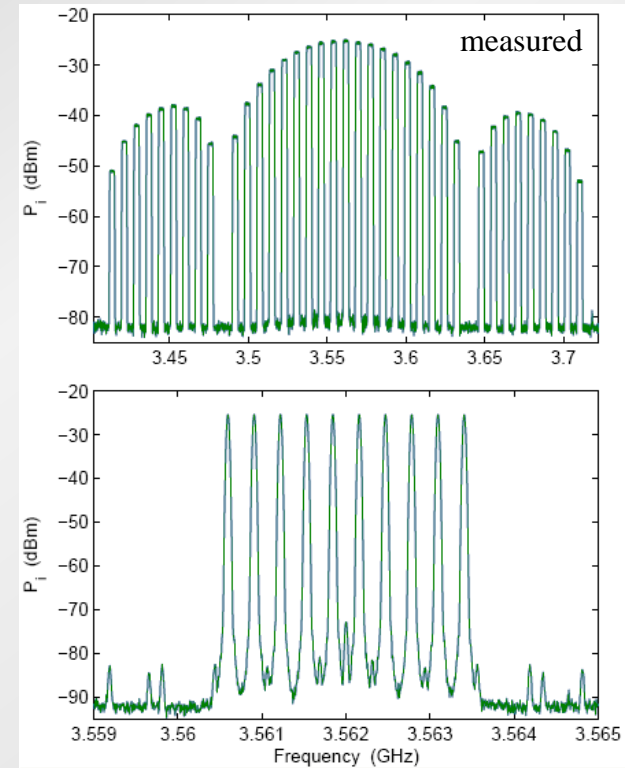
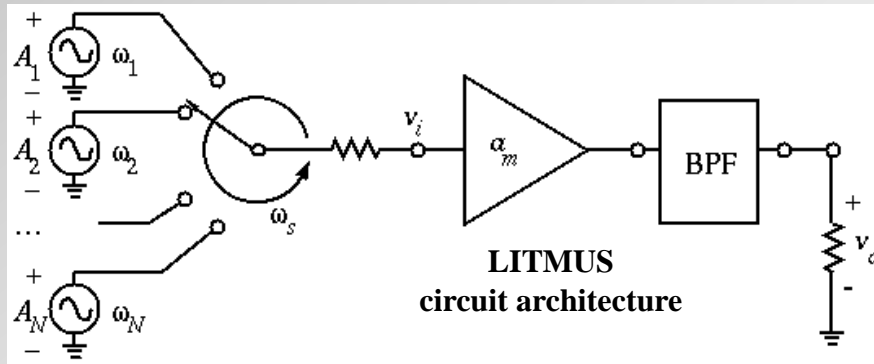


**Passband extraction for bandpass filter**  
7<sup>th</sup>-order 900-MHz Chebyshev design

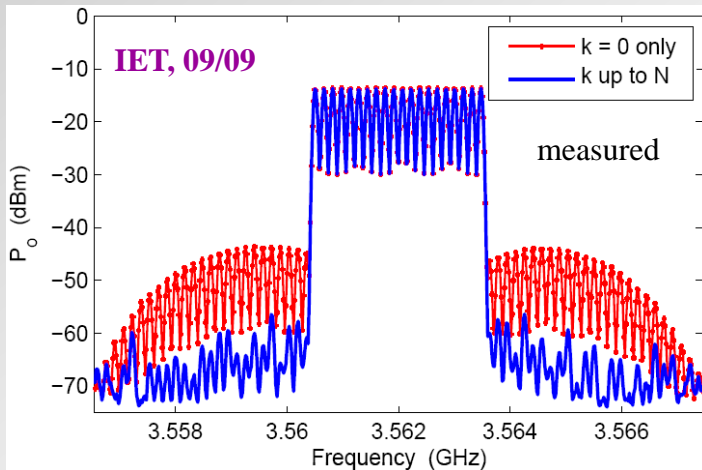
Nearest prior work: **Walker (2005)** – steady-state two-tone testing

# Linear Amplification by Time-Multiplexed Spectrum

- How can we improve linearity by applying time-frequency techniques?



Wideband & narrowband spectra for  $N = 10$  generated by Agilent N6030A + QM3337A modulator



**Distortion reduction for  $N = 20$**   
non-multiplexed (red) vs. multiplexed (blue)  
Ophir 5162 amplifier

- the IMD associated with amplitude modulation can be reduced by trading signal bandwidth for smaller Peak-to-Amplitude Ratio



# Summary: Time-Frequency Effects

Narrowband transients last longer than expected.

co-site interference

- (a) identified resonant cascade as a source of long tails
- (b) developed a differential-equation simplification
- (c) showed frequency-dependence of the tails causes pulse overlap
- (d) evaluated ISI and IMD for frequency-hopping scenarios

Used filter transients to develop new measurement techniques:

- (a)  $Q$ -factor of a single resonator
- (b) bandwidth, without  $S$ -parameters
- (c) broadband  $S$ -parameters from a single time-domain trace
- (d) device passband from a single input port

non-destructive testing

Time-multiplexing & filtering — LITMUS:

reduces IMD associated with amplitude modulation

transmitter  
linearity

# Summary

- High dynamic range measurement system
- Time-Frequency effects produce apparent PIM

# Review of Time-Frequency Effects

## Time-Frequency Effects: Tucker/Eaglesfield (1946)

- commonly-used  
6-element  
bandpass  
filter

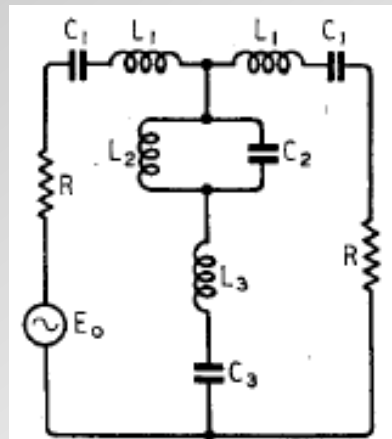


Fig. 3. 6-element symmetrical filter.

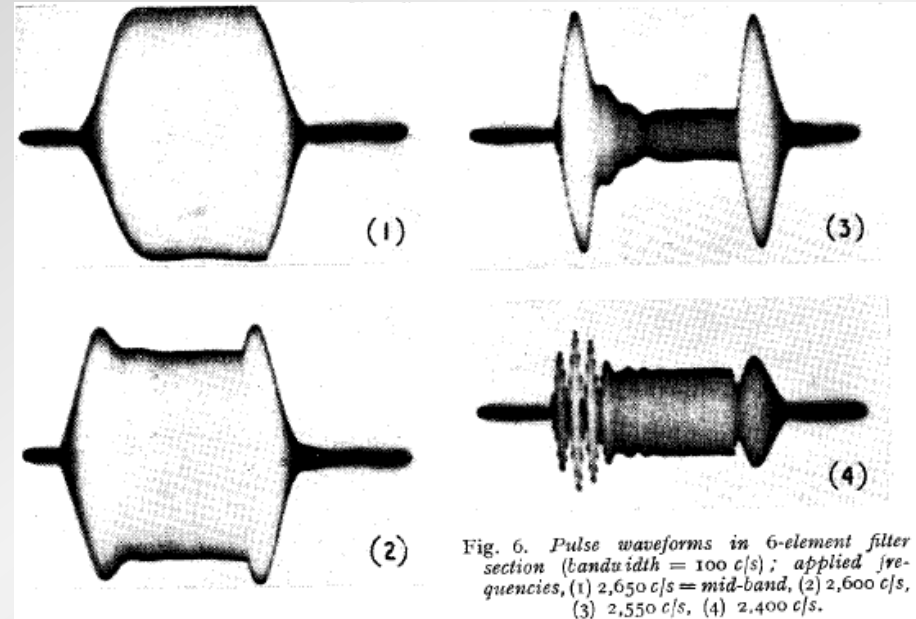


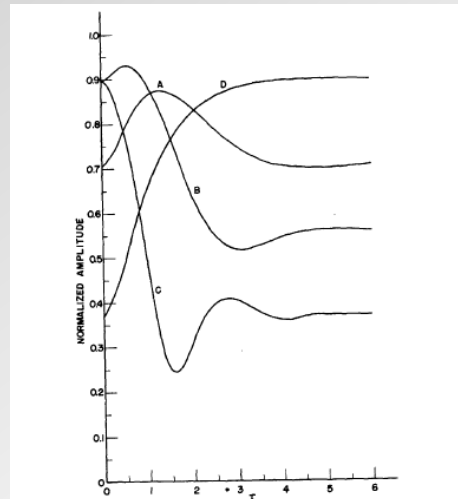
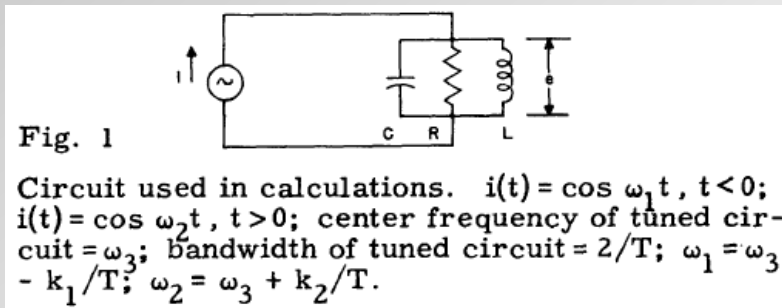
Fig. 6. Pulse waveforms in 6-element filter section (bandwidth = 100 c/s); applied frequencies, (1) 2,650 c/s = mid-band, (2) 2,600 c/s, (3) 2,550 c/s, (4) 2,400 c/s.

Filtered Pulse Responses

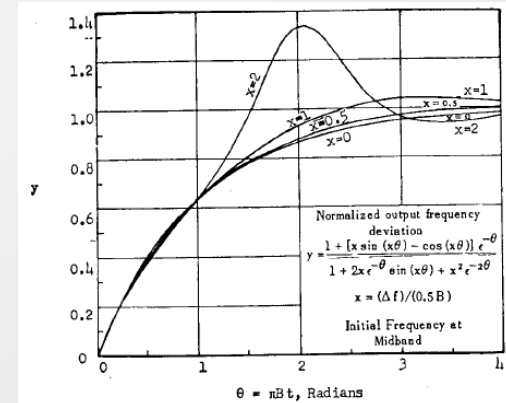
- while analyzing *non-ideal* (transmission-characteristic) filters...
- oscilloscopes can capture filtered pulse envelopes
- differential operators (precursor to Laplace Transforms) can be used to solve for analytical forms for pulse responses

# Time-Frequency Effects: Hatton (1951) & McCoy (1954)

- amplitude transients & frequency transients for a single resonator



**Normalized Amplitude Transients**



**Normalized Frequency Transients**

- while comparing frequency-modulation to amplitude-modulation...
- overshoots in amplitude & frequency are possible for input frequency transitions within a filter's passband

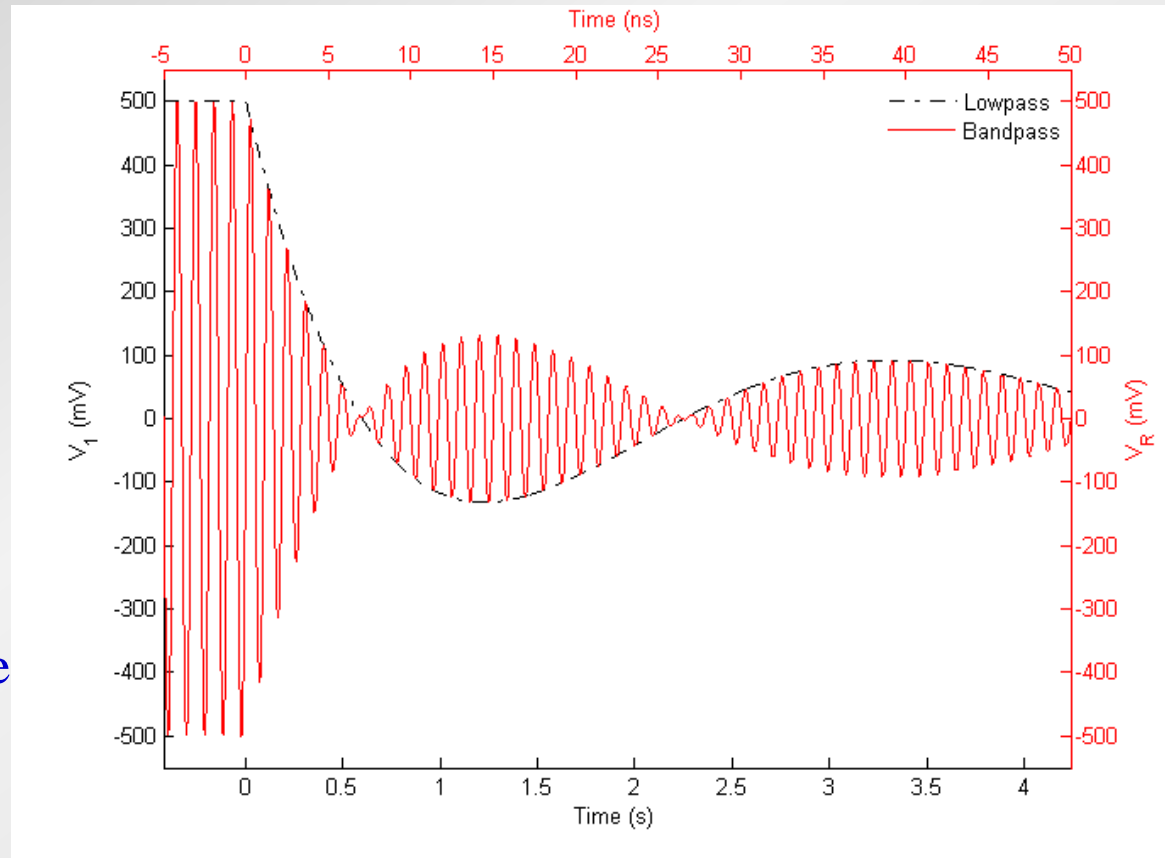
“Simplified FM transient response,” MIT, Cambridge, MA, Tech. Rep. 196, Apr. 1951

“FM transient response of band-pass circuits,” *Proc. IRE*, vol. 42, no. 3, pp. 574-579, Mar. 1954

# Time-Frequency Effects: Blinchikoff (2001)

- Lowpass vs. bandpass transient responses

$$u_b(t) \approx u_l(t_N) \cos(\omega_0 t + \theta)$$



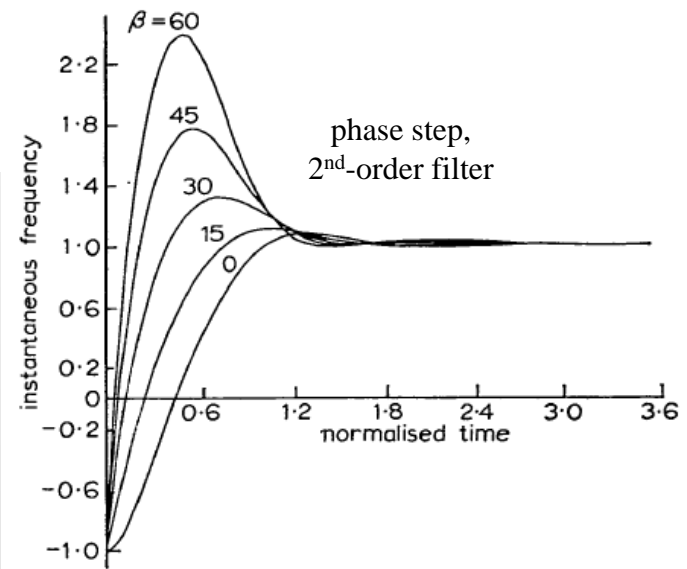
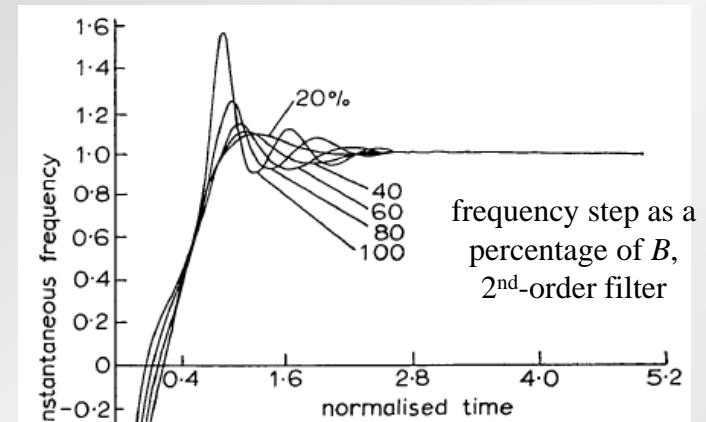
- transient response at midband is a time-scaled version of the lowpass turn-on response

## Time-Frequency Effects: Chohan/Fidler (1973)

- frequency transients, steps of phase/frequency at filter input

- while investigating filtering effects on FSK- and PSK-type signals...
- generalized earlier narrowband Laplace methods for any order & any Q value

“Generalised transient response of bandpass transfer functions to FSK and PSK-type signals,”  
*Electronics Letters*, vol. 9, no. 14,  
 pp. 320-321, July 1973.



## Time-Frequency Effects: Vendik/Samoilova (1997)

- resonators: transmission line & microstrip

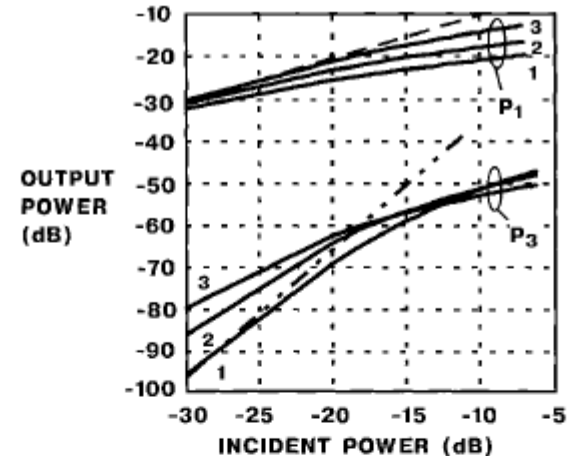
- attributed nonlinearities to
  - crystalline structure
  - charge carrier density
  - Abrikosov vortices

- resistance is a function of current

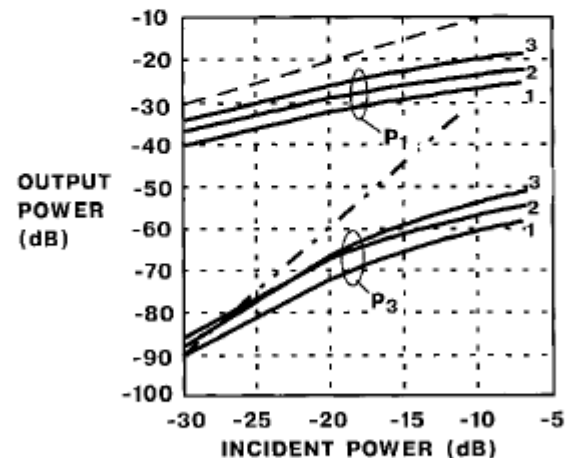
$$R_1(x, t) = R_1 \left[ 1 + \frac{I^2(x, t)}{I_0^2} \right]$$

“Nonlinearity of superconducting transmission line and microstrip resonator”

*IEEE Trans. Microw. Theory Tech.*, vol. 45, no. 2, pp. 173-178, Feb. 1997.



(a)



(b)

Fig. 7. Output power of first ( $P_1$ ) and third ( $P_3$ ) harmonics as functions of incident power  $P_{\text{incid}}$ . The power is normalized to the characteristic power  $P_0$ . (a)  $Q_u=10\,000$ ;  $Q_c$ : 1: 500, 2: 1000, 3: 2000; (b)  $Q_u=1000$ ;  $Q_c$ : 1: 500, 2: 1000, 3: 2000. In the figure, dashed line corresponds to the slope of power 1; dashed-dotted line corresponds to the slope of power 3.



## Time-Frequency Effects: Pereda (1992)

- estimation of quality factor from resonant decay

$$S(n\Delta t) = \sum_{i=1}^p A_i \exp((\alpha_i + j2\pi f_i)n\Delta t)$$

**Prony analysis**

$$\text{for } n = 0, \dots, N - 1, \quad (1)$$

- while investigating resonance in dielectric resonators...
- reduced time to compute resonant frequencies and quality factor using FDTD and Prony analysis

“Computation of resonant frequencies and quality factors of open dielectric resonators by a combination of finite-difference time-domain and prony’s methods,”

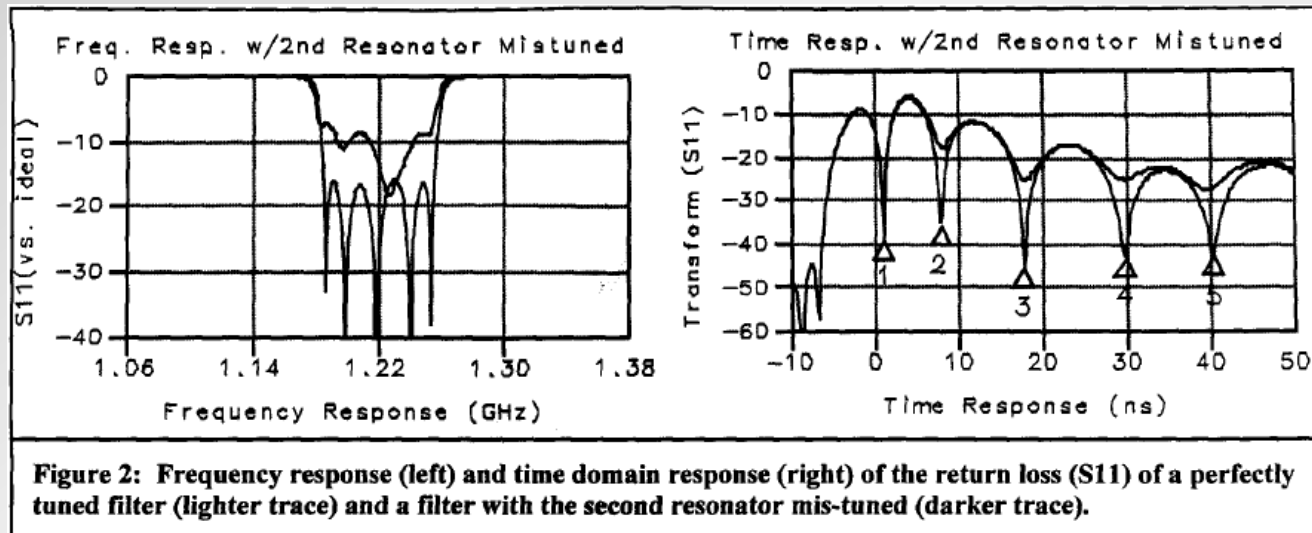
*IEEE Microwave and Guided Wave Letters*, vol. 11, no. 2, pp. 431-433, Nov. 1992.

TABLE I-A  
COMPARISON OF THE RESONANT FREQUENCIES AND  $Q$ -FACTORS OF THE SIX  
LOWEST MODES OF AN ISOLATED DR OBTAINED BY VARIOUS METHODS.  
AXISYMMETRIC MODES

	TE <sub>01</sub>		TM <sub>01</sub>		TE <sub>02</sub>	
	F(GHz)	Q	F(GHz)	Q	F(GHz)	Q
Moment Method [9]	4.829	45.8	7.524	76.8		
Null-Field Method [8]	4.8604	40.819	7.5384	76.921	8.3311	301.02
Measured [10]	4.85	51	7.60	86		
Present Method	4.862	47	7.524	71	8.320	302

## Time-Frequency Effects: Dunsmore (1999)

- Time-domain coupled-resonator filter tuning
  - while working at Hewlett-Packard Microwave Instruments Division...
  - showed how to tune individual resonators using time-domain return loss



“Tuning band pass filters in the time domain,”

*IEEE MTT-S Int. Microw. Symp.*, Anaheim, CA, June 1999, pp. 1351-1354.

## Time-Frequency Effects: Courtney (1999)

- Frequency measurements from time-domain traces

- while trying to determine broadband permittivity and permeability of a sample material...

- found a way to measure  $T$  and  $\Gamma$  by time-domain-reflectometry with nanosecond impulses

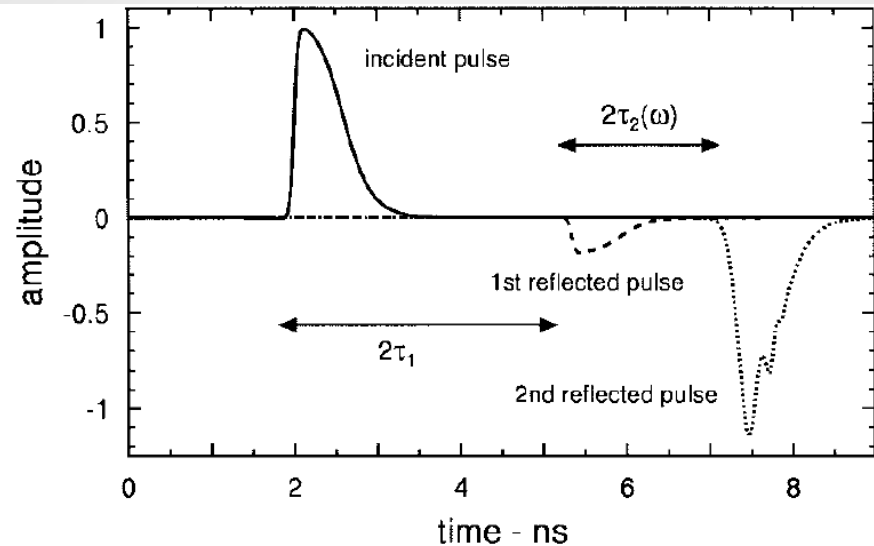


Fig. 3. The simulated incident and computed first and second reflected waveform components.

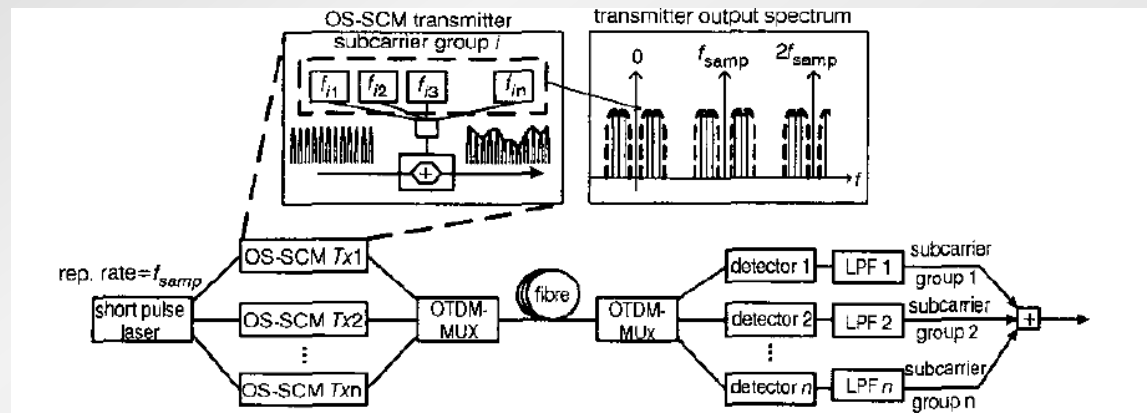
“One-port time-domain measurement of the approximate permittivity and permeability of materials”  
*IEEE Trans. Microw. Theory Tech.*, vol. 47, no. 5, pp. 551-555, May 1999.

# Time-Frequency Effects: Hung et. al. (2002)

- Nonlinear distortion reduction by time-multiplexing

- working with optical cable television transmission...

- found a way to reduce IMD by transmitting subcarrier frequencies in different time slots



**Fig. 1** Nonlinear distortion reduction scheme using OS-SCM and OTDM

Subcarriers are divided into  $M$  groups, each group may contain up to  $N$  subcarriers,  $M > N$ ,  $i \leq M$ ,  $n < N$

“Optical sampled subcarrier multiplexing scheme for nonlinear distortion reduction in lightwave CATV networks,” *Electronics Letters*, vol. 38, no. 25, pp. 1702-1704, Dec. 2002.