



Practical Papers, Articles and Application Notes

Kye Yak See, *Technical Editor*

I hope you enjoyed reading the three papers published in the Spring 2011 issue in this section of the EMC Newsletter. For this current issue, I am delighted to present to you an additional three quality contributions covering a wide range of EMC-related subjects: electrostatic discharge (ESD), the concept of electrical dimension, and a causality issue in electromagnetic simulation.

The first paper, “Easy Access to Pulsed Hertzian Dipole Fields Through Pole-Zero Treatment,” was contributed by Timothy J. Maloney from Intel Corporation. Tim’s rich experiences in ESD protection design for semiconductor devices have led to breakthroughs in ESD performance enhancements for a wide variety of Intel products. In this paper, based on a Laplace Transform approach, he cleverly derives the s-domain radiated field equations for a pulsed current source. The result is a pole-zero expression similar to that of the ordinary circuit analysis, where time-dependent fields at any distance can be calculated through easily accessible inverse Laplace Transform software. The time-domain radiated fields are useful for one to assess how the charged device model’s ESD radiations can be detected.

The second paper entitled “Physical Dimensions versus Electrical Dimensions” is authored by our regular contributor, Professor Clayton Paul. With digital circuits operating at higher speeds and shorter logic transition times, digital circuit designers are confused about the condition in which to apply a lumped circuit or transmission line model for their circuit analyses. They will find the answer in this pa-

per. Dr. Paul shares with us how to determine the condition where the interconnect lines connecting the source and the load become electrically long. Hence, the standard lumped-circuit model is no longer valid and the transmission line model is necessary.

The last paper entitled, “A Simple Causality Checker and Its Use in Verifying, Enhancing, and Depopulating Tabulated Data from Electromagnetic Simulation,” is jointly authored by Brian Young and Amarjit S Bhandal from Texas Instruments USA and UK, respectively. With more powerful and accurate EM simulators available in the market, they become valuable tools for analyzing complex EMC problems. How do you know that the simulated results are correct, reliable, and usable? Causality check is one effective way to ensure that the simulated results are accurate and valid. Brian and Amarjit share with us the implementation details of a simple causality checker. The causality checker is used to derive an algorithm for selecting sampling rates and bandwidth for EM extractions of good interconnects, enabling a potentially large reduction in data points and run time. The improved extraction data has been shown to significantly improve S-parameter data and time domain simulation accuracy.

In conclusion, your active participation as authors and reviewers is needed so as to make this column a quality read. I wish you an enjoyable and fulfilling summer and feel free to share with me your feedback and comments, preferably by email at ekysee@ntu.edu.sg.

Easy Access to Pulsed Hertzian Dipole Fields Through Pole-Zero Treatment

Timothy J. Maloney, Intel Corporation, Santa Clara, CA; timothy.j.maloney@intel.com

Abstract: The equations for EM dipole near and far radiation fields are formulated for the complex frequency domain with a Laplace Transform analysis for Hertzian dipoles. An s-domain pulsed current source function from ordinary circuit analysis is used in the expressions, and is augmented as needed to refine the pulse. This formulation allows a lucid pole-zero treatment of the field transfer function, yielding any field at any distance through the inverse Laplace Transform. Zeros of these expressions always include the “radiation zeros”, essential properties of the dipole fields themselves. Methods for recovery of current pulse waveforms from E- and H-field measurements, using filter functions, are described. The inverse Laplace Transform of

pole-zero expressions through Heaviside expansion is more accessible than ever through free web applets and commonly available software. Study of the small pulsed dipole has become important in semiconductor manufacturing, as engineers seek to monitor and control charged device model ESD events that could destroy components.

Introduction

Dipole radiation is treated in many physics and engineering textbooks on electromagnetism (EM), only a few of which are cited here [1–3]. The most familiar treatment results in

expressions for the near and far fields is for the harmonic (sinusoidal) source, but that is often generalized to the time-dependent dipole moment source, usually called $p(t)$ for the electric dipole and $m(t)$ for the magnetic dipole. The generalized time-dependent Hertzian (i.e., infinitesimal) dipole in free space will be useful for exploring pulsed fields. The complementary features of electric and magnetic dipole radiation and their E and H fields are well treated in EM textbooks, so we first will center the discussion on electric dipoles. Once the impact of the electric dipole moment $p(t)$ and its time derivative on the fields is better understood, it will be clear how to apply these methods to magnetic dipole radiation in the same way.

There are numerous motives for studying pulsed dipole radiation in free space, not least of which is an existing vast literature on antennas for pulsed applications. Many contemporary works still refer to a landmark study from Caltech in 1974 called simply "Pulsed Antennas" [4], with 69 references and several lucid examples, beginning with the point source or Hertzian dipole. More recently, Schantz [5] studied the flow of electromagnetic power for pulsed Hertzian dipoles in the context of antenna design, and observed some interesting near and far field phenomena that relate to the present work, which will be discussed later. Atmospheric scientists who observe and often induce lightning strokes [6] have also produced a vast literature on pulsed fields; the present author hopes that this one reference could help lead the interested reader to more publications. While lightning is not an "infinitesimal" source except at very far fields, researchers often start with the Hertzian dipole concept and may view lightning as a stack of such dipoles.

Another motivation to study pulsed dipole fields is closer to the present author's interests, which include charged device model (CDM) electrostatic discharge (ESD) threats to semiconductor components. These phenomena have been known since the 1970s, and standardized tests have been formulated [7] to simulate the phenomena based on some well-designed equipment from the 1980s [8]. Radiation detection is not part of these semiconductor test activities, but it has been used to detect CDM events in the factory as part of a static control program [9]. More recently, semiconductor workers have looked more closely at the relation between CDM-like events and signals from a nearby EMI-type antenna [10, 11]. Thus we have become highly interested in the fields produced by CDM pulses, including the strong near fields that a factory monitor antenna could pick up. The CDM test machine [7, 8] provides easy access to the current pulse information, so we would like to turn this into full, time-dependent near and far field information as easily as possible, using a Hertzian dipole approximation.

Figure 1 illustrates a familiar 3-axis scheme for electric dipole radiation, showing the dipole (of presumed height dl) at the origin, and the names for Cartesian (x, y, z) , spherical (r, θ, ϕ) , and cylindrical (ρ, ϕ, z) coordinates that may be used.

Transforming Dipole Field Equations

If we pick and choose among textbook treatments of electric dipole time-dependent fields [1–3], we can formulate an expression in "practical" units for the most interesting field for electric dipole radiation, in terms of dipole moment $p(t)$ and its first two time derivatives, the latter shown as p -dot and p -double-dot:

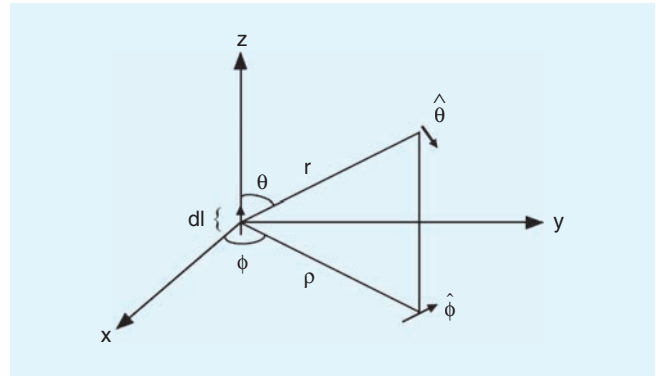


Fig. 1. Coordinates for dipole radiation fields.

$$E_{\theta}(t) = \frac{\sin \theta}{4\pi\epsilon_0} \left(\frac{[\ddot{p}]}{c^2 r} + \frac{[\dot{p}]}{cr^2} + \frac{[p]}{r^3} \right). \quad (1)$$

c is, of course, the speed of light and ϵ_0 the permittivity of free space. At all times the fields are understood to be delayed by the propagation time, so we will not be writing $(t-r/c)$. There is also a radial E field and an azimuthal H field, but they do not contain all three terms in $p(t)$, commonly called the static (p), inductive (p -dot) and far field radiative (p -double-dot) terms. We will treat these fields later. It is now clear that the pulsed field E_{θ} is a maximum at the "equator" ($\sin \theta = 1$, where E_{θ} and E_z are the same magnitude) and that full knowledge of the current $I(t)$ plus the dipole moment length dl is sufficient to find $p(t)$ and its derivatives, as $p(t) = Q(t) \cdot dl$, and $I(t) = dQ(t)/dt$.

How do we gain the promised "easy access" to these pulsed fields at all distances? Equation (1), in the context of current pulses beginning at time zero, is a perfect target for use of Laplace Transforms [12], familiar to practitioners of electrical circuit theory [13]. The use of Laplace Transforms (when named as such; we will avoid a digression on the near-equivalence of Fourier Transforms) for pulsed EM field problems seems to fall in and out of favor over the years. For example, in 1958 the well-respected physicist Paul I. Richards [14] used a Laplace Transform method and some very insightful coordinate transformations to look at pulsed EM waves in a conductive medium, seawater [15], without significant use of a computer. Despite such studies over the years showing the usefulness of Laplace Transforms in pulsed EM field problems, the present author has not been able to locate a simple Laplace Transform treatment of the pulsed Hertzian dipole in a popular EM textbook. But the Laplace Transform approach to pulsed (or even continuous wave) Hertzian dipole fields offers considerable insight into the phenomena and easy access to the fields for the engineer short on time and resources, so let us begin.

Equation (1) is transformed into to the Laplace (complex frequency; $s = \sigma + j\omega$) domain by recalling [12] that the time derivative d/dt operator is s , and the integration operator is $1/s$. This means that $p(t)$ as above transforms to $I(s)/s$ in the Laplace domain, and the time derivatives in (1) become s and s^2 . The propagation time to radius r is $\tau = r/c$ so it can be a "constant" at a particular radius for the sake of an s -domain field equation. Eq. 1 can thus be expressed, very unusually, with $1/r^3$ factored out, and transformed into the s -domain as

$$E_{\theta}(s) = \frac{I(s)\sin \theta}{4\pi\epsilon_0 s r^3} dl \cdot (1 + s\tau + s^2\tau^2), \quad \tau = \frac{r}{c}. \quad (2)$$

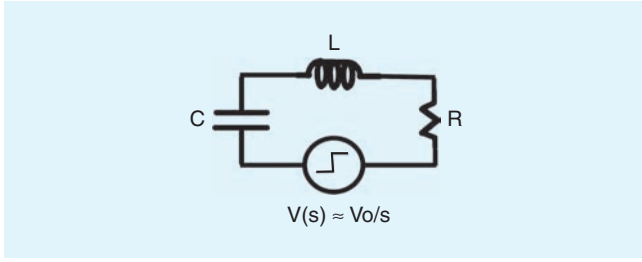


Fig. 2. Simple RLC model of a pulse source caused by a collapsing dipole, current beginning and ending at zero.

The radius becomes a scaling factor and it now simply remains to use circuit theory to express $I(s)$ for the pulse source. That is not difficult; in the simplest approximation of the CDM source, it is a two-pole series RLC circuit responding to a step (collapsing dipole of a charged device touching ground through one pin) as in Figure 2. Numerous works on CDM begin with this kind of circuit [16].

In a collapsing dipole, the capacitor begins with charge and ends with no charge (step-down), which in linear circuit theory is equivalent to a step-up. The current expression emerges from the admittance $Y(s) = 1/Z(s)$ of the series RLC loop and, through standard methods, is found to be

$$I(s) = V(s)Y(s) = \frac{V_0}{s} \cdot \frac{Cs}{LCs^2 + RCs + 1} = \frac{CV_0}{LCs^2 + RCs + 1}. \quad (3)$$

This is our two-pole RLC pulse source that, depending on circuit model values, may or may not include ringing. It is now clear that $E_\theta(s)$ becomes a **pole-zero expression** and that a time domain solution $E_\theta(t)$ is available through the **Heaviside expansion method** of obtaining an inverse Laplace Transform in terms of a series of exponentials [12].

$$E_\theta(s) = \frac{CV_0 \cdot dl}{4\pi\epsilon_0 r^3} \cdot \frac{(1 + s\tau + s^2\tau^2)}{s(1 + RCs + LCs^2)} \sin \theta. \quad (4)$$

There are several things to notice about Eq. (4). The s factor in the denominator means the field is some kind of step function, which makes sense given that the step in voltage and charging or discharging of the capacitor means that a static field either appears or disappears. However, if the step is differentiated (finite width pulse for voltage) and the polarization begins and ends at zero, the s disappears from the denominator and the field also begins and ends with zero. This resembles the case of the Gaussian polarization pulse for a Hertzian dipole in [4], only now there is a defined $t = 0$ and the ability to construct a slightly underdamped pseudo-Gaussian pulse [17] to represent how a real Gaussian-like Hertzian dipole would behave, without requiring infinite time. There is also the freedom to add some high-frequency poles to $I(s)$ to produce a gradual rise of the pulse and make it even more like a Gaussian. In retrospect, there may have been too much reliance on Gaussian pulse examples in the antenna literature over the years, while this pole-zero alternative was not recognized.

The numerator of Eq. (4) contains the essentials of the dipole radiation field in the compact expression $1 + s\tau + s^2\tau^2$, also an unchanging feature of (2) and (4). For a given radius r such that

$\tau = r/c$, this expression gives the complex frequency zeros of the E_θ field (let's call them **radiation zeros** or **field zeros**) as

$$z_{1,2} = \frac{-1 \pm j\sqrt{3}}{2\tau}. \quad (5)$$

These, along with the poles (roots of the denominator of (4)) play a role in the Heaviside inversion to the time domain [12], and have the general effect of sharpening the field compared to the current, as will be seen below. But the student of circuit theory looks at (4) and is immediately likely to ask about the curious case of pole-zero cancellation, where in this case, we would have $RC = \sqrt{LC} = \tau = r/c$, possibly true at a particular radius r . This leaves only the s term in the denominator, meaning that for a collapsing dipole there is a sharp drop in the static field at that radius, nothing more. Is this a paradox?

It turns out that this unusual case of dipole field collapse was lucidly described by Schantz [5], although not called pole-zero cancellation. Figure 3 is from [5], showing energy density and flow and a stationary sphere at the expected radius. No energy crosses the radius where there is pole-zero cancellation.

Figure 4 shows the sort of $I(t)$ pulse that results in pole-zero cancellation as described above for Eq. (4). This one was done for $\tau = 500$ psec because it is closer to a CDM pulse that will interest us. All such pulses for E_θ look the same; only the time scale changes. The damping factor ($D = RC/2\sqrt{LC}$) is 0.5, underdamped as is the case when the two poles are complex conjugates. In this case, the dark sphere as in Fig. 3 would occur at 15 cm or about 6 inches.

In discussion of the material in Fig. 3, above, Schantz notes that since no energy crosses the dark sphere, the stored energy outside it must escape to infinity (i.e., be radiated), and the energy inside it must of necessity collapse back into the dipole as the pulse finishes, as it cannot escape. Such a boundary is thus unusually definitive because of pole-zero cancellation. Meanwhile, we suspect Schantz is correct about no energy crossing the sphere boundary at any time, but the Laplace Transform method gives us good tools to confirm this rigorously, particularly for $t = 0^+$. To do so we must know the H field, and then confirm there is no impulse (delta function) at $t = 0$.

For the electric dipole, the H field is entirely azimuthal, orthogonal to E_θ and thus produces inward or outward flow of energy through the Poynting vector. The H expression to go with Eq. (1) has no static field component and is as follows [1–3]:

$$H_\phi(t) = \frac{c \sin \theta}{4\pi} \left(\frac{[\dot{p}]}{c^2 r} + \frac{[\ddot{p}]}{cr^2} \right). \quad (6)$$

Using the same methods as above, the s -domain expression is

$$H_\phi(s) = \frac{cI(s) \cdot dl}{4\pi sr^3} \cdot s\tau(1 + s\tau) \sin \theta = \frac{I(s) \cdot dl \cdot (1 + s\tau)}{4\pi r^2} \sin \theta. \quad (7)$$

Note the cancellation of s -terms, now that there is no static field, and of an r since $c\tau = r$. $H_\phi(t)$ can thus be seen as a mixture of $I(s)$ and its derivative. The two-pole $I(s)$ of Eq. (3) starts at 0 and has a finite derivative (as in Fig. 4), so clearly $H_\phi(t)$ is finite at $t = 0$ (i.e., no impulse due to differentiating a perfect step), so we agree that, for pole-zero cancellation, there is no energy flow through the dark sphere even at $t = 0$. The radiation zero for H_ϕ is real and negative, at $-1/\tau$, but there

was also a zero at zero, cancelling the s of electric polarization $I(s)/s$. The complementary E_ϕ expression for the magnetic dipole also has a zero at zero, but recall that the magnetic dipole moment $m(t)$ goes as $I(s)$ times an area.

For completeness, we should record the last electric dipole field component, radial E-field. This component goes as $\cos \theta$ (peaks at polar regions) and has only static and inductive components, no $1/r$ fields radiated to infinity:

$$E_r(t) = \frac{\cos \theta}{2\pi\epsilon_0} \left(\frac{[\dot{p}]}{cr^2} + \frac{[p]}{r^3} \right). \quad (8)$$

The cross product of E_r with H is necessarily in the θ direction, so it does not produce radial energy flow. The s -domain expression for E_r is

$$E_r(s) = \frac{I(s) \cdot dl}{2\pi\epsilon_0 r^3} \cdot \frac{(1 + s\tau)\cos \theta}{s}. \quad (9)$$

Due to the static field, the s is back in the denominator. E_r has the same radiation zero as H_ϕ , at $-1/\tau$. The radiation zeros are shown in the complex plane in Figure 5. Students of circuit analysis will recognize that the field equations have been turned into transfer functions, and that a pole-zero plot expresses all the amplitude and phase information at once. The radiation zeros as in Fig. 5 are always the starting point, and the field problem is essentially solved once the current-related poles join the plot.

Before we leave Fig. 5 and do some pole-zero expansions to calculate time-dependent fields, it is useful to view Fig. 5 in the context of the “radiansphere” as described by Harold Wheeler in 1959 [18]. Wheeler was also concerned with small dipoles but with continuous wave (cw) harmonic signals ($s = j\omega$), and marked the boundary between near and far fields as the sphere with a radius of one radian of wavelength, i.e., $\omega\tau = 1$. Fig. 5 is thus seen as the case where poles $\pm j\omega$ would be plotted at $\pm j$ for the radiansphere boundary. At closer distances, the zeros are further out (they start at infinity at the dipole source) and have much stronger influence, but then they cross the unit circle at the radiansphere, as described, and continue on at larger distances toward the origin in a straight line, as the far field comes to dominate. Wheeler also recognized (what we call) $1 + s\tau + s^2\tau^2$ in the context of a transfer impedance between dipoles at a distance defined by our $\tau = r/c$, and in terms of an RLC network with values based on EM properties of free space. If Wheeler had been more interested in complex frequencies and pulsed dipoles, the analysis could have been extended to a pole-zero treatment as we have here, and the history might be different.

Time-Domain Dipole Fields

As noted previously, inversion of the above s -domain equations into the time domain involves Heaviside expansion of a ratio of polynomials, as described in [12] and in a host of college-level calculus texts. Essentially, if $f(s) = p(s)/q(s)$, $q(s) = (s - a_1)(s - a_2) \cdots (s - a_m)$, $p(s)$ a polynomial of degree $< m$,

$$F(t) = \sum_{n=1}^m \frac{p(a_n)}{q'(a_n)} e^{a_n t}. \quad (10)$$

A simple example with no zeros would be two complex conjugate poles following Eq. (5) for $\tau = 500$ psec and a normalized (integrating to 1) version of the current (3) as plotted in Fig. 4, or

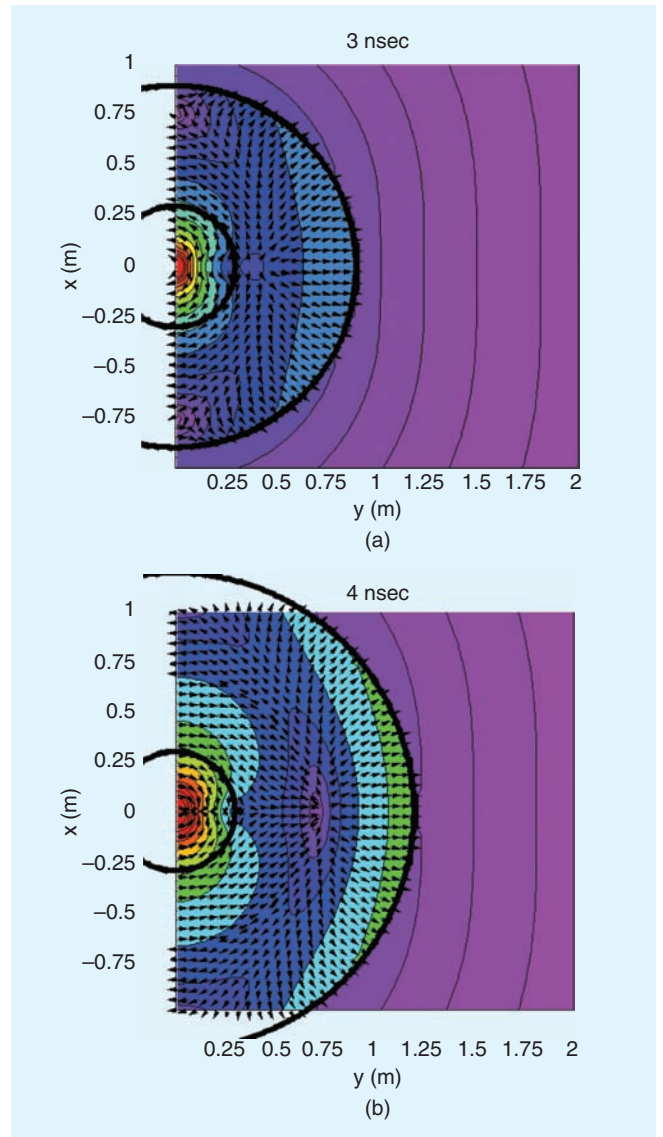


Fig. 3. from Schantz [5], © 2001, IEEE. Energy density and flow at $t = 3$ nsec (Fig. 3a) and $t = 4$ nsec (Fig. 3b) for a damped harmonic with poles matching the zeros in Eq. (5) and $t = 1$ nsec or 30 cm. Note the stationary sphere at 30 cm, regardless of time.

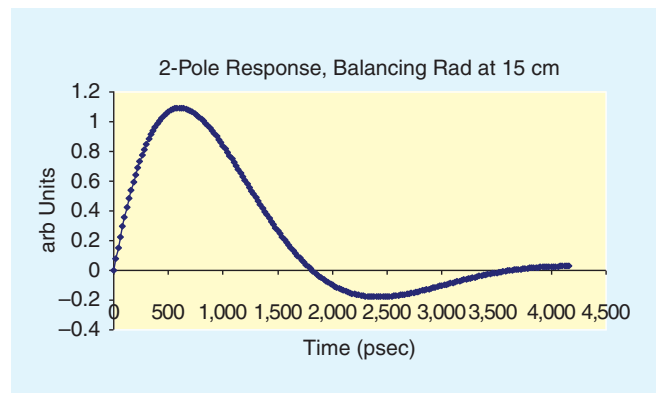


Fig. 4. 2-pole pulse source that would cancel radiation zeros at 15 cm.

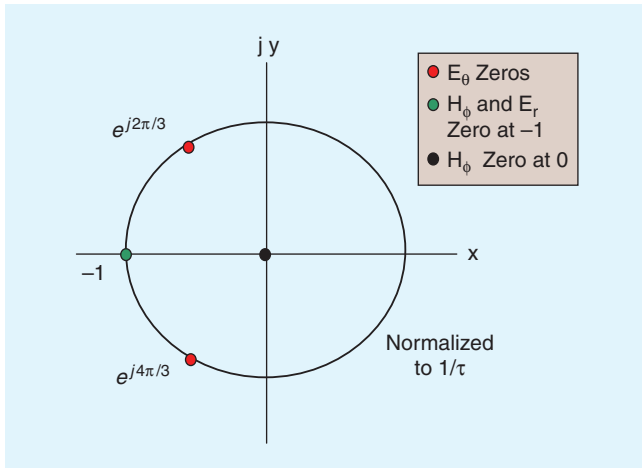


Fig. 5. Complex plane plot of the radiation zeros for all field components of electric dipole.

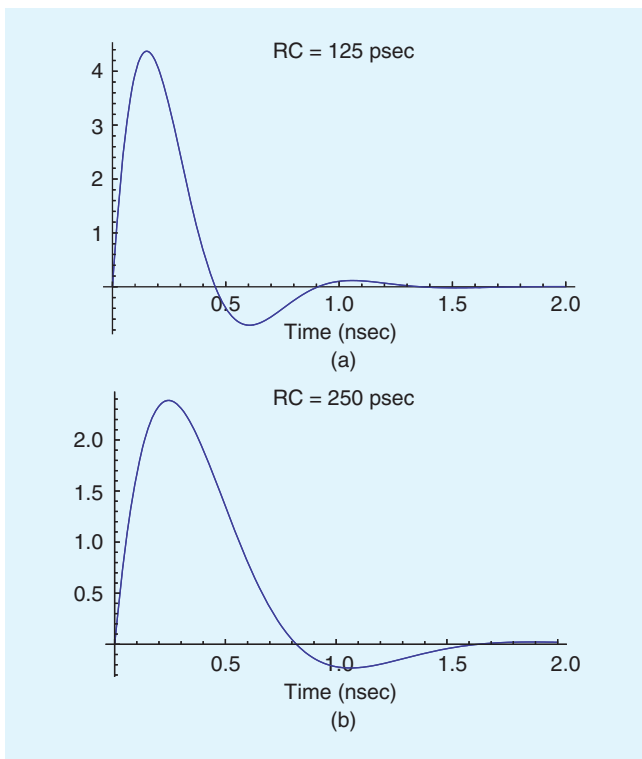


Fig. 6. Normalized current profiles of two possible CDM events, one for 5 pF package capacitance (Fig. 6a) and the other for 10 pF (Fig. 6b). Spark resistance is 25 ohms; package inductance scaled with the square root of package area.

$$I(s) = \frac{1}{1 + 0.5s + 0.25s^2} \Rightarrow I(t) = \frac{4}{\sqrt{3}} e^{-t} \sin(\sqrt{3}t). \quad (11)$$

Here the time is in nanoseconds and s in GHz. Note that for “ordinary” passive circuit elements describing the pulse source as in Eq. (3), the polynomial coefficients of $q(s)$ will be positive and real, thus giving poles that are negative and real, or complex conjugates with negative real parts. In [5], Schantz solved for the polarization of a collapsing dipole (our $I(s)$ s or integrated current) and its derivatives for the case of a current source producing stationary dark sphere at 30 cm ($\tau = 1$ nsec),

as described above, and found the expected participation of $\sqrt{3}$ in the natural frequencies and precisely the same current waveform as Fig. 4, aside from the time scale set by τ . The appearance of the dark sphere as discussed above is, again, explained by pole-zero cancellation at a critical radius. Now let us try some field calculations.

Inverting Laplace Transforms through Heaviside expansion can be done with one- or two-line commands on a computer. Many software packages do this (the present author uses Mathematica) but this paper has promised “easy access” to field solutions for the reader, and that should mean free software with a very short learning curve. There is indeed a free Java applet for the inverse Laplace Transform, available on the Internet [19]. The user need only type in numerator and denominator polynomials in s (our $p(s)$ and $q(s)$) and push a button, which certainly amounts to a lower barrier to this kind of computational assistance than was the case in years past. It is why the author thinks that these highly accessible tools are what students and working engineers need to acquire a feel for pulsed and cw dipole radiation in any environment, and without wanting to gloss over the dreaded near field effects when $r \leq \lambda/2\pi$.

Let us look at a few current and E-field profiles of CDM-like events with realistic parameters. Spark resistance for CDM is around 25 ohms [16] and there is usually some mild undershoot after the main pulse so that $D = 0.5-0.7$ is appropriate. External capacitance to ground for ICs could be 5 pF for a fairly small to mid-size package and 10 pF for a larger one. Package inductance varies, but it should scale with trace length (roughly square root of area) while capacitance should scale with area. Thus D should increase by $2^{1/4}$ for the larger package (D goes from 0.5 to 0.595), so the normalized (integrates to unity) current expressions become (s in GHz, coefficients in nanoseconds)

$$I(5pF) = \frac{1}{1 + 0.125s + 0.15625s^2}, \text{ and}$$

$$I(10pF) = \frac{1}{1 + 0.25s + 0.044s^2}. \quad (12)$$

These would be current profiles for equal amounts of charge, although in the factory, one may expect CDM-induced charge quantities to scale with area. This is what Gauss’ Law gives for a fixed electric field, or for area-scaled accumulation of triboelectric charge by a package. These two normalized CDM current profiles are plotted in Figure 6.

The normalized (reaching a final value of unity, the static field) equatorial E-field E_z at 15 cm ($\tau = 500$ psec) for these cases is taken from Eq. (4),

$$E_z(s) = \frac{1 + s\tau + s^2\tau^2}{s(1 + RCs + LCs^2)}, \quad (13)$$

where RC and LC are the values in Eq. (12). These are plotted in Figure 7.

Notice that while the current scales by the expected factor of two for the two cases, the maximum field scales by about $3x$; also there is sharpening, and there is an unrealistic sudden step at $t = 0$, owing to the finite second derivative at $t = 0$ for a two-pole pulse. But the CDM spark itself is expected to have a rise time of at least 60 psec, so it is easy to insert a double 30 psec real pole pair into Eq. (13), for a more realistic field expression:

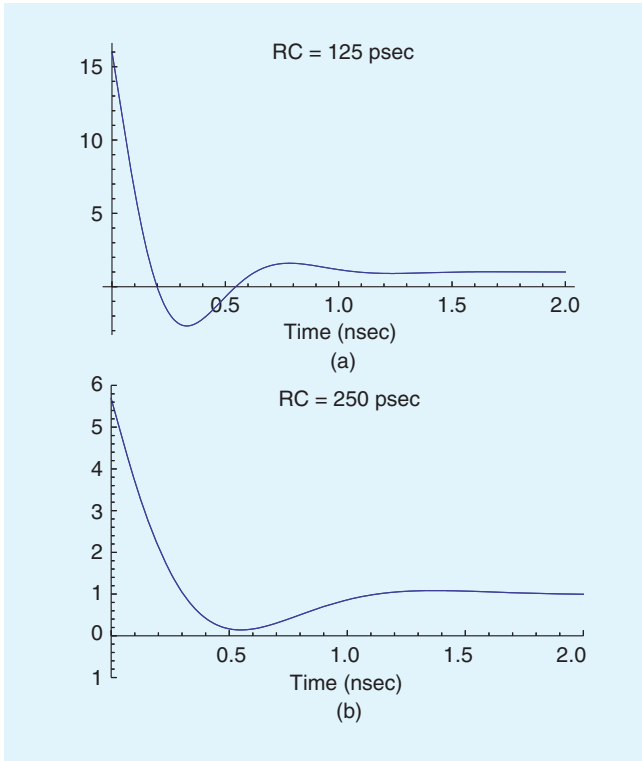


Fig. 7. Normalized vertical E-fields for the current profiles in Fig. 6.

$$E_z(s) = \frac{1 + s\tau + s^2\tau^2}{s(1 + 0.03s)^2(1 + RCs + LCs^2)}. \quad (14)$$

These easily calculated CDM E-fields are shown in Figure 8.

As noted earlier, the charge-up case is equivalent to charge-down, so CDM pulse fields would ordinarily be shifted down (by -1 for these normalized pulses) to show zero field at steady state.

In the more realistic case of Fig. 8, the E-field amplitude swing is still about $3x$ more for the faster device, which has $2x$ the peak current and equal charge compared to the other. Because of the derivatives (in the radiation polynomials of Eqs. 13–14), fields are definitely sharper and of shorter time duration than the current of Fig. 6, even after the spark rise time is added; the spark rise time affects the startup phase of the pulses. At 15 cm, the slower 250 psec = RC pulse in Fig. 8b is clearly more in the near field zone because of its lower frequency content, meaning that the final static field $E_z = 1$ is fairly large compared to transient fields.

Before we look at field measurement, let us calculate a transient magnetic field. Going back to the collapsing dipole example of Schantz [5] at the dark sphere at 30 cm, we decided that \mathbf{ExH} integrated over time has to be zero at that radius, although there is a finite magnetic field as the electric field steps down suddenly. Now employing the radiation zeros for H_ϕ , the normalized equatorial field, following Eq. (7) and with GHz units for s and nanoseconds for τ , is

$$H_\phi(s) = \frac{I(s)}{s} \cdot s(1 + s\tau) = \frac{1 + s\tau}{1 + s\tau + s^2\tau^2} = \frac{1 + s}{1 + s + s^2},$$

for $\tau = 1$ nsec. (15)

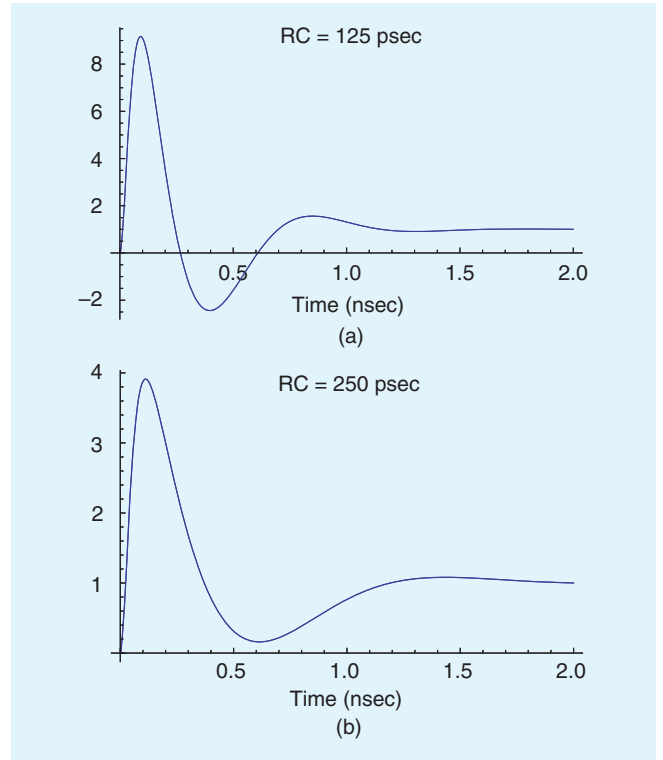


Fig. 8. Normalized vertical E-fields as described by Eq. (14), with extra double pole for 60 psec spark rise time. Peak-peak amplitude is almost $3x$ greater for the smaller, faster device in Fig. 8a.

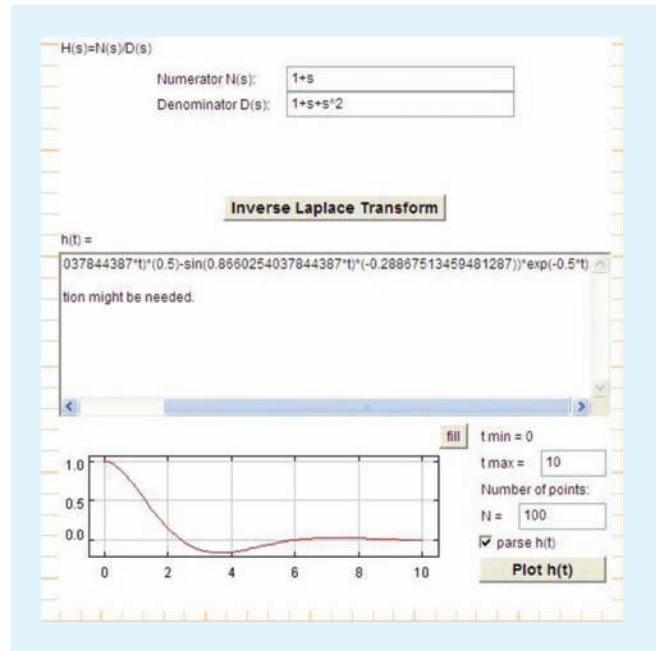


Fig. 9. Inversion of Eq. (15) to give $H_\phi(t)$, using web applet [19]. Time scale in nanoseconds; expression is normalized to give integral of unity.

$H_\phi(\tau)$ is plotted in Figure 9, calculated from the inverse Laplace Transform web Java applet [19].

Because of the finite second derivative of $I(t)$ in the two-pole form, the H_ϕ field has a pure step at $t = 0$. But because the finite \mathbf{ExH} lasts for zero time, no energy is transmitted across the dark

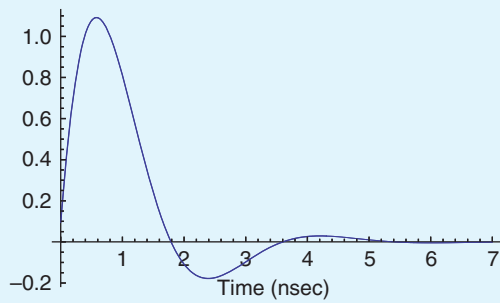


Fig. 10. Normalized filter function impulse response, as in Eq. (17), for a small E-probe. $Z_0C_m = 25.2$ psec, $L_mC_m = 541.6$ (psec)², $r = 15$ cm. For these values, there is also a very small Dirac delta function (0.002) at the origin that brings the integral to unity. This function would be convolved (e.g., with free tools as in (24)) with the measured field signal $V_m(t)$ to produce an image of the time-dependent source current $I(t)$.

sphere. However, the E-field at all radii also has a $t = 0$ step as in Fig. 7, which led us to the spark rise time poles of Eq. (14) and the more realistic fields of Fig. 8. Such rise time poles would remove the pure steps from E and H fields at the dark sphere and introduce a small but finite ExH energy flow during the spark rise time.

Field Measurement and the Goal of Current Imaging

We will now briefly discuss transient field detection, and how it applies to the foregoing calculations and some related practi-

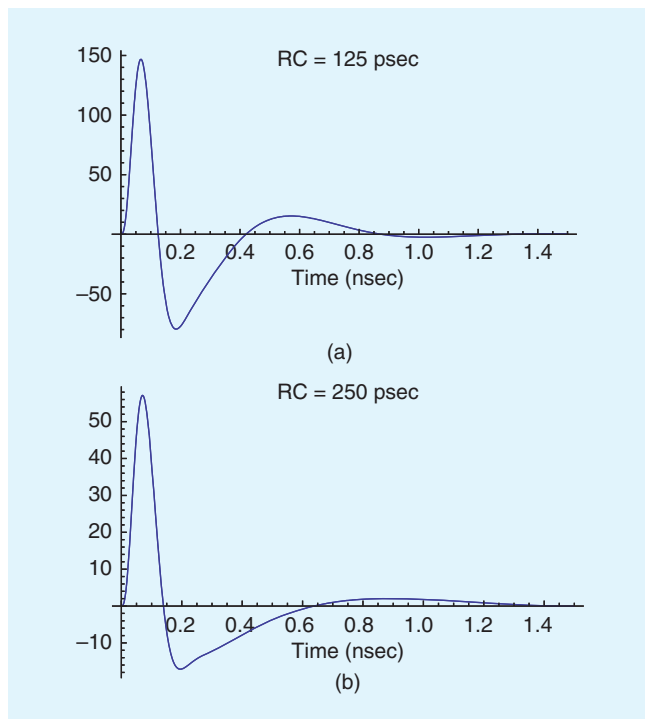


Fig. 11. Normalized E-field signals, predicted for measurement at 15 cm using the E-probe transfer function in Eq. (16) as described for Fig. 10. For equal charge, the smaller device (5 pF, Fig. 10a) has about 3x the peak-peak voltage swing (V_p - p) of the larger (10 pF) device.

cal situations for EMC and ESD engineers. E and H field detection is of course a vast subject, so we will cover only a few high points here, and defer a more complete discussion of transient field measurements to a future article.

No discussion of ESD-created transient fields as created by Hertzian dipoles would be complete without citing Wilson and Ma [20], a work now over 20 years old. Using a broadband horn antenna for E-fields, and an ESD pulser gun resembling one that would now be compliant with IEC 61000-4-2, the authors measured and compared pulse currents and radiated fields. Field results seemed most successful for measurements at 150 cm distance from the pulser gun and, to this reader, the minor discrepancies in theory vs. experiment were largely cleared up by some work published in 2007 [21] that included Microwave Studio (MWS) computer simulations. Caniggia and Maradei [21] found substantial effect of the return path of the current, which depends on gun strap placement and is even frequency-dependent. Nonetheless, at 150 cm distance from the source, there is now some case for viewing the current pulse as, primarily, a magnetic dipole. Note that with a magnetic dipole, the dipole moment goes as $I(s)$ instead of $I(s)/s$, and that, mirroring the H field for electric dipole radiation, there is no long-term static electric field. In short, the extra derivative of the magnetic dipole model leads to a reasonably good fit of the E-field profile as measured at 150 cm in [20], including the undershoot, when combined with a simple model (double exponential plus step) for the current as measured at the target. The foregoing is a nearly ideal application of the Laplace Transform field calculation methods described above, and would make a fine homework assignment for students and engineers trying to learn about transient fields. We hope the authors of [20] understand that this is the benefit of hindsight, and the much later efforts of [21] and a result of perhaps other works that led to a more complete understanding. Even so, it appears that the dipole radiation model is still meaningful.

We do not always have a broadband TEM horn antenna with flat frequency response for measuring E-fields, as in [20]. Something smaller is needed in practical manufacturing situations, where a small near field antenna is required [9]. Conveniently, Caniggia and Maradei [21] also discuss basic E-field and H-field probes and their agreement with simple theory. The E-field monopole probe (coaxial cable with extended center conductor) agrees remarkably well with a two-pole, one zero RLC model for the transfer function. Using the notation of the present article, the measured signal as compared to vertical E-field is essentially

$$\frac{V_m(s)}{E_z(s)} = \frac{l_m Z_0 C_m s}{1 + Z_0 C_m s + L_m C_m s^2}, \quad (16)$$

for which Z_0 is cable impedance (usually 50 ohms), C_m and L_m are the inductive and capacitive equivalents of the probe wire, and l_m is the length of the probe wire. Model parameters can be calculated as described in [21] and cited earlier references [22], although it has long been known that the exact solution is a little more complicated [23]. The result for a 6 mm monopole probe as in [21] is a very good dE/dt probe up to 1 GHz or so, and not too severe a departure from the simple model of Eq. (16) beyond that. Such models enhance our prospects for recovering the current $I(s)$ and $I(t)$ (i.e., current imaging) through filtering of the measured field signal. For

example, if (normalized) Eq. (16) is combined with (normalized) Eq. (2) at the equator, we find that

$$\begin{aligned} I(s) &= V_m(s) \frac{1 + Z_0 C_m s + L_m C_m s^2}{s} \cdot \frac{s}{1 + s\tau + s^2\tau^2} \\ &= V_m(s) \frac{1 + Z_0 C_m s + L_m C_m s^2}{1 + s\tau + s^2\tau^2}. \end{aligned} \quad (17)$$

This means that we transform our signal $V(t)$ by the filter function described by the last factor of Eq. (17), and then multiply by the appropriate constants as listed in Eqs. (2) and (16), and we have a time-dependent image of the current $I(t)$. The filtering can be done through direct convolution [13] and there are also free software tools for that, downloadable from the Internet [24]. A time-dependent impulse response for the filter function in (17) is found through the inverse Laplace Transform as usual (it involves a Dirac delta function when numerator and denominator are of equal order, but Mathematica can handle this—it just means that the original function is copied with no time lag, to form a portion of the convolved function) and then convolved with the measured field signal, a very quick spreadsheet operation. It is also clear from (17) that the E-field and its measured signal are generally sharper than the source current producing them, as we're using a low-pass filter function to recover the current pulse from the field. A view of such a filter function is in Figure 10, calculated for 15 cm and with parameters calculated for a 6 mm E-field monopole probe as described in [21], with extra capacitance due to the practice of protecting the probe wire with dielectric cap. Network analyzer measurements of the E-probe antenna should be done to confirm this model, as we will want a reasonable fit to high frequency.

It is interesting to take the parameters for the small E-probe as described for Fig. 10 and apply them to our examples of calculated realistic fields as in Fig. 8, in order to see what kind of signal is expected for CDM events of that sort. These predicted signals, in normalized form following Eq. (16), are shown in Figure 11.

Fig. 11 is our predicted measurement at 15 cm for the CDM pulse currents for the two devices of Fig. 6. Equal charge results in about 2x difference in peak current (Fig. 6) but about 3x the Vp-p for the dE/dt-like measurement. However, other low-pass filtering of the raw signals pictured in Fig 11 could take place. First is the coaxial cable itself, which must respond to these fast signals, where the first half cycle takes less than 150 psec. If the cable is good, the oscilloscope or pre-amplifier must also be fast or it will smooth out these pulses; good models of scope response are discussed in [17]. But we do want a certain amount of smoothing, as shown by the filter function of Fig. 10. It turns out that Fig. 10 is fairly close to the impulse function of a 350 MHz two-pole filter, even one with $D \approx 0.7$ as suggested for oscilloscope in [17]. In this case (note that it applies to a particular probe design and a particular distance from the source, 15 cm), the correct completion of the measurement channel will produce a good current image, with expected current scaling. In this way, the entire measurement channel, plus the effect of the radiation zeros, can be tuned to a particular distance from the dipole to give a current image. With enough low-pass filtering, only an indication of the charge Q will remain, but for the case here, the filter would have to be well below 100 MHz for the two pulses to look nearly the same.

With a tuned measurement channel as described above for current imaging, the last factor in Eq. (17) has, in effect, been

absorbed into the measurement channel to achieve complete pole-zero cancellation. But note that if the measurement channel including probe is not quite right at a particular distance, software filtering can complete the process to give a current image. For practical situations in the factory or laboratory—anywhere outside controlled conditions in an anechoic chamber, one would think—the true current image may last only the first few nanoseconds at most, before reflections, resonances and other effects intrude. Even so, in the presence of a known current source location, Eq. (17) inspires us to produce “equivalent small dipole current source” waveforms from our field measurement data, once we decide between electric and magnetic dipole for the source.

Conclusions

Pulsed radiation has been with us for a long time, but a relatively recent motive to study it in semiconductor manufacturing has been the importance of charged device model ESD and the need to avoid damage to sensitive components. Thus there is renewed incentive to study, measure, and analyze the fields of a small or Hertzian dipole, including at near and intermediate range.

The equations for EM dipole near and far radiation fields were presented in this work for the complex frequency domain with a Laplace Transform analysis of the Hertzian dipole case. Expressions in the s-domain for the pulsed current source are then built up from ordinary circuit analysis, and the result is a pole-zero expression for the field, startling in its simplicity. Singularities and abrupt steps can be removed by refining the pulse expression to capture such real effects as spark rise time. There is easy access to these fields at any distance through the inverse Laplace Transform, and access to the latter is easier than ever through software and free web applets. The concept of using these simple models to recover current pulse waveforms, or at least their main features, from E- and H-field measurements, is also viable once the properties of the measurement instruments are known. The field calculation methods thus lead to simple extraction of filter impulse functions that can be used with convolution methods (also deployable through free software) to find the time-dependent waveform of the source current at a given distance from the detector. In some cases, an amplifier, hardware filter, or well-chosen slow oscilloscope (e.g., 350 MHz) can be part of the measurement channel to achieve much the same filtering, thus producing a current image in hardware.

The zeros of the pole-zero expressions for fields always include the “radiation zeros”, which are essential properties of the dipole fields themselves. Pure numbers like $\exp(j\pi(1 \pm 1/3))$ appear to have a deep physical significance, as they are the roots of $(1 + x + x^2)$ and include information about all the fields (static, inductive, radiative) of the radiating dipole. Indeed, as Schantz [5] points out, this complex conjugate pair was found by J.J. Thomson in 1884 [25] to describe the natural frequency of “electrical oscillations” of a perfectly conducting metal sphere, normalized to radius $r = c\tau$. Thomson summarized that study in a longer 1893 work that is available on the Internet [26], and the conducting sphere problem was also later treated by Sommerfeld [27]. But the dipole radiation equations are seldom if ever reduced to a Laplace Transform-inspired pole-zero expression as done here. Doing so yields simple calculation methods, quick solutions, and, for the student, deep insight to the physical phenomena. As the limiting case of the infinitesimal Hertzian dipole has always been a college or

graduate student's starting point for serious consideration of radiation, good interactive tools for developing insight are helpful. Now that we find the small pulsed dipole has remarkable significance for observed CDM radiation, as above, we also need simple, accessible tools for busy working engineers to use for comprehending these practical problems, and thus the methods described in this work were developed.

The author always found the use of " $j\omega$ " in EM-related books to be a bit restrictive, having learned the "secret" of the Laplace Transform and complex frequencies as a college sophomore. He felt free to let $j\omega = s$ on most occasions when reading those books, as the expressions would seem a bit simpler, while also becoming more general. The s -domain expressions in this paper are a good example of that practice, one that brought unusual clarity to the subject under study. The author continues to cross-check as many EM problems as possible with the s -domain approach, using field equations as expressed in this work. Somehow, the "bookkeeping" of the various fields and their r -dependence is more tractable. Consider, for example, the physics examples of Prof. K.T. McDonald of Princeton University [28]. If, like the author, you have often searched the Internet for information on EM problems, you have undoubtedly encountered Prof. McDonald's examples and articles, multiple times. Some of his EM examples are admittedly incomplete, i.e., works in progress. Reformulating the EM dipole equations and current sources in Laplace Transform format can be quite revealing, at least when there is a defined beginning at $t = 0$. Indeed, it was not a field problem but an incomplete capacitor problem posed by McDonald and solved by both of us in 2008 [29] that convinced the author that more Laplace Transform analysis is needed to understand and solve ESD problems. After all, ESD is a pulse that begins at time zero.

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Biography



Timothy J. Maloney received an S.B. degree in physics from the Massachusetts Institute of Technology in 1971, an M.S. in physics from Cornell University in 1973, and a Ph.D. in electrical engineering from Cornell in 1976, where he was a National Science Foundation Fellow. He was a Postdoctoral Associate at Cornell until 1977, when he joined the Central Research Laboratory of Varian Associates, Palo Alto, CA. At Varian until 1984, he worked on III-V semiconductor photocathodes, solar cells and microwave devices, as well as silicon molecular beam epitaxy and MOS process technology. Since 1984 he has been with Intel Corp., Santa Clara, CA, where he has been concerned with integrated circuit electrostatic discharge (ESD) protection and testing, CMOS latchup, fab process reliability, signal integrity, and system ESD testing, including cable discharge. His papers at the 2008 and 2010 EMC Symposium relate to system ESD tests. He is now a Senior Principal Engineer at Intel. He has received the Intel Achievement Award for his patented ESD protection devices, which have achieved breakthrough ESD performance enhancements for a wide variety of Intel products. He now holds thirty-two patents, with several more pending.

Dr. Maloney received Best Paper Awards for his contributions to the EOS/ESD Symposium in 1986 and 1990, was General Chairman for the 1992 EOS/ESD Symposium, and received the ESD Association's Outstanding Contributions Award in 1995. He has taught short courses at UCLA, University of Wisconsin, and UC Berkeley. He is co-author of a book, "Basic ESD and I/O Design" (Wiley, 1998), and is a Fellow of the IEEE.

EMC

Physical Dimensions vs Electrical Dimensions

Clayton R. Paul, Mercer University, Macon, GA (USA), paul_cr@Mercer.edu

Abstract – With the operating frequencies of today’s high-speed digital and high-frequency analog systems increasing, previous lumped-circuit analysis methods will no longer be valid and will give incorrect answers. When the maximum physical dimensions of the system are *electrically large* (greater than a tenth of a wavelength) the system cannot be reliably analyzed using Kirchhoff’s voltage and current laws and lumped-circuit methods.

I. Deficiencies With The Exclusive Use of Kirchhoff’s Laws and Lumped-Circuit Models

The spectral (frequency) content of modern high-speed digital waveforms today is extending into the GHz regime. Similarly, the operating frequencies of analog systems are extending well into the GHz range. A digital clock waveform has a trapezoidal shape as illustrated in Fig. 1:

Since a digital clock waveform is a periodic, repetitive waveform, according to the Fourier series their time-domain waveforms can be alternatively viewed as being composed of an infinite number of harmonically related sinusoidal components as [1]

$$\begin{aligned} x(t) &= c_0 + c_1 \cos(\omega_0 t + \theta_1) + c_2 \cos(2\omega_0 t + \theta_2) \\ &\quad + c_3 \cos(3\omega_0 t + \theta_3) + \dots \\ &= c_0 + \sum_{n=1}^{\infty} c_n \cos(n\omega_0 t + \theta_n) \end{aligned} \quad (1)$$

The period T of the periodic waveform is the reciprocal of the clock fundamental frequency, f_0 , and the fundamental radian frequency is $\omega_0 = 2\pi f_0$. The rise/fall times are denoted as τ_r and τ_f , respectively, and the pulse width (between 50% levels) is denoted as τ . As the fundamental frequencies of the clocks, f_0 , are increased, their period $T = 1/f_0$ decreases and hence the rise/fall times of the pulses must be reduced commensurately in order that pulses resemble a trapezoidal shape rather than a “saw tooth” waveform thereby giving adequate “setup” and “hold” time intervals. Reducing the pulse rise/fall times has had the consequence of increasing the spectral content of the wave shape. Typically this spectral content is significant up to the inverse of the rise/fall times, $1/\tau_r$. For example, a 1 GHz digital clock signal having rise/fall times of 100ps has significant spectral content at multiples (harmonics) of the basic clock frequency (1 GHz, 2 GHz, 3 GHz, ...) up to around 10 GHz.

In the past, clock speeds and data rates of digital systems were in the megahertz (MHz) range with rise/fall times of the pulses in the nanosecond ($1\text{ns} = 10^{-9}\text{s}$) range. Prior to that time, the “lands” (conductors of rectangular cross section) that interconnect the electronic modules on printed circuit boards (PCBs) had little effect on the proper functioning of those electronic circuits. The time delays through the modules dominated the time delay imposed by the interconnect conductors.

Today, the clock and data speeds have rapidly moved into the low gigahertz (GHz) range. The rise/fall times of those digital waveforms have decreased into the picosecond ($1\text{ps} = 10^{-12}\text{s}$) range. The delays of the interconnects have become the dominant factor.

Although the “physical lengths” of the lands that interconnect the electronic modules on the PCBs have not changed significantly over these intervening years, their “electrical lengths” (in wavelengths) have increased dramatically because of the increased spectral content of the signals that the lands carry. Today these “interconnects” can have a significant effect on the signals they are carrying so that just getting the systems to work properly has become a major design problem. Remember that it does no good to write sophisticated software if the hardware cannot faithfully execute those instructions. This has generated a new design problem referred to as *Signal Integrity*. Good signal integrity means that the interconnect conductors (the lands) should not adversely affect the operation of the modules that the conductors interconnect. Because these interconnects are becoming “electrically long”, lumped-circuit modeling of them is becoming inadequate and gives erroneous answers. The interconnect conductors must now be treated as distributed-circuit *transmission lines*.

II. Traveling Waves, Time Delay and Wavelength

In the analysis of electric circuits using Kirchhoff’s voltage and current laws and lumped-circuit models, we *ignored* the connection leads attached to the lumped elements. When is this permissible? Consider a lumped-circuit element having attachment leads of total length \mathcal{L} shown in Fig. 2. *Single-frequency, sinusoidal* currents along the attachment leads are in fact *traveling waves* which can be written in terms of position z along the leads and time t as

$$i(t, z) = I \cos(\omega t - \beta z) \quad (2)$$

where the radian frequency ω is written in terms of cyclic frequency f as $\omega = 2\pi f$ ^{radians/s} and β is the *phase constant* in

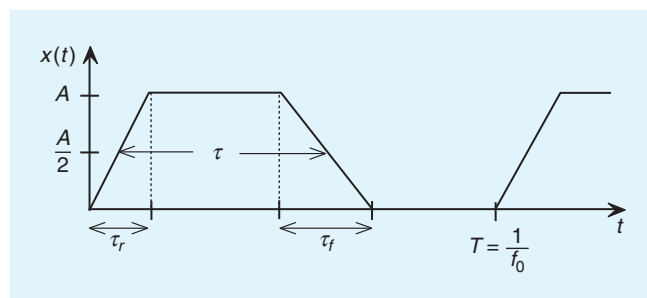


Fig. 1. A typical digital clock/data waveform.

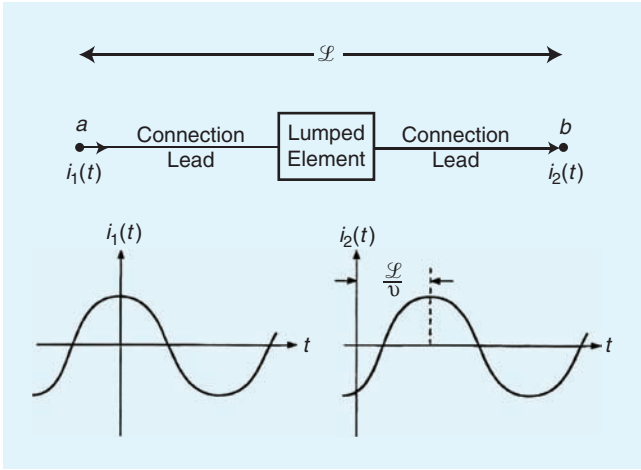


Fig. 2. Current waves on connection leads of lumped-circuit elements.

units of $\text{radians}/\text{m}$. (Note that the argument of the cosine must be in radians and not degrees.) In order to observe the movement of these current waves along the connection leads, we observe and track the movement of a point on the wave in the same way as we observe the movement of an ocean wave at the seashore. Hence the argument of the cosine in (2) must remain constant in order to track the movement of a point on the wave so that $\omega t - \beta z = C$ where C is a constant. Rearranging this as $z = (\omega/\beta)t - (C/\beta)$ and differen-

tiating with respect to time gives the velocity of propagation of the wave as

$$v = \frac{\omega}{\beta} \quad \frac{\text{m}}{\text{s}} \quad (3)$$

Since the argument of the cosine, $\omega t - \beta z$, in (2) must remain a constant in order to track the movement of a point on the wave, as time t increases so must the position z . Hence the form of the current wave in (2) is said to be a *forward-traveling wave* since it must be traveling in the $+z$ direction in order to keep the argument of the cosine constant for increasing time. Similarly, a *backward-traveling wave* traveling in the $-z$ direction would be of the form $i(t, z) = I \cos(\omega t + \beta z)$ since as time t increases, position z must decrease in order to keep the argument of the cosine constant and thereby track the movement of a point on the waveform. Since the current is a *traveling wave*, the current entering the leads, $i_1(t)$, and the current exiting the leads, $i_2(t)$, are separated in time by a *time delay* of

$$T_D = \frac{L}{v} \quad \text{s} \quad (4)$$

as illustrated in Fig. 2. These single-frequency waves suffer a *phase shift* of $\phi = \beta z$ radians as they propagate along the leads. Substituting (3) for $\beta = (\omega/v)$ into the equation of the wave in (2) gives an equivalent form of the wave as

$$i(t, z) = I \cos\left(\omega \left(t - \frac{z}{v}\right)\right) \quad (5)$$

which indicates that *phase shift is equivalent to a time delay*.

Figure 2 plots the current waves *versus time*. Figure 3 plots the current wave *versus position in space at fixed times*. As we will see, the critical property of a traveling wave is its *wavelength* denoted as λ . A *wavelength* is the distance the wave must travel in order to shift its phase by 2π radians or 360° . Hence $\beta\lambda = 2\pi$ or

$$\lambda = \frac{2\pi}{\beta} \quad \text{m} \quad (6)$$

Substituting the result in (3) for β in terms of the wave velocity of propagation v gives an alternative result for computing the wavelength:

$$\lambda = \frac{v}{f} \quad \text{m} \quad (7)$$

Table 1 gives the wavelengths of single-frequency sinusoidal waves in free space (essentially air) where $v_0 \cong 3 \times 10^8$. (The velocities of propagation of current waves on the lands of a PCB are less than in free space which is due to the interaction of the electric fields with the board material. Hence wavelengths on a PCB are shorter than they are in free space.) Observe that a wave of frequency 300 MHz has a wavelength of 1m. Note that the product of the frequency of the wave and its wavelength equals the velocity of wavelength of the wave, $f\lambda = v$. Wavelengths scale linearly with frequency. As frequency decreases, the wavelength increases and vice-versa. For example, the wavelength of a 7 MHz wave is easily computed as

$$\lambda|_{@7 \text{ MHz}} = \frac{300 \text{ MHz}}{7 \text{ MHz}} \times 1 \text{ m} = 42.86 \text{ m}$$

Similarly, the wavelength of a 2GHz cell phone wave is 15cm which is approximately 6in.

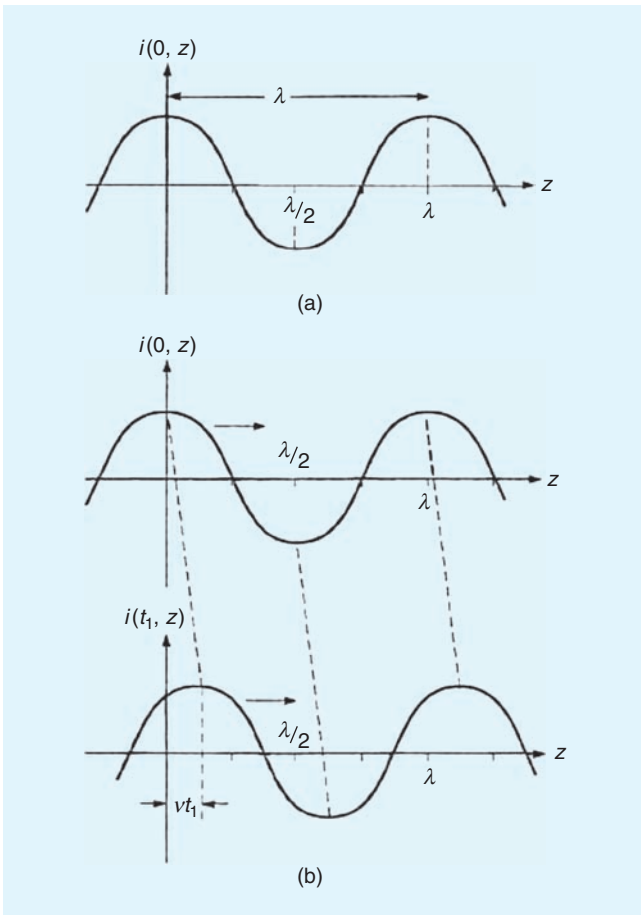


Fig. 3. Illustration of waves in space and wavelength.

TABLE 1. FREQUENCIES OF SINUSOIDAL WAVES IN FREE SPACE (AIR) AND THEIR CORRESPONDING WAVELENGTHS

Frequency (f)	Wavelength (λ)
60 Hz	3107 miles (5000 km)
3 kHz	100 km
30 kHz	10 km
300 kHz	1 km
3 MHz	100 m (\approx 300 feet)
30 MHz	10 m
300 MHz	1 m (\approx 3 feet)
3 GHz	10 cm (\approx 4 inches)
30 GHz	1 cm
300 GHz	0.1 cm

Now we turn to the important criterion of physical dimensions in terms of wavelengths, i.e., “electrical dimensions”. In order to determine a physical dimension, \mathcal{L} in terms of wavelengths (its “electrical dimension”) we write $\mathcal{L} = k\lambda$ and determine the length in wavelengths as

$$k = \frac{\mathcal{L}}{\lambda} = \left(\frac{\mathcal{L}}{v}\right)f$$

where we have substituted the wavelength in terms of the frequency and velocity of propagation as $\lambda = v/f$. Hence we obtain an important relation for the electrical length in terms of frequency and time delay:

$$\frac{\mathcal{L}}{\lambda} = f \frac{\mathcal{L}}{v} = f T_D \quad (8)$$

so that a dimension is one wavelength, $\mathcal{L}/\lambda = 1$, at a frequency that is the inverse of the time delay:

$$f|_{\mathcal{L}=\lambda} = \frac{1}{T_D} \quad (9)$$

A single-frequency, sinusoidal wave shifts phase as it travels a distance \mathcal{L} of

$$\phi = \beta \mathcal{L} = 2\pi \frac{\mathcal{L}}{\lambda} \text{ radians} = \frac{\mathcal{L}}{\lambda} \times 360^\circ \text{ degrees} \quad (10)$$

Hence if a wave travels a distance of one wavelength, $\mathcal{L} = \lambda$, it shifts phase by $\phi = 360^\circ$. If the wave travels a distance of one-half wavelength, $\mathcal{L} = 1/2 \lambda$, it shifts phase by $\phi = 180^\circ$. This can provide for cancellation for example when two antennas which are separated by a distance of one-half wavelength transmit the same frequency signal. Along a line containing the two antennas, the two radiating waves being of opposite phase cancel each other giving a result of zero. This is the essential reason why antennas have “patterns” where a null is produced in one direction, whereas a maximum is produced in another direction. Phased-array radars electronically “steer” their beams using this principle rather than by mechanically rotating the antennas. Next consider a wave that travels a distance of one-

tenth of a wavelength, $\mathcal{L} = 1/10 \lambda$. The phase shift incurred in doing so is only $\phi = 36^\circ$, and a wave that travels one-one hundredth of a wavelength, $\mathcal{L} = 1/100 \lambda$, incurs a phase shift of $\phi = 3.6^\circ$. Hence we say that

for any distance less than, say, $\mathcal{L} < 1/10\lambda$, the phase shift is said to be negligible and the distance is said to be electrically short.

For electric circuits whose maximum physical dimension is electrically short, $\mathcal{L} < 1/10\lambda$, Kirchhoff’s voltage and current laws and other lumped-circuit analysis solution methods work very well. For physical dimensions that are not electrically short, Kirchhoff’s laws and lumped-circuit analysis methods give erroneous answers! For example, consider an electric circuit that is driven by a 10 kHz sinusoidal source. The wavelength at 10 kHz is 30km (18.641 mi)! Hence at this frequency any circuit having a maximum dimension less than 3km (1.86 mi) can be successfully analyzed using Kirchhoff’s laws and lumped-circuit analysis methods. Electric power distribution systems operating at 60 Hz can be analyzed using Kirchhoff’s laws and lumped-circuit analysis principles so long as their physical dimensions such as the transmission line length are less than some 310 mi! Similarly, a circuit driven by a 1 MHz sinusoidal source can be successfully analyzed using lumped-circuit analysis methods if its maximum physical dimension is less than 30 m! On the other hand, cell phone electronic circuits operating at a frequency of around 2 GHz cannot be analyzed using lumped-circuit analysis methods unless the maximum dimension is less than around 1.5 cm or about 0.6 in! We can alternatively determine the frequency where a dimension is electrically short in terms of the time delay from (8):

$$f|_{\mathcal{L}=\frac{1}{10}\lambda} = \frac{1}{10T_D} \quad (11)$$

Substituting $\lambda f = v$ into the time delay expression in (4) gives the time delay as a portion of the period of the sinusoid, T :

$$T_D = \frac{\mathcal{L}}{v} = \left(\frac{\mathcal{L}}{\lambda}\right)\left(\frac{1}{f}\right) = \left(\frac{\mathcal{L}}{\lambda}\right) T \quad (12)$$

where the period of the sinusoidal wave is $T = 1/f$. This shows that if we plot the current waves in Fig. 2 that enter and leave the connection leads versus time t on the same time plot, they will be displaced in time by a fraction of the period, \mathcal{L}/λ . If the length of the connection leads \mathcal{L} is electrically short at this frequency, then the two current waves will be displaced from each other in time by an inconsequential amount of less than $T/10$ and may be considered to be coincident in time. This is the reason why Kirchhoff’s laws and lumped-circuit analysis methods work well only for circuits whose maximum physical dimension is “electrically small”.

This has demonstrated the important principle in electromagnetics that “physical dimensions” of structures don’t matter: their “electrical dimensions in wavelengths” are important.

III. An Example

Consider the typical source-load circuit shown in Fig. 4. A single-frequency, sinusoidal source, $V_S(t) = V_S \cos(\omega t + \theta_S)$, having a source resistance R_S sends a signal to a load represented by a load resistance R_L . The source and load are separated by a parallel pair of wires or a pair of lands of length \mathcal{L} .

The lumped-circuit model *ignores* the two interconnect conductors of length \mathcal{L} . Analyzing this configuration as a lumped circuit gives (using voltage division and ignoring the interconnect conductors) the ratio of the source and load voltage magnitudes as

$$\frac{V_L}{V_S} = \frac{R_L}{R_S + R_L}$$

and the phase angles are identical: $\theta_S = \theta_L$. These, according to a lumped-circuit model of the line, remain the same for *all source frequencies!*

Consider a specific configuration shown in Fig. 5. The parameters are $R_S = 10\Omega$, $R_L = 1000\Omega$ for a line of total length of $\mathcal{L} = 0.3\text{m}$ (or about 12 inches). Ignoring the interconnect conductors gives $V_L/V_S = 0.99$ and the phases are related as $\theta_L - \theta_S = 0^\circ$.

The *exact solution* is obtained by including the two interconnect conductors of length \mathcal{L} as a distributed-parameter *transmission line*. The circuit analysis computer program, PSPICE, contains an exact transmission line model of the interconnect conductors [1]. Figure 6 shows the *exact* ratio of the voltage magnitude, V_L/V_S , and voltage angle, $\theta_L - \theta_S$, versus the frequency of the source as it is swept in frequency from 1MHz to 1GHz. Model the interconnect conductors as a distributed parameter, transmission line having a characteristic impedance of $Z_C = 50\Omega$ and a one-way delay of the interconnect line of $T_D = (\mathcal{L} = 0.3\text{m})/(v_0 = 3 \times 10^8)(\text{m/s}) = 1\text{ns}$. The entire configuration is analyzed using PSPICE. Figure 6 shows that the magnitudes and angles of the *transfer function* voltages, V_L/V_S , and $\theta_L - \theta_S$, begin to deviate rather drastically from the low frequency, lumped-circuit analysis result of $V_L/V_S = 0.99$ and $\theta_L - \theta_S = 0^\circ$ above about 100 MHz.

The line is one-tenth of a wavelength (electrically short) at $f|_{\mathcal{L}=(1/10)\lambda} = (1/10T_D = 10\text{ ns}) = 100\text{ MHz}$ (denoted by the

vertical line at 100 MHz in both plots). This is evident in the plots in Fig. 6. Hence the interconnect line is electrically long above 100 MHz. The interconnect line is one wavelength at 1 GHz: $f|_{\mathcal{L}=\lambda} = (1/T_D = 1\text{ ns}) = 1\text{ GHz}$. Observe that the magnitude plot in Fig. 6(a) shows two peaks of 250 MHz and 750 MHz where the interconnect line electrical length is $\lambda/4$ and $3/4\lambda$, respectively, and the magnitude of the transfer function increases to a level of 4. There are two minima at 500 MHz and 1 GHz where the interconnect line electrical length is $\lambda/2$ and λ , respectively. Above 1 GHz (the last frequency plotted) the pattern replicates which is a general property of transmission lines.

Finally we investigate the *time-domain* response of the line where we drive the line with a clock signal of 10 MHz fundamental frequency (a period of 100 ns), an amplitude of 1 V, rise/fall times of 10 ns, and a 50% duty cycle as shown in Fig. 7. It is typical for the rise/fall times of digital waveforms to be chosen to be around 10% of the period T in order to give adequate "setup" and "hold" times.

Figure 8 shows the comparison of the load voltage waveform, $V_L(t)$, and the source voltage waveform, $V_S(t)$, for this source waveform over two cycles of the source. The source voltage and load voltage waveforms are virtually identical, and the interconnect line clearly has no substantial effect. From the frequency response of the waveform in Fig. 6 we see that the first 10 harmonics of this waveform (the bandwidth of the waveform is $\text{BW} = 1/\tau_r = 100\text{ MHz}$), 10 MHz, 20 MHz, 30 MHz, 40 MHz, 50 MHz, 60 MHz, 70 MHz, 80 MHz, 90 MHz, 100 MHz, all fall below the frequency where the line ceases to be electrically short: 100 MHz. This is what we expect when the major harmonic components of the waveform (its BW) fall into the frequency range where the line is electrically short for all of them.

Figure 9 shows the same comparison when the source parameters are changed to a 100 MHz fundamental frequency (a period of 10 ns), having an amplitude of 1 V, rise/fall times of

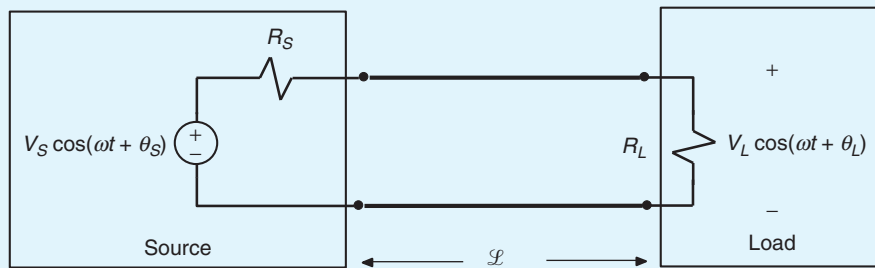


Fig. 4. A general source-load configuration.

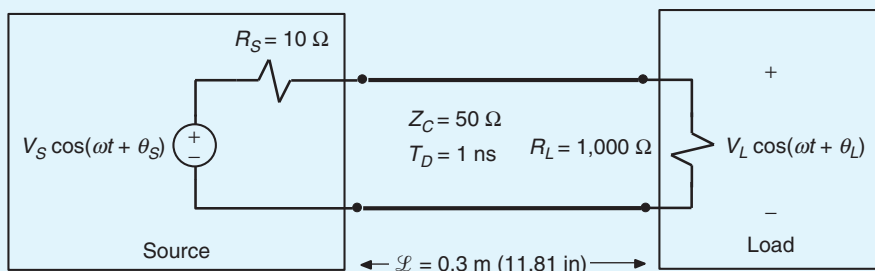


Fig. 5. A specific example treating the connection lands as a transmission line.

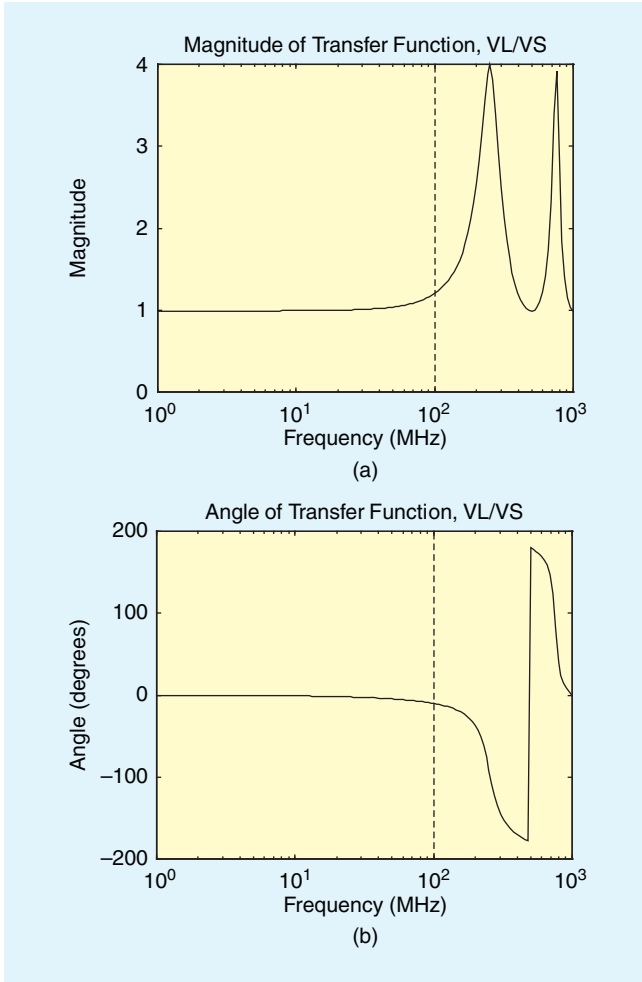


Fig. 6. Frequency response of the line in Fig. 5.

1ns, and a 50% duty cycle. From Fig. 6, this waveform contains the first 10 harmonics that constitute the major components in its bandwidth ($BW=1/\tau_r = 1$ GHz): 100 MHz, 200 MHz, 300 MHz, 400 MHz, 500 MHz, 600 MHz, 700 MHz, 800 MHz, 900 MHz, 1 GHz. The line length is $\lambda/10$ at the fundamental frequency of it, 100 MHz, and 1λ at its tenth harmonic of 1 GHz. Observe that the load voltage waveform bears no resemblance to the source waveform. From the frequency-response of the system in Fig. 6, we see that all of these harmonics fall in the frequency range where the interconnect line is *electrically long* (>100 MHz) so this is expected.

The plots in Figure 8 and 9 were both plotted using PSPICE. The load voltages, $V_L(t)$, can be manually plotted using the simple method described in [2]. This solution for the $V_S(t)$ for the waveform of Fig. 9 is shown in Fig. 10 as the superposition of the scaled and delayed versions of $V_S(t)$. This shows how the final waveform is composed of the sum of the scaled and delayed $V_S(t)$ as [2]:

$$\begin{aligned}
 V_L(t) &= \frac{Z_C}{Z_S + Z_C} (1 + \Gamma_L) [V_S(t - T_D) + (\Gamma_S \Gamma_L) V_S(t - 3T_D) + \\
 &\quad (\Gamma_S \Gamma_L)^2 V_S(t - 5T_D) + (\Gamma_S \Gamma_L)^3 V_S(t - 7T_D) + \dots] \\
 &= 1.59 V_S(t - 1 \text{ ns}) - 0.96 V_S(t - 3 \text{ ns}) + 0.58 V_S(t - 5 \text{ ns}) \\
 &\quad - 0.35 V_S(t - 7 \text{ ns}) + 0.21 V_S(t - 9 \text{ ns}) + \dots
 \end{aligned}$$

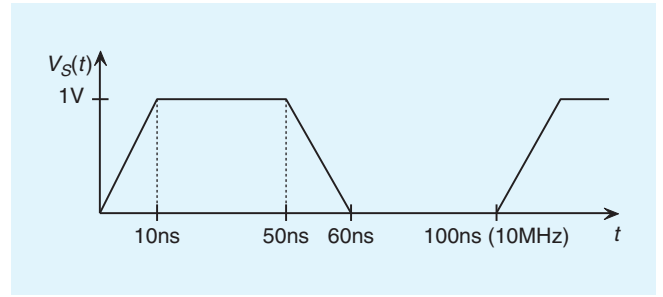


Fig. 7. The source voltage.

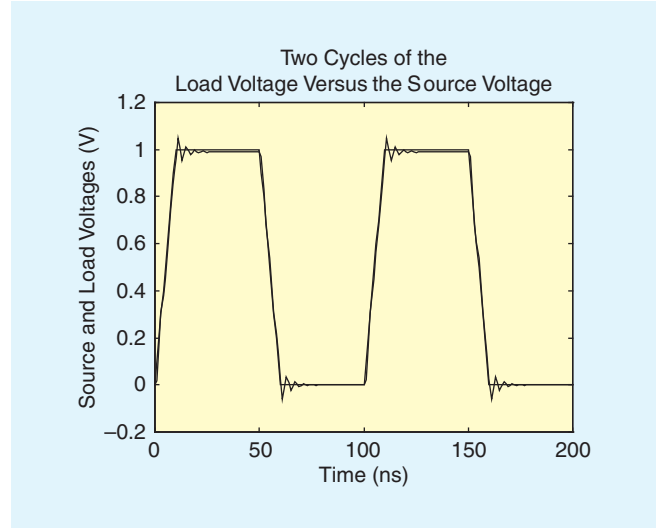


Fig. 8. Comparison of the source and load waveforms for a 1 V, 10 MHz waveform with rise/fall times of $\tau_r = \tau_f = 10$ ns and a 50% duty cycle (see Fig. 7).

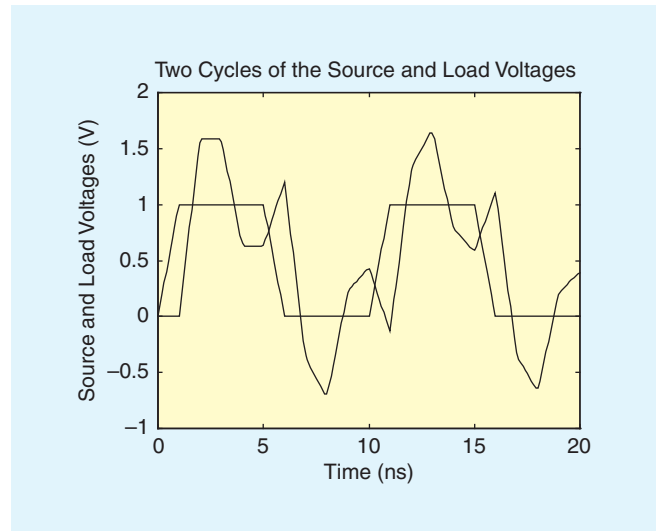


Fig. 9. Comparison of the source and load waveforms for a 1 V, 100 MHz waveform with rise/fall times of $\tau_r = \tau_f = 1$ ns and a 50% duty cycle.

where $Z_C/(Z_S + Z_C)(1 + \Gamma_L) = 1.59$ and $(\Gamma_S \Gamma_L) = -0.6$ and the source and load reflection coefficients are $\Gamma_S = (R_S - Z_C)/(R_S + Z_C) = -0.667$ and $\Gamma_L = (R_L - Z_C)/(R_L + Z_C) = 0.905$.

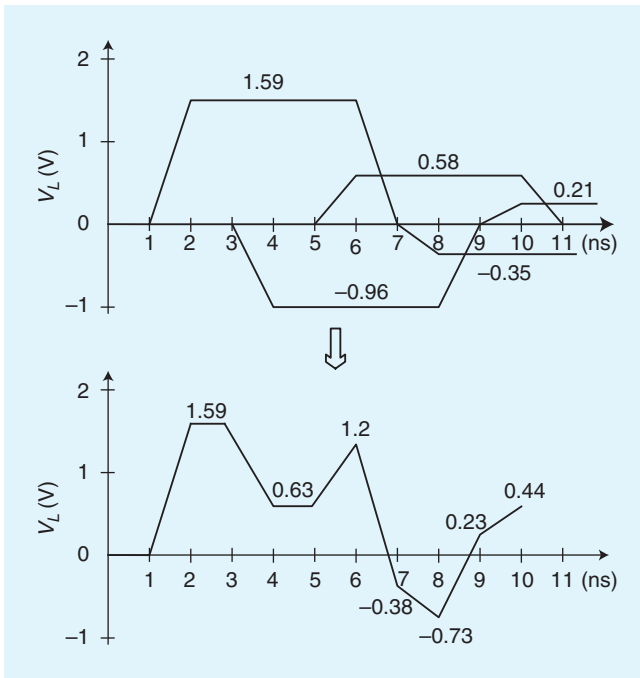


Fig. 10. Manual sketching the load voltage for Fig. 9 using the method of [2].

This simple manual solution method described in [2] clearly shows how the various parameters (particularly the relation of the pulse rise/fall times versus the line one-way time delay) affect the final waveform. For example, Fig. 10 shows that because the rise/fall times of the source for Fig. 9 is the same as the one-way delay of the line of 1ns, the various individual waveforms combine to give a complex final waveform. On the other hand, the rise/fall times of the source voltage for the solution in Fig. 8 are 10ns such that $\tau_r = 10 \text{ ns} = 10T_D$. Hence the waveforms to be superimposed in Fig. 8 are widely separated whose sum give a smooth and reduced amplitude final waveform. This confirms a previously obtained criterion that $\tau_r > 10T_D$ implies that the line is electrically short for all the frequency components that the source waveform contains in its BW (BW = 100 MHz for $\tau_r = 10 \text{ ns}$ but not for the case of BW = 1 GHz for $\tau_r = 1 \text{ ns}$).

IV. Summary

This article has shown that as the frequencies of the sources increase to the point where the interconnect lines connecting the source and the load become *electrically long*, the standard lumped-circuit models are no longer valid and give erroneous answers. The requirement to model electrically long interconnects requires that we master transmission line modeling. Although the analysis is more difficult for electrically large circuits, we have no choice as the frequencies continue to increase, seemingly without bound.

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Biography



Clayton R. Paul received the B.S. degree, from The Citadel, Charleston, SC, in 1963, the M.S. degree, from Georgia Institute of Technology, Atlanta, GA, in 1964, and the Ph.D. degree, from Purdue University, Lafayette, IN, in 1970, all in Electrical Engineering. He is an Emeritus Professor of Electrical Engineering at the University of Kentucky where he was a member of the faculty in the Department of Electrical Engineering for 27 years retiring in 1998. Since 1998 he has been the Sam Nunn Eminent Professor of Aerospace Systems Engineering and a Professor of Electrical and Computer Engineering in the Department of Electrical and Computer Engineering at Mercer University in Macon, GA. He has published numerous papers on the results of his research in the Electromagnetic Compatibility (EMC) of electronic systems and given numerous invited presentations. He has also published 18 textbooks and Chapters in 4 handbooks. Dr. Paul is a Life Fellow of the Institute of Electrical and Electronics Engineers (IEEE) and is an Honorary Life Member of the IEEE EMC Society. He was awarded the 2005 IEEE Electromagnetics Award and the 2007 IEEE Undergraduate Teaching Award.

A Simple Causality Checker and Its Use in Verifying, Enhancing, and Depopulating Tabulated Data from Electromagnetic Simulation

Brian Young and Amarjit S. Bbandal, ASIC Package Design Texas Instruments, Austin, TX, USA; Northampton, UK, brian.young@ti.com; a-bbandal@ti.com

Introduction

Electromagnetic (EM) simulators are very powerful, flexible, and accurate. They are also necessarily somewhat complex to setup, requiring user inputs on materials and material models, ports, boundary conditions, meshing frequencies, bandwidth, convergence tolerance, and other required and optional variables. The simulators are in use by the full spectrum of engineers, from new college graduates with little formal EM training to highly experience engineers with advanced degrees in EM and numerical methods. Issues can range from poorly conceived setups to simple typos. All users face the same problem: How do you know that the computed results are correct, reliable, and usable? In transient simulations, low quality computed results can easily result in non-causal models and simulation artifacts, such as faster-than-light signal propagation [1][2][3].

For the most part, the decision on usability of computed results is based on the user's judgment of the "quality" of the results from inspection, on whether the results match expectations, and on the convergence error numbers produced by the simulator. Such an experienced-based approach needs to be augmented by a quantified quality check to help ensure the consistent development of high-quality models.

All data must be causal to be usable, and a causality check of the data is a strong test of data quality that is quantifiable. Many causality tests have been proposed and discussed [4][5][6][7]. The causality checker presented in [7] is reviewed and demonstrated here to show that a good causality checker is relatively simple to implement and can produce powerful observations on the quality of data while guiding its enhancement.

Causality Checker

Causal data must satisfy the Hilbert Transform, so a direct calculation of the Hilbert Transform produces a check of causality. Assuming that the S-parameters are split into real and imaginary parts as $S(\omega) = U(\omega) + jV(\omega)$, then the Hilbert Transform is

$$U(\omega) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{V(\omega')}{\omega - \omega'} d\omega' + K \quad (1)$$

$$V(\omega) = -\frac{1}{\pi} \int_{-\infty}^{\infty} \frac{U(\omega')}{\omega - \omega'} d\omega' \quad (2)$$

The integrals are defined according to the Cauchy principal value, and K is an unknown constant. The main difficulties

in executing the integration are manually extracting the singularity, extending the integration to infinity from bounded data, extrapolation to zero frequency, and determining K.

A causality checker can be implemented by simply calculating an estimate for $U(\omega)$ from the original $V(\omega)$ data using (1) and finding the error between the original and estimated data. Similarly, (2) can be used to estimate $V(\omega)$ from the original $U(\omega)$. In this work, rather than view the errors of the real and imaginary parts, the magnitudes and phases are compared. Interpretation of error plots is sometimes eased by averaging the errors over a rolling $\pm 20\%$ bandwidth, and the plots using averaging are labeled with the averaging bandwidth. For multiport data, the causality checker is applied independently to each port at a time.

The integrals can be computed using a piece-wise linear approximation. To keep the implementation simple, the data is mirrored to negative frequencies, where the real part is an even function of frequency and the odd part is an odd function. The implementation is further simplified by deleting the data at zero frequency and letting the even/odd properties synthesize the data at zero. The piece-wise linear approximation is

$$\tilde{U}(\omega) = m_{Uk}\omega + b_{Uk}, \quad \omega_k < \omega < \omega_{k+1} \quad (3)$$

$$\tilde{V}(\omega) = m_{Vk}\omega + b_{Vk}, \quad \omega_k < \omega < \omega_{k+1} \quad (4)$$

where the slopes m and the intercepts b are calculated from the tabulated data. Inserting (3) into (2) and (4) into (1) results in a reconstruction of the original data as

$$\hat{U}(\omega) = \frac{1}{\pi} \sum_{k=0}^{N-1} \int_{\omega_k}^{\omega_{k+1}} \frac{m_{Uk}\omega' + b_{Uk}}{\omega - \omega'} d\omega' + K + \frac{1}{\pi} \int_{-\infty}^{\omega_0} \frac{V(\omega')}{\omega - \omega'} d\omega' + \frac{1}{\pi} \int_{\omega_N}^{\infty} \frac{V(\omega')}{\omega - \omega'} d\omega' \quad (5)$$

$$\hat{V}(\omega) = -\frac{1}{\pi} \sum_{k=0}^{N-1} \int_{\omega_k}^{\omega_{k+1}} \frac{m_{Vk}\omega' + b_{Vk}}{\omega - \omega'} d\omega' - \frac{1}{\pi} \int_{-\infty}^{\omega_0} \frac{U(\omega')}{\omega - \omega'} d\omega' - \frac{1}{\pi} \int_{\omega_N}^{\infty} \frac{U(\omega')}{\omega - \omega'} d\omega', \quad (6)$$

where $k = 0 \dots N$ covers all tabulated discrete frequencies, both positive and negative, from smallest to largest. The general linear integration term is given by

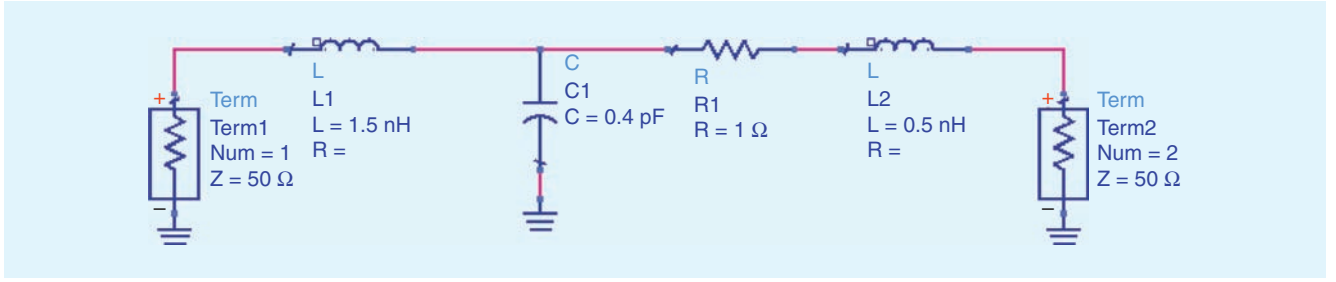


Fig. 1. Lumped circuit for causality test.

$$\int_{\omega_k}^{\omega_{k+1}} \frac{m_k \omega' + b_k}{\omega - \omega'} d\omega'$$

$$= \begin{cases} -m_k(\omega_{k+1} - \omega_k) - [m_k \omega + b_k] \ln\left(\frac{\omega_{k+1} - \omega}{\omega_k - \omega}\right), \\ -m_k(\omega_{k+1} - \omega_k) - [m_k \omega_k + b_k] \ln(\omega_{k+1} - \omega_k), \omega = \omega_k \\ -m_k(\omega_{k+1} - \omega_k) + [m_k \omega_{k+1} + b_k] \ln(\omega_{k+1} - \omega_k), \omega = \omega_{k+1} \end{cases} \quad (7)$$

To solve the special case where $\omega = \omega_k$, the integration is performed for the intervals ω_{k-1} to $\omega_k - \varepsilon$ and $\omega_k + \varepsilon$ to ω_{k+1} , then let $\varepsilon \rightarrow 0$. The result is then split over the two intervals.

The integration terms from negative infinity and to positive infinity must be approximated since the actual data does not exist. It is assumed that the data is simulated to very high frequencies so that simple extrapolation is sufficient. For the real part, an even function is required, and the simplest available is

a constant function matching the value at the highest available frequency. As before, the positive and negative frequency intervals are solved together. For $\hat{V}(\omega)$ in (6),

$$\int_{-\infty}^{\omega_0} \frac{U(\omega')}{\omega - \omega'} d\omega' + \int_{\omega_N}^{\infty} \frac{U(\omega')}{\omega - \omega'} d\omega'$$

$$\cong \int_{-\infty}^{-\omega_N} \frac{U(-\omega_N)}{\omega - \omega'} d\omega' + \int_{\omega_N}^{\infty} \frac{U(\omega_N)}{\omega - \omega'} d\omega'$$

$$= U(\omega_N) \ln\left(\frac{\omega_N - \omega}{\omega_N + \omega}\right). \quad (8)$$

For the imaginary part, an odd function is required, and the simplest available with a decreasing magnitude with increasing frequency is $1/\omega$. For $\hat{U}(\omega)$ in (5),

$$\int_{-\infty}^{\omega_0} \frac{V(\omega')}{\omega - \omega'} d\omega' + \int_{\omega_N}^{\infty} \frac{V(\omega')}{\omega - \omega'} d\omega'$$

$$\cong - \int_{-\infty}^{-\omega_N} \frac{V(\omega_N) \omega_N}{\omega'(\omega - \omega')} d\omega' + \int_{\omega_N}^{\infty} \frac{V(\omega_N) \omega_N}{\omega'(\omega - \omega')} d\omega'$$

$$= V(\omega_N) \frac{\omega_N}{\omega} \ln\left(\frac{\omega_N - \omega}{\omega_N + \omega}\right). \quad (9)$$

The special cases when $\omega = \omega_0$ and $\omega = \omega_N$ do not significantly enhance a causality check, so they are omitted for simplicity.

The constant K in (1) is determined by simply shifting in $\hat{U}(\omega)$ amplitude so that $\hat{U}(\omega_{\min}) = U(\omega_{\min})$, where ω_{\min} is the smallest positive frequency.

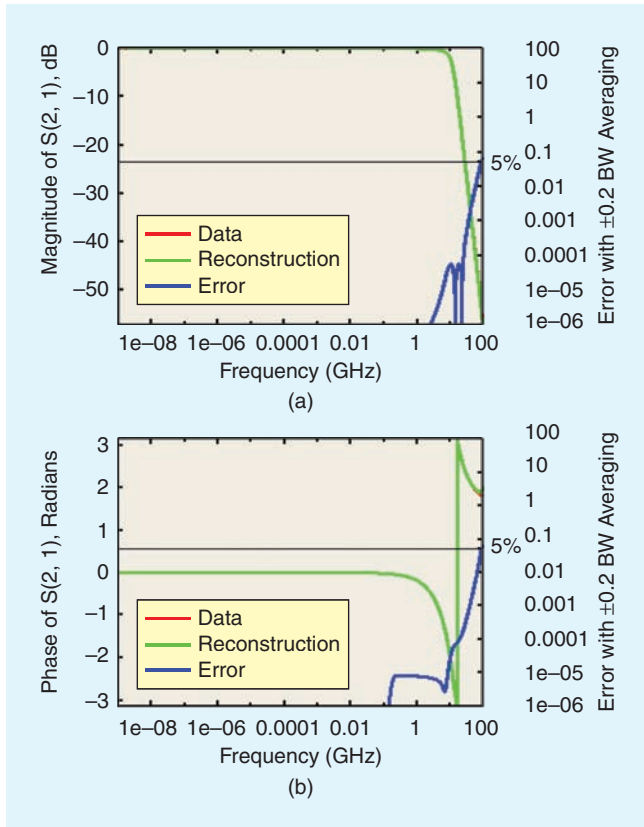


Fig. 2. Reconstruction and error for a computed causal lumped data set. (a) magnitude and (b) phase.

Test on Causal Data

To demonstrate the level of accuracy expected from the described causality checker, a set of 2-port S-parameters are generated for the causal lumped circuit shown in Fig. 1. S_{21} magnitude and phase reconstructions and errors are shown in Fig. 2. The results show that the methodology is good to about a 1% error at 80% bandwidth, a level good enough for a causality checker. Reconstruction errors at the bandwidth limits are normal and ignored.

Using the Causality Checker

This section demonstrates a few modeling and extraction issues that can be clarified and/or fixed through the use of a causality

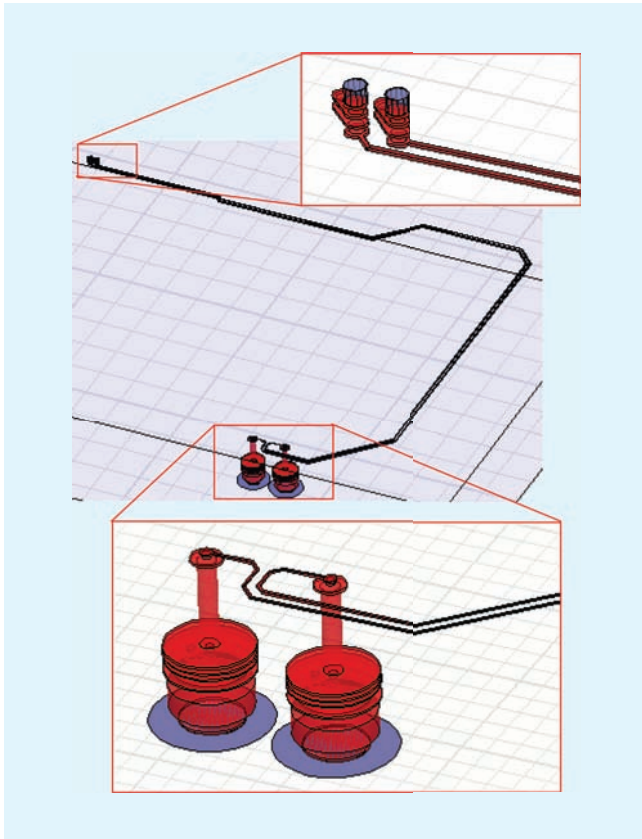


Fig. 3. Package differential pair for extraction studies.

checker. The examples are based on multiple 3D EM extractions of an organic package differential pair or coupled pairs, where the single pair is shown in Fig. 3. In the first extraction, the vendor-supplied dielectric constant and loss tangent at a list of frequency points are used. Fig. 4(a) shows the magnitude of S_{11} of one trace, where it can be readily identified that something is wrong from the unrealistic behavior above 25 GHz. The causality checker is applied to the data, with the results plotted in Fig. 4(b) showing very high reconstruction error not only at the problematic high frequencies but also at midrange frequencies where the data show no obvious problems.

The extraction is re-run with the vendor-supplied dielectric constant data augmented by an additional data point to eliminate the non-physical behavior above 25 GHz, and the results are shown in Fig. 5(a). The results are quite plausible, but are the data completely fixed, reliable, and usable? The causality check in Fig. 5(b) shows much improvement, but the errors are still quite high, indicating that the results are not yet good enough for use even though they appear good from visual inspection.

It is known that small sets of tabulated dielectric constant and loss tangent data are generally incapable of supporting causal modeling. One causal dielectric model is described in [8], the Djordjevic-Sarkar or D-S model. The 3D EM extraction is repeated with the causal D-S model, and the results are shown in Fig. 6, where just the combined data and causality check are shown. The causality error is greatly improved at all frequencies. Around 0.1 GHz, the error rises as the magnitude becomes very small, so the causality error is inconsequential. At frequencies above 30 GHz, the error increases, highlighting the fact that the data is aliased above

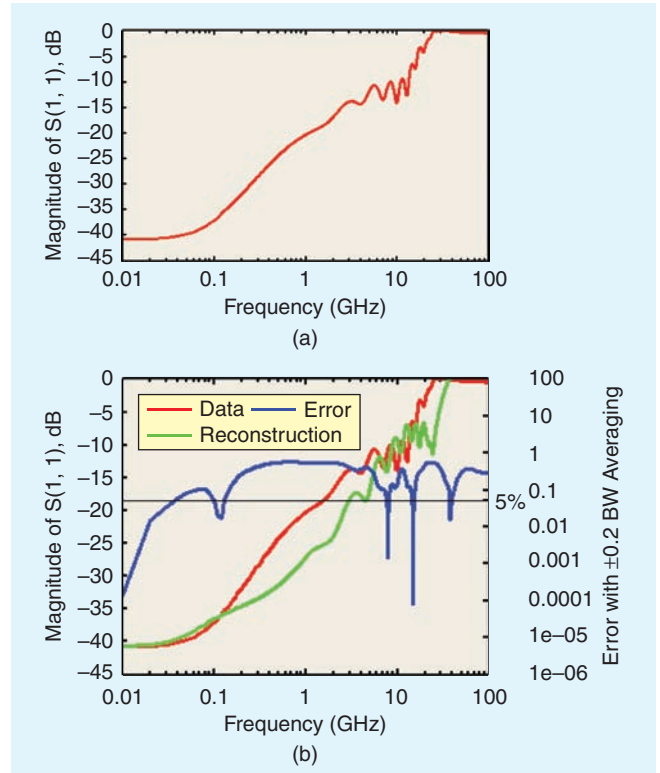


Fig. 4. 3D EM extraction of a package trace in an organic flip chip ball grid array package showing suspicious results. (a) magnitude and (b) magnitude reconstruction and reconstruction error.

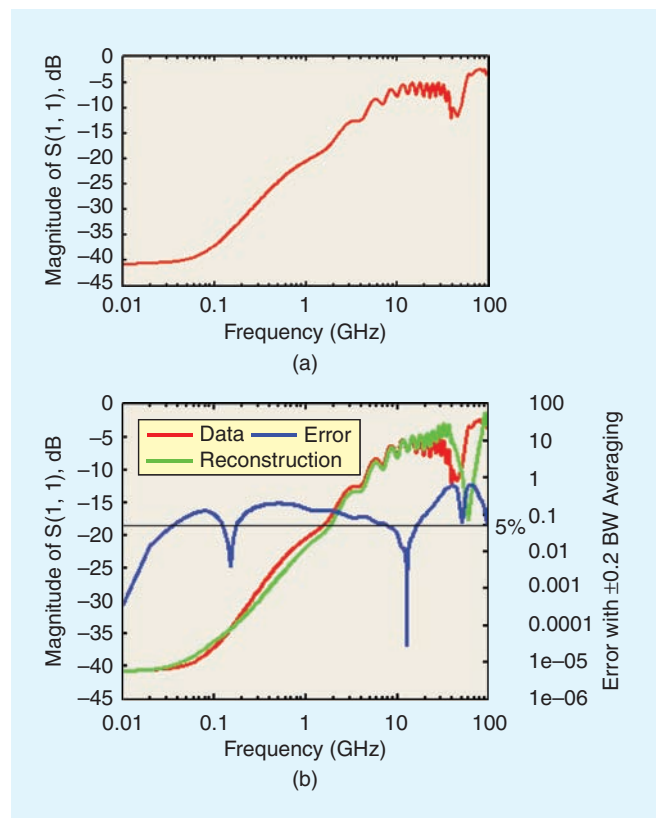


Fig. 5. The package extraction from Fig. 4 is repeated with an additional data point describing the properties of the dielectrics. (a) magnitude and (b) magnitude reconstruction and reconstruction error.

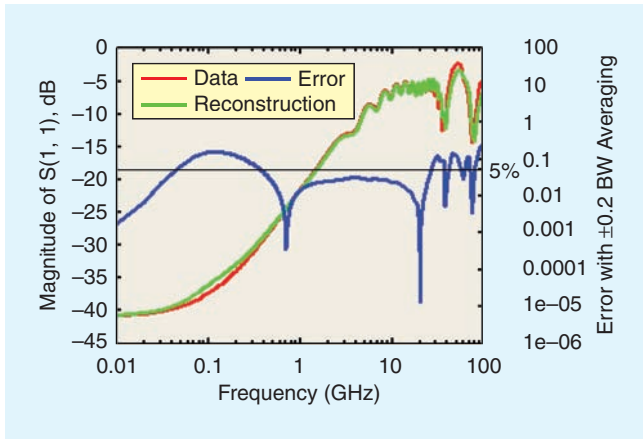


Fig. 6. The package extraction from Fig. 4 is repeated using the causal Djordjević-Sarkar dielectric model.

40 GHz, where the linear frequency spacing increases from 10 MHz to 5 GHz steps.

Data depopulation can be systematically explored using a causality checker [9][10]. Continuing the examination of the example data set computed with the D-S dielectric model, S_{31}

is shown in Fig. 7 with the full data density and progressively depopulated data along with causality checks. The error progressively increases with depopulation, enabling the modeler to select the smallest data set consistent with a given causality error. The full data set is highly over-sampled with 10 MHz linear sampling steps, while sampling at 500 MHz intervals greatly reduces the size of the data set while maintaining the causality error to about 5%. Depopulation at 1000 MHz intervals is clearly too sparse. Bandwidth can similarly be explored with a causality checker, with an example shown in Fig. 8.

A strategy for finding a minimum number of data points to model a good, wide-band interconnect is developed in [10]. To achieve a 5% causality error, the algorithm is

- Calculate $\Delta f_{\max} = 1/(8t_d)$
- Use $1.1 \times \log$ frequency spacing until $\Delta f \geq \Delta f_{\max}$
- Then switch to linear spacing using Δf_{\max}
- Set f_{\max} after -30 dB rolloff if causality check is used to validate data

where t_d is the interconnect delay, Δf_{\max} is the high-frequency linear sampling interval, and f_{\max} is the maximum model bandwidth. Applying the algorithm to depopulate the example data enables a 35X reduction in the size of the original data set, with the before-and-after results shown in Fig. 9.

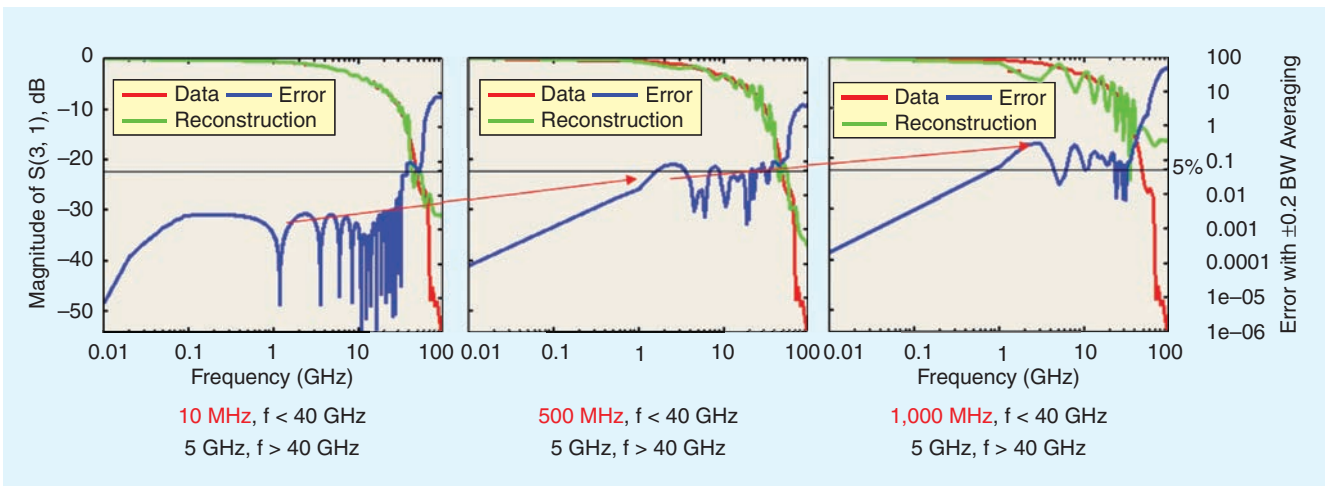


Fig. 7. Progressively higher data depopulation leads to higher causality errors. Linear sampling rates are shown.

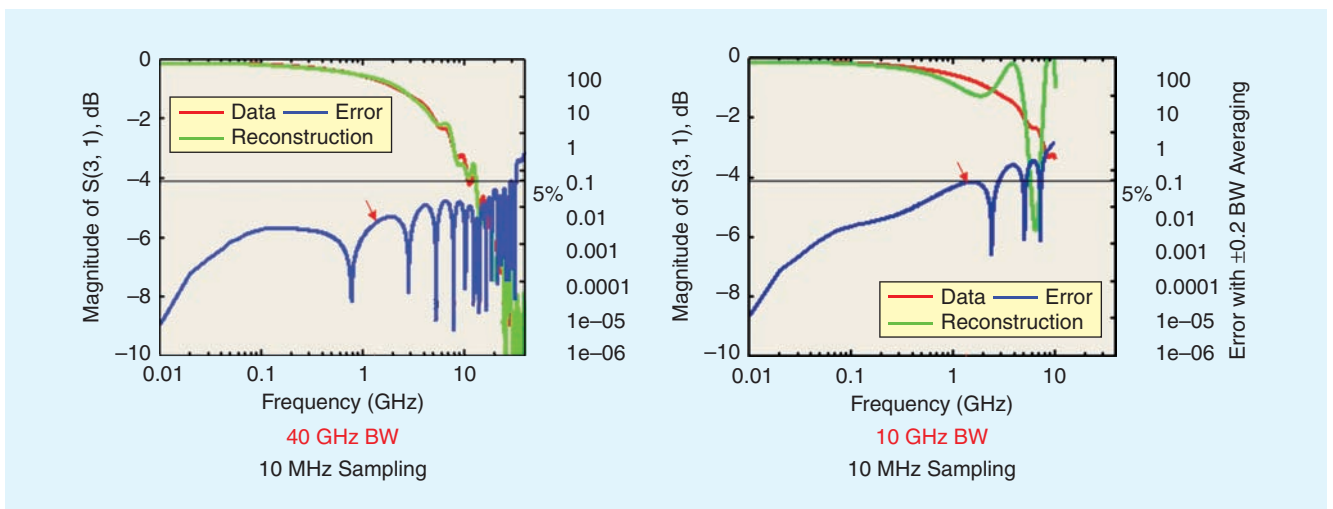


Fig. 8. Bandwidth reduction leads to higher causality errors.

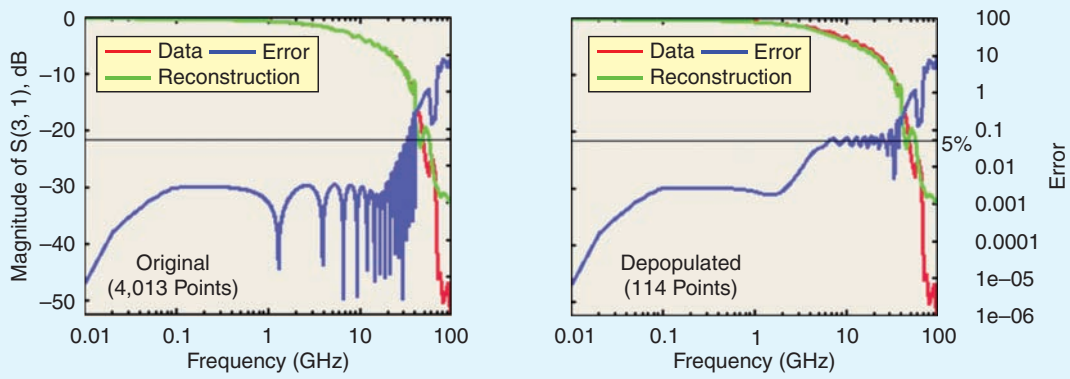


Fig. 9. Data depopulation using a systematic strategy based on causality checking enables a large reduction in data density with controlled increase in causality error. Note that rolling bandwidth averaging is not used in these plots.

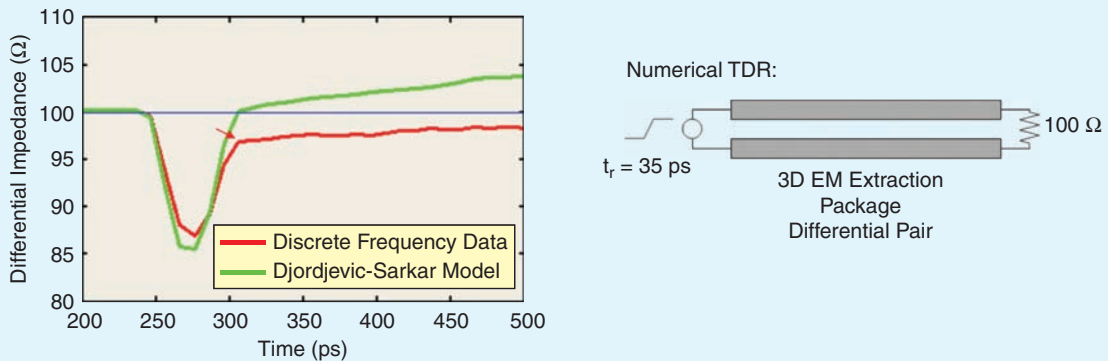


Fig. 10. Simulated TDR for a differential pair computed with two different models for the package materials.

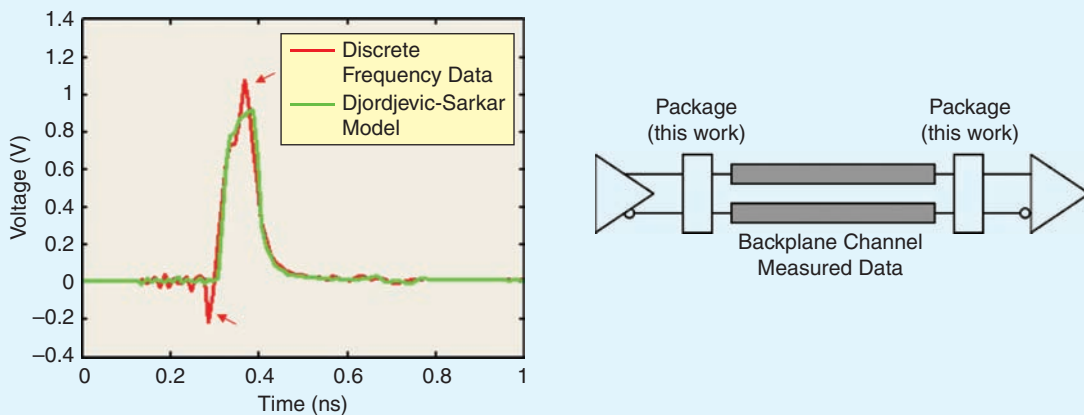


Fig. 11. SerDes channel impulse response computed for two different models for the package materials.

Time-domain simulations are strongly affected by the level of causality of the interconnect data. Fig. 10 shows a differential time-domain reflectometry (TDR) simulation using the non-causal S-parameter data set from the simulations for Fig. 4 vs. the causal data set using the D-S model from Fig. 5. The trace starts at about 310 ps as indicated by the red arrow. Measurements and 2D EM extraction show that the impedance should be 100 Ω. The non-causal data causes several Ohms of error in the simulated trace impedance.

The negative impact of non-causal data is further demonstrated in Fig. 11 using the same data sets as Fig. 10 to calculate the impulse response of the interconnect including the backplane. The non-causal data exhibits a large undershoot preceding the actual rise in the data and a similar overshoot before the fall. These flaws are not observed in the results using the D-S model. Note that the package models have the same bandwidth and data density and that the same backplane data is used for both impulse response calculations.

Conclusion

The implementation details of a simple causality checker are reviewed, and the checker is used to demonstrate that it can effectively identify flawed extraction data, weak material sets, and under-sampled data. The causality checker is used to derive an algorithm for selecting sampling rates and bandwidth for EM extractions of good interconnects, enabling a potentially large reduction in data points and run time. Improved extraction data is shown to significantly improve S-parameter data, time domain modeling accuracy, and time-domain system-level channel simulations.

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Biographies



Brian Young received the BSEE from Texas A&M University in 1984, the MSEE from the University of Illinois in 1985, and the Ph.D. from the University of Texas in 1987. He taught electromagnetics and microwaves at Texas A&M University before moving to Hughes Aircraft to design microwave circuits and packaging for transmit/receive modules for phased array radar.

He then transitioned to Motorola to develop modeling, simulation and characterization techniques for digital packaging. This was followed by LVCMOS, LVDS, and HSTL IO circuit design at Motorola and Texas Instruments. In 2005, he started a new signal and power integrity group at Texas Instruments to ensure the successful integration of high-performance ASICs, and he now also manages the package design team in the ASIC product group. He was an Associate Editor for the IEEE Transactions on Advanced Packaging from 2001 to 2003. He is on the technical program committee for the IEEE Conference on Electrical Performance of Electronic Packaging and Systems, and he is the conference co-chair for 2011–2012. He is the author of the book "Digital Signal Integrity: Modeling and Simulation with Interconnects and Packages" and has authored or co-authored 33 papers and conference publications, and he holds eight patents. He is a registered professional engineer in the state of Texas.



Amarjit S. Bhandal graduated from the University of Southampton in 1987; since that time, he has been in continuous employment in the electronics or automotive industries. For the last 15 years he has been with Texas Instruments where he is currently a Member of Group Technical Staff. Amarjit is a specialist in the electrical analysis and design of custom packages for application specific devices.

His areas of expertise encompass the modelling and design of packaging interconnects for high speed signalling. During his career, Amarjit has published technical papers at several conferences and is also the holder of seven patent awards.

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