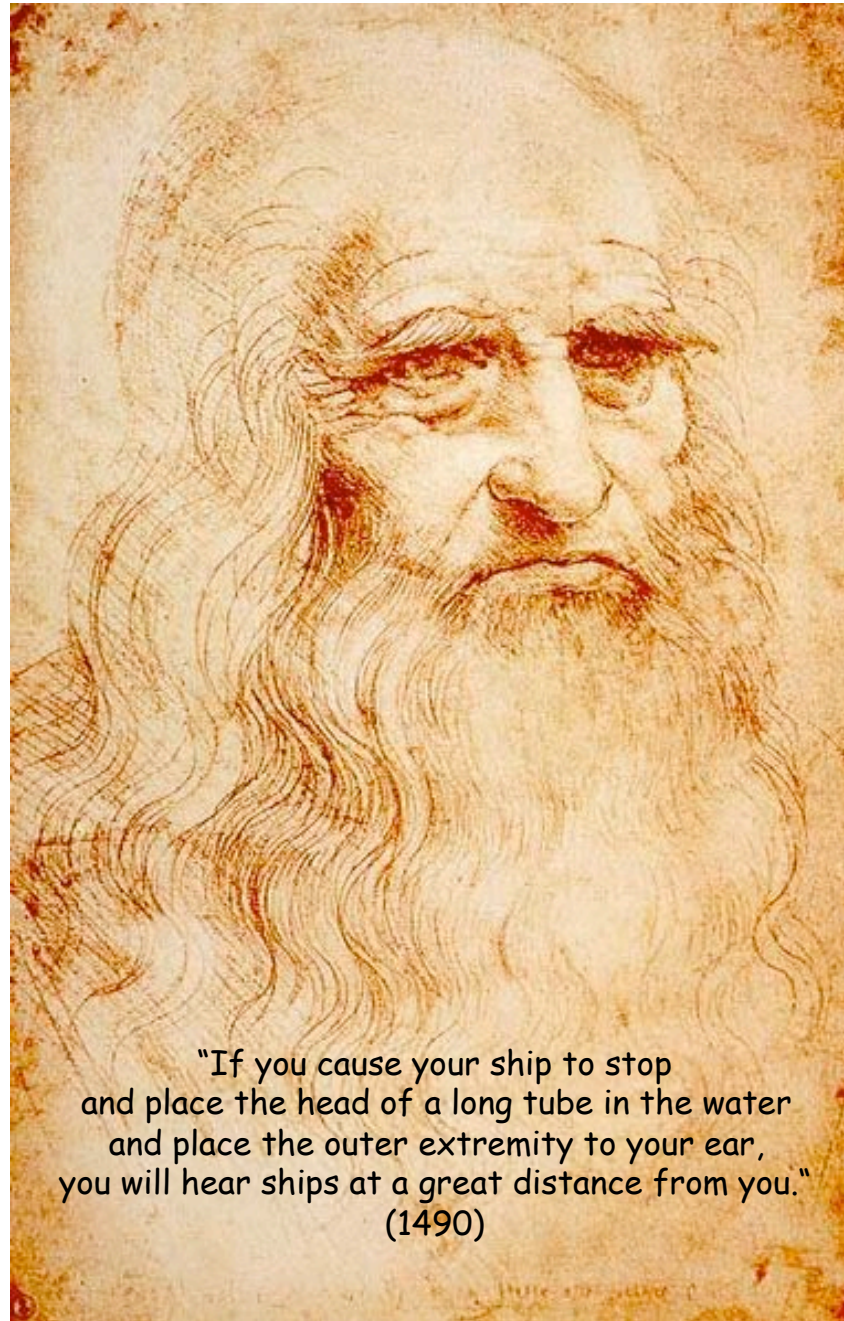




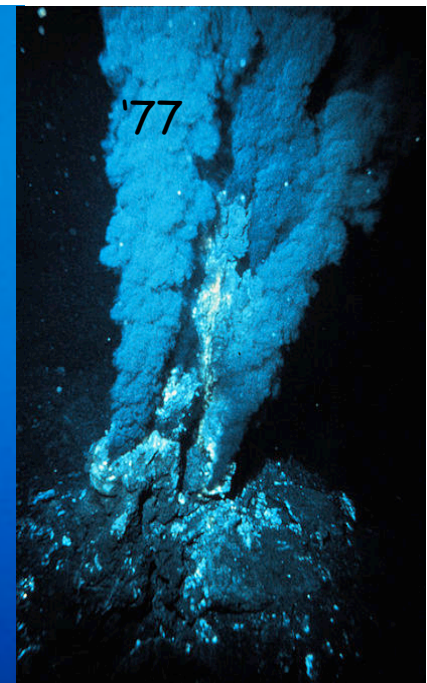
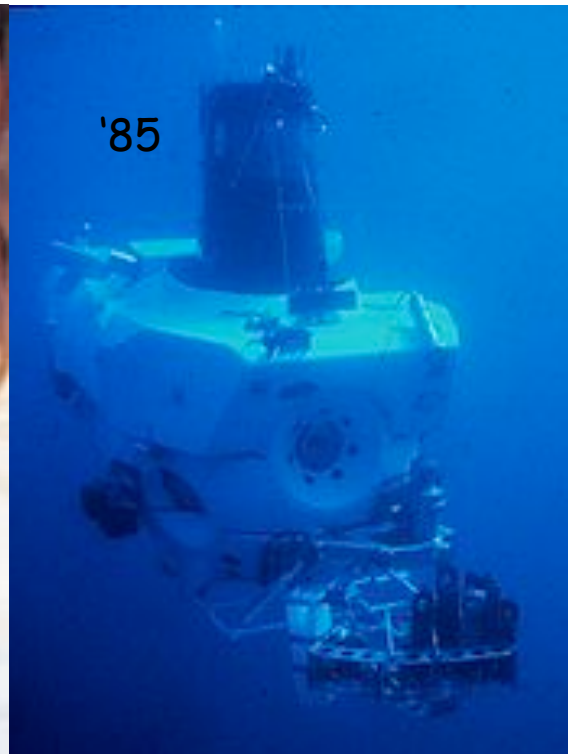
**Signal Processing  
for  
Underwater Communications**

Milica Stojanovic  
millitsa@ece.neu.edu



"If you cause your ship to stop  
and place the head of a long tube in the water  
and place the outer extremity to your ear,  
you will hear ships at a great distance from you."  
(1490)





## Underwater wireless communications

### Why?

Major scientific discoveries: cabled submersibles

Cables are heavy, expensive, restrict motion (but offer high bandwidth)

Applications:

- ocean monitoring (climate, pollution, oil, fisheries, earthquakes,...)
- underwater exploration (marine archaeology, natural resources, ...)
- search and survey (shipwrecks, mines, area mapping,...)

### How?

Radio: ~100 Hz, very high attenuation (~m @ 10kHz)

Optical: short distances (<100m), pointing precision

Acoustical: a solution

### What has been done?

Underwater telephone (WW2, analog SSB 8-11 kHz)

DSP technology: acoustic modems (few kbps over few km)

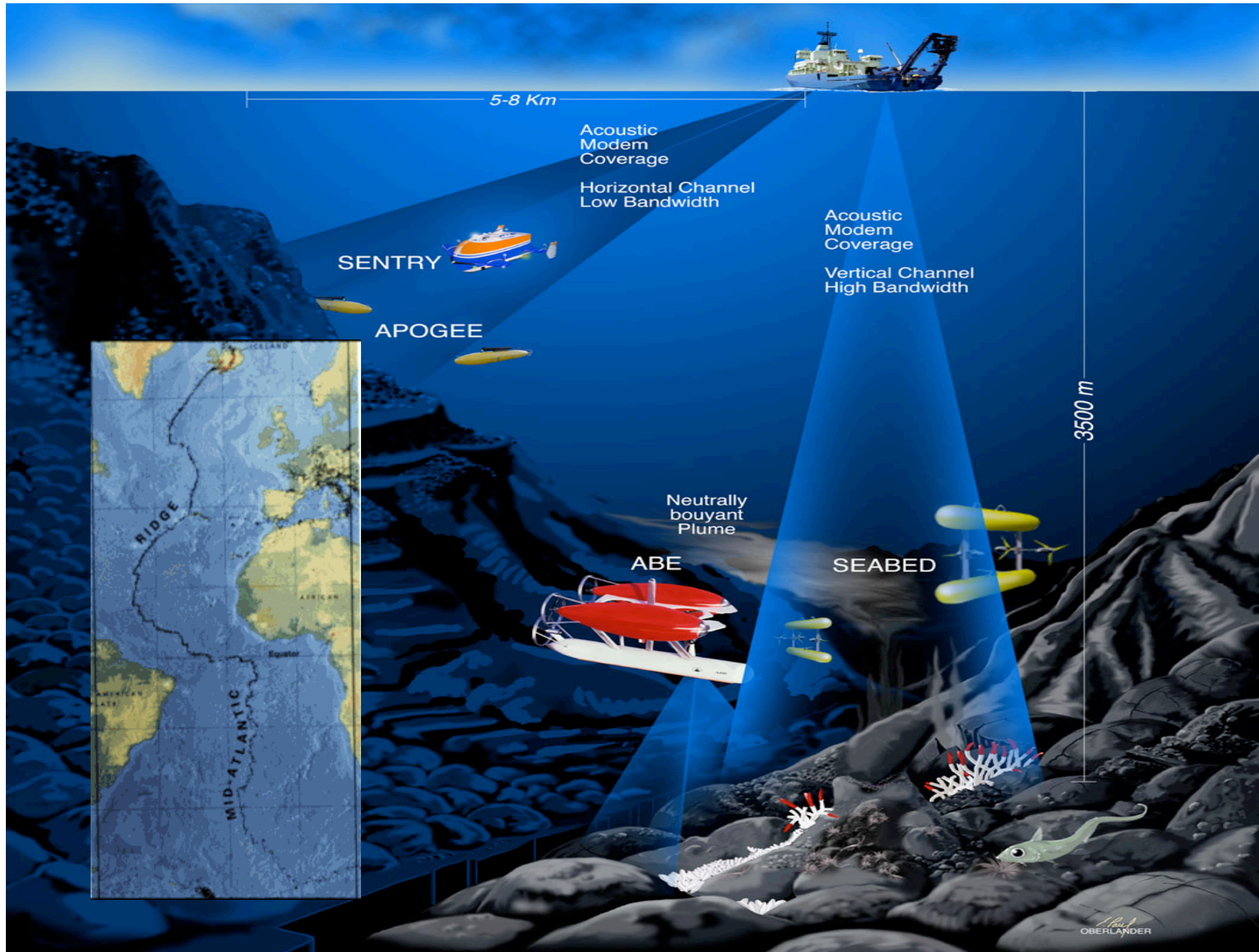
70's,80's: noncoherent mod/demod → commercially available

90's: bandwidth-efficient mod/demod → prototypes

### What is next?

More signal processing, networks.





## Overview

### communication channel

- attenuation and noise
- multipath propagation
- time-variability

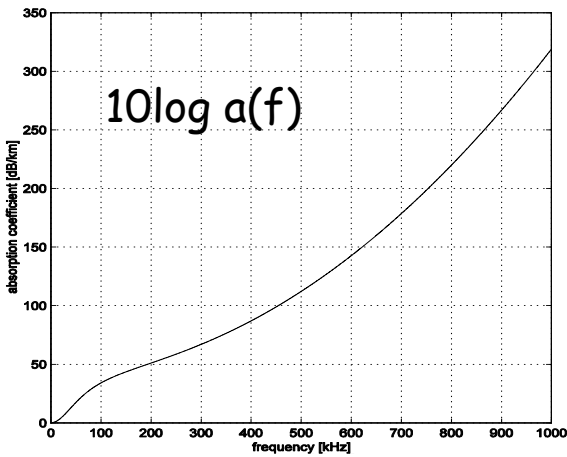
### signal processing

- single-carrier, multi-carrier
- single-user, multi-user (SIMO/MIMO)

### implications for networking

# Underwater acoustic channel: attenuation and noise

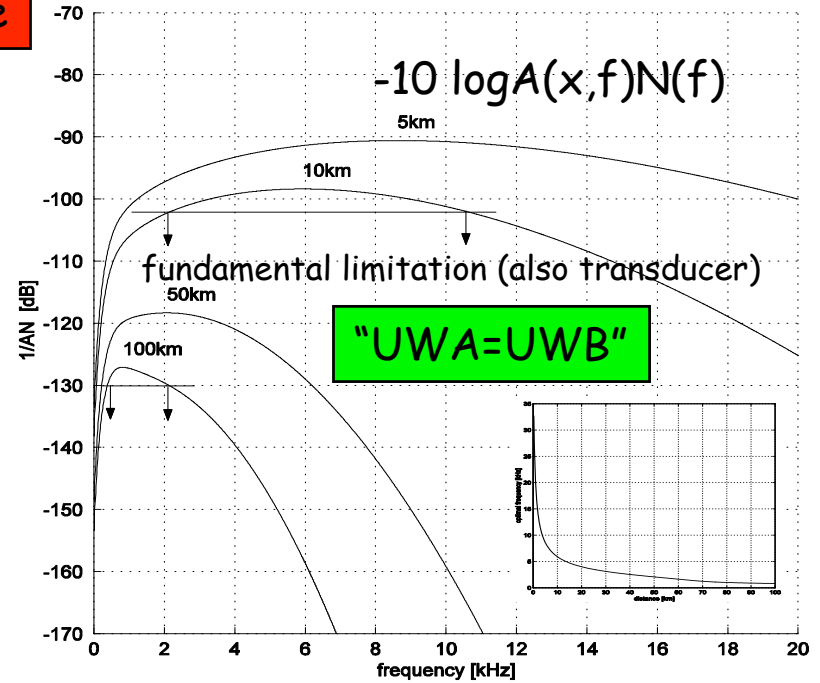
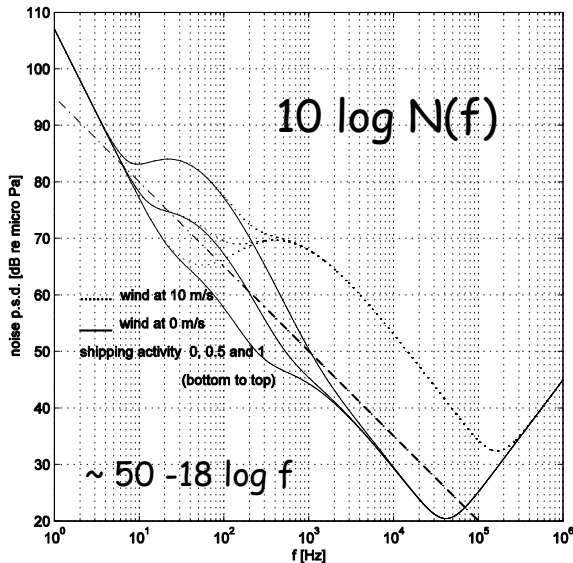
$A(x,f) \sim x^k a^x(f)$  spreading + absorption  
(k:1-2)



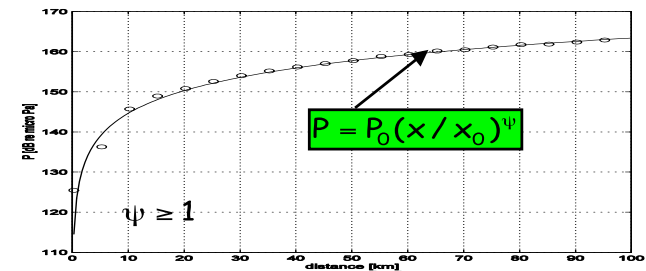
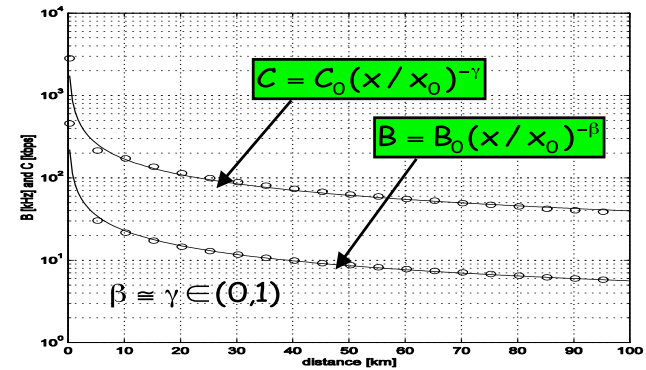
$$SNR = \frac{P_x}{P_{noise}} \sim \frac{P / A(x,f)}{N(f)\Delta f} \sim \frac{1}{A(x,f)N(f)}$$

$$10 \log a(f) = 0.11 f^2 / (1+f^2) + 44 f^2 / (4100+f^2) + 0.000275 f^2 + 0.003 \text{ dB/km, for } f \text{ [kHz]}$$

noise = turbulence + shipping + surface + thermal + other  
 ↓  
 site-specific: man-made, biological, ice, rain, seismic

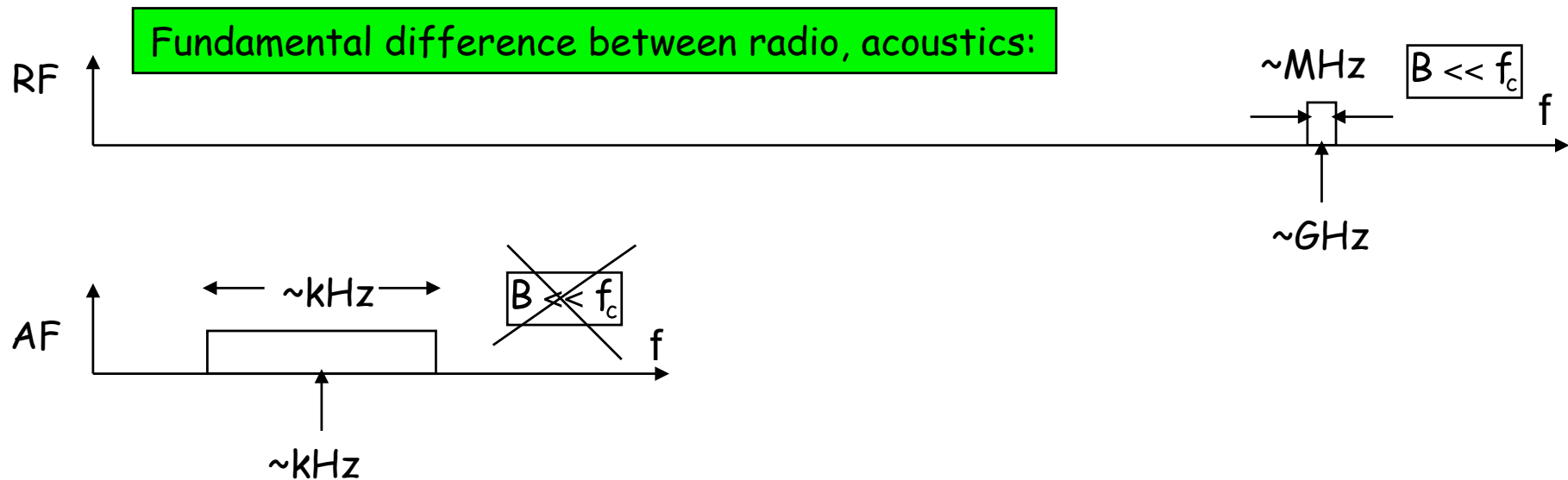


capacity, bandwidth, power: dependence on distance





A "high-rate" acoustic system is inherently wideband ("UWA=UWB")



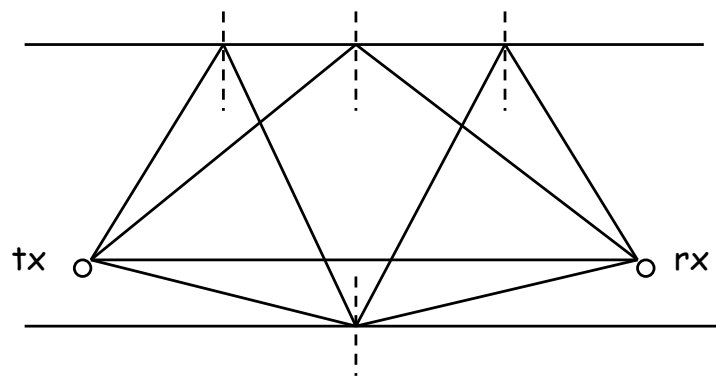
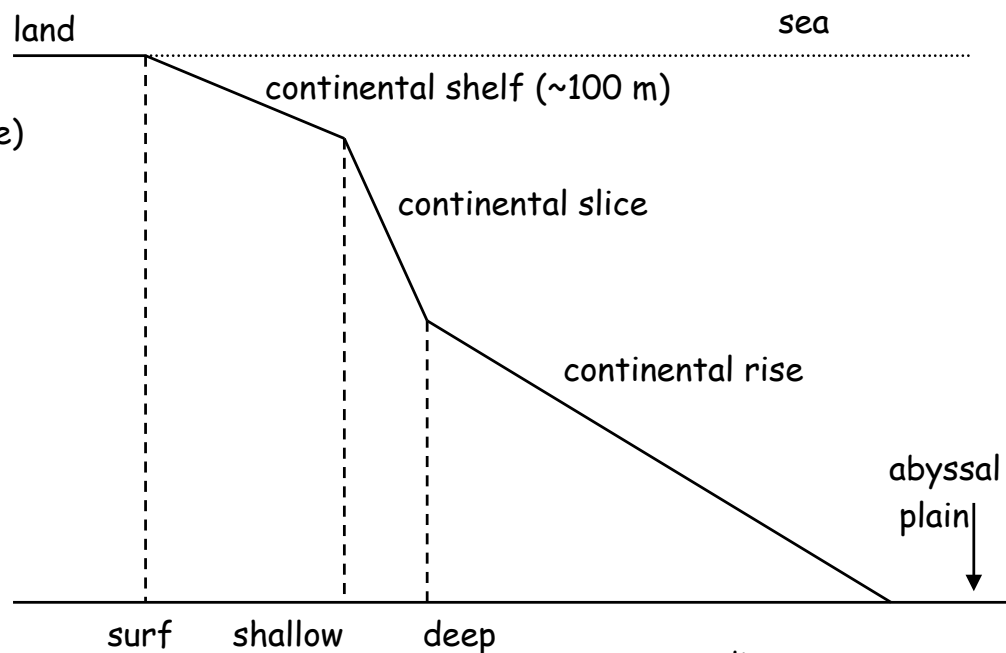
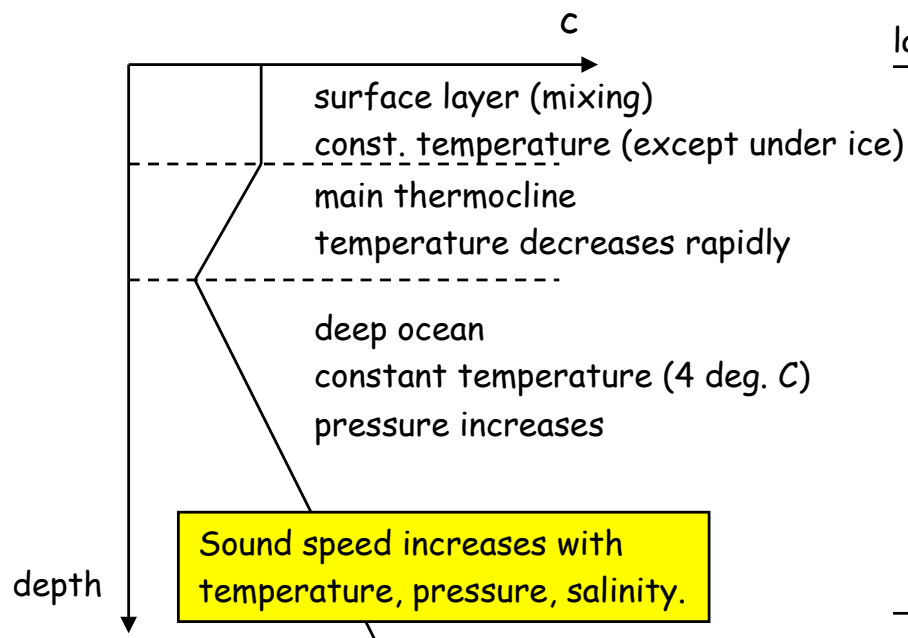
Absolute bandwidth may be "low," but it is **not** negligible w.r.t. center frequency (e.g. 1 kHz @ 1 kHz, 5 kHz @ 10 kHz, 20 kHz @ 30 kHz).

System is band-limited, narrowband assumption does **not** hold.

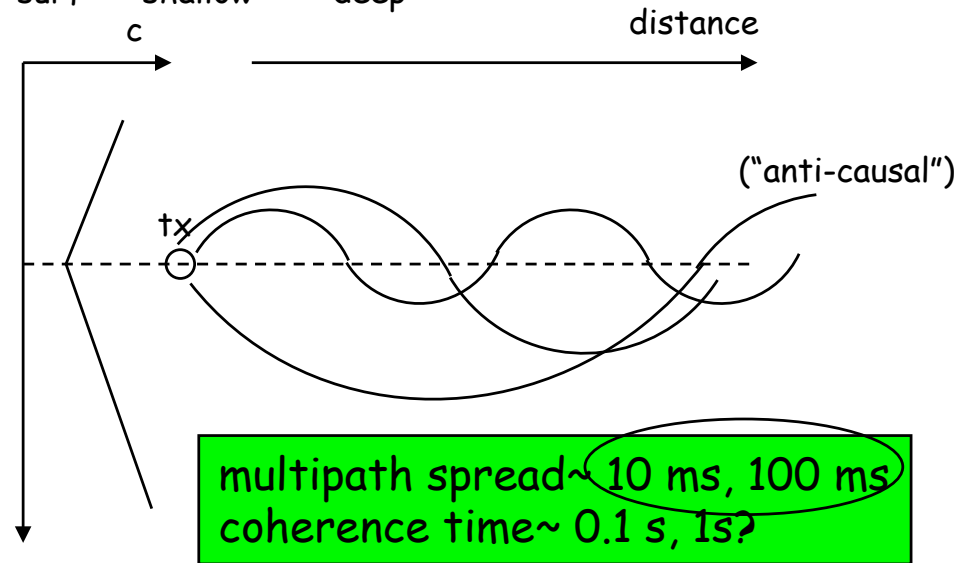
Implications :

- need bandwidth efficient modulation methods (coherent detection)
- cannot use signal processing methods that rely on narrowband assumption (array processing, synchronization)

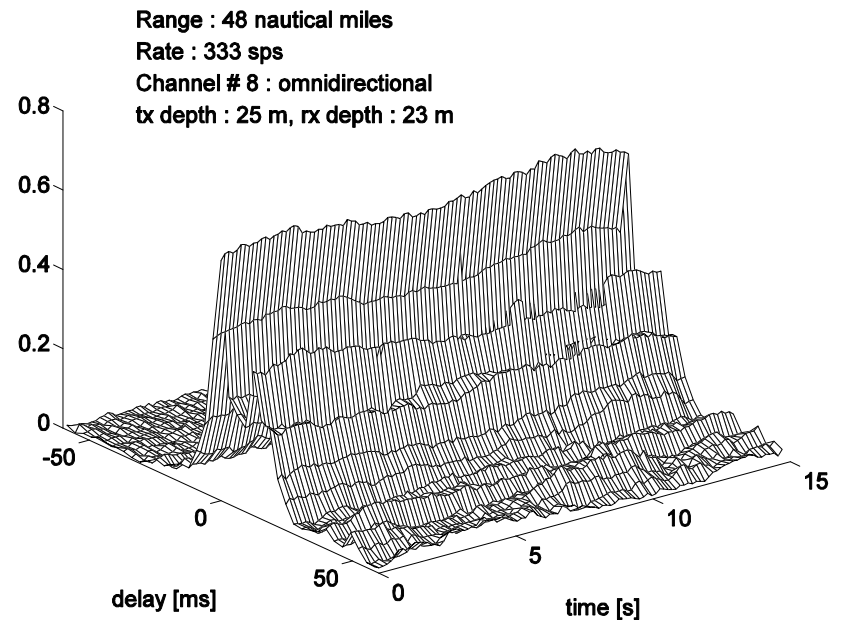
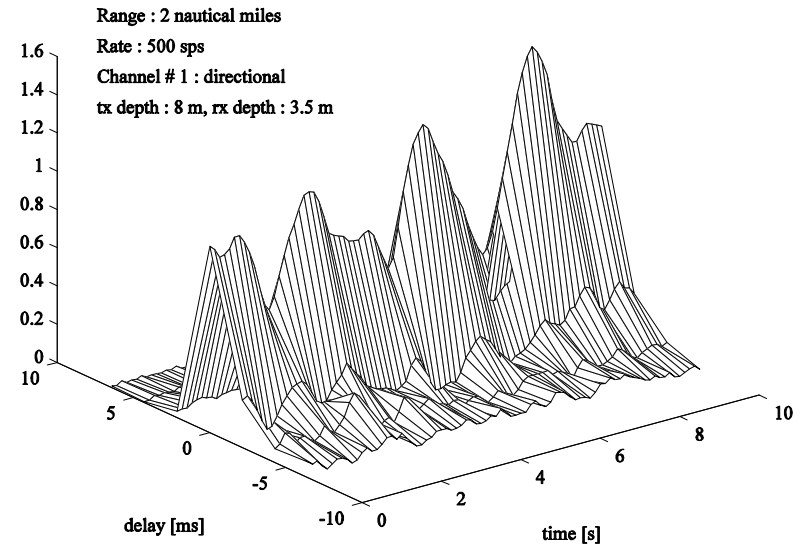
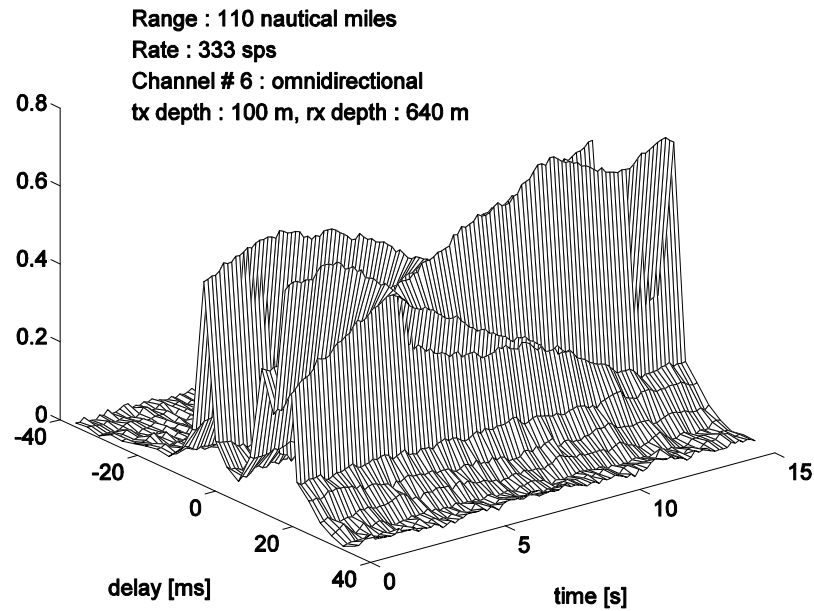
# Underwater acoustic channel: multipath and time-variability



Channel variation: large/small scale  $\rightarrow$  surface motion, internal waves, turbulence, fine changes in the sound speed profile.



## Examples: measured channel responses

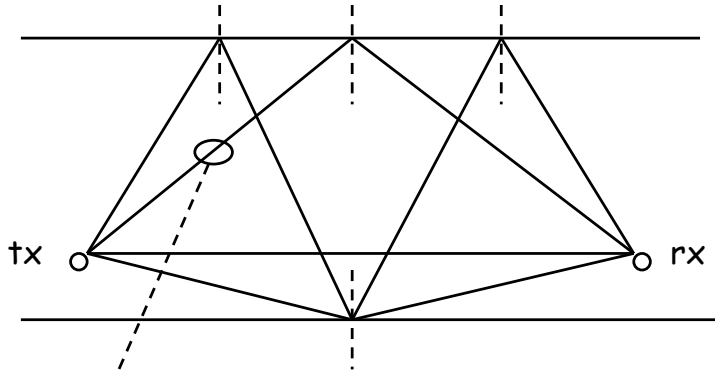


There are no widely accepted statistical channel models.



# Channel modeling (for signal processing)

## (1) time-invariant channel



Each path:

- length, delay
- propagation loss  $A$
- reflection coefficient  $\Gamma$

$$\bar{H}_p(f) = \frac{\Gamma_p}{\sqrt{A(l_p, f)}} \leftrightarrow \bar{h}_p(\tau)$$

Each path in an acoustic channel acts as a (low-pass) filter.

$$\bar{H}(f) = \sum_p \bar{H}_p(f) e^{-j2\pi f \tau_p} \leftrightarrow \bar{h}(\tau) = \sum_p \bar{h}_p(\tau - \tau_p) \approx \sum_p \bar{h}_p \cdot \bar{h}_o(\tau - \tau_p) \neq \sum_p \bar{h}_p \cdot \delta(\tau - \tau_p)$$

path filters: same shape, different gain

## (2) time-variation

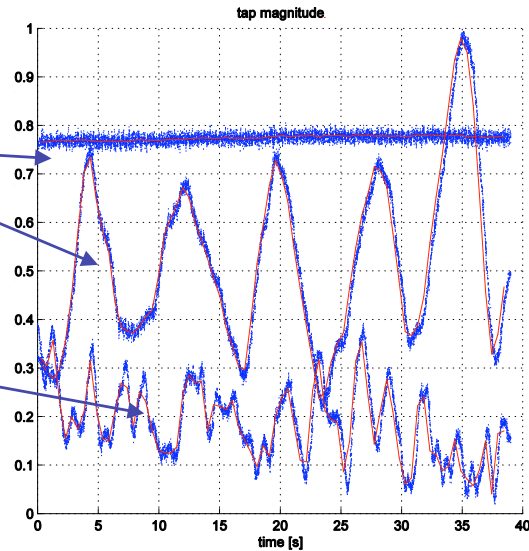
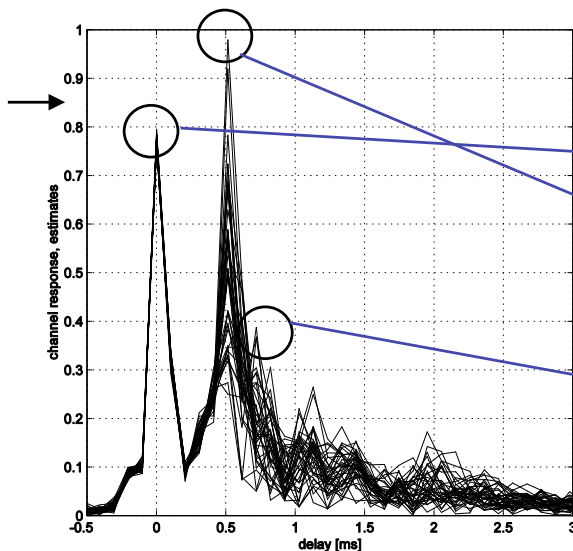
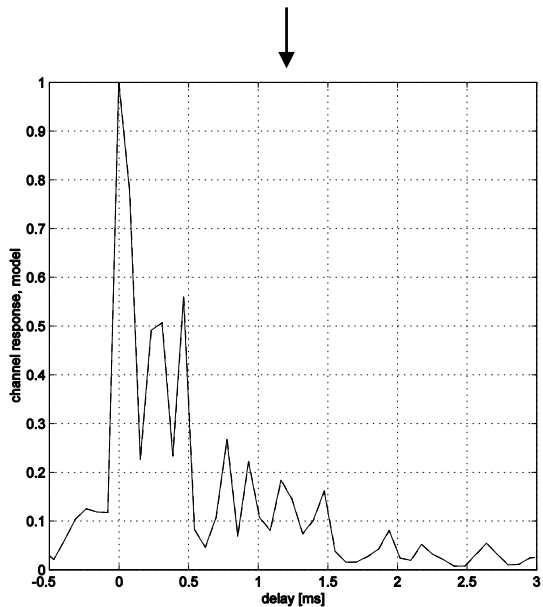
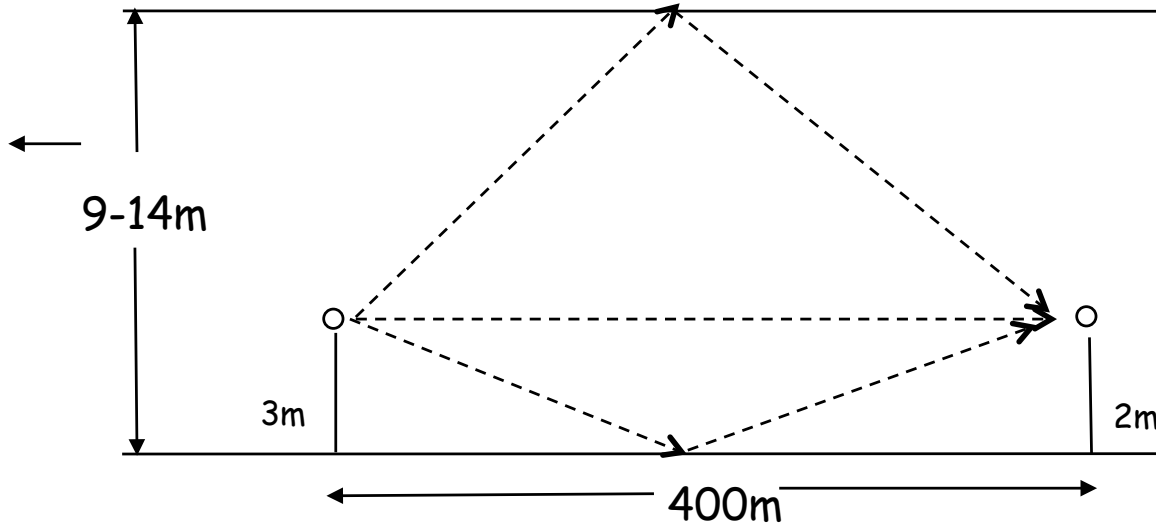
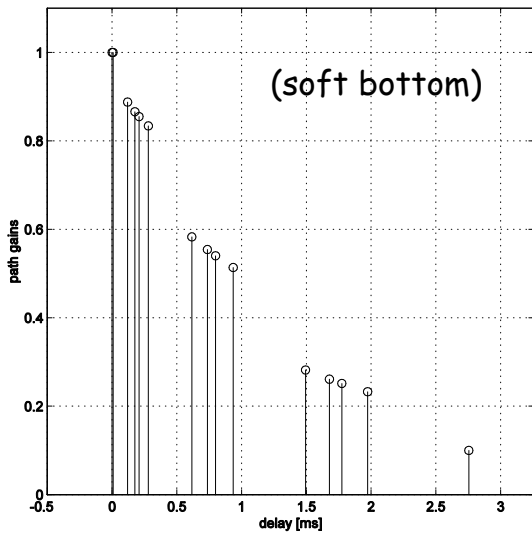
$$\bar{h}(\tau) \rightarrow h(\tau, t) \approx \sum_p \bar{h}_p(t) \cdot \bar{h}_o(\tau - \tau_p(t))$$

time variation: inherent, motion-induced (random, deterministic/unknown)

# Example

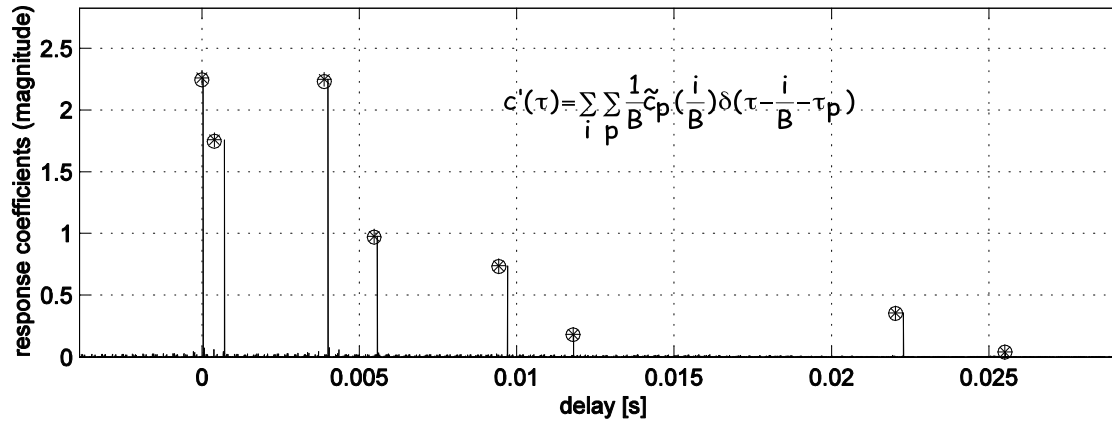
Narragansett Bay, March 2008

8-18 kHz



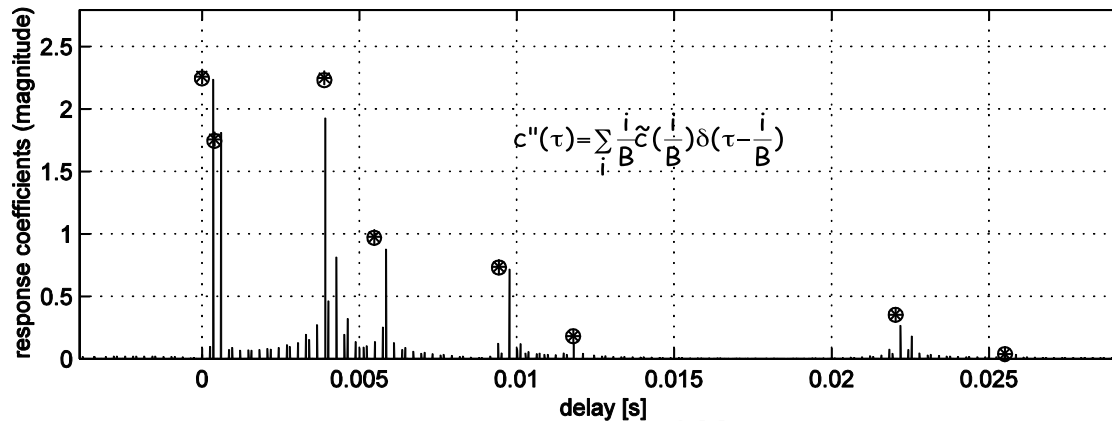
(no motion of tx/rx)

# Equivalent band-limited baseband discrete-path models



non-uniform  
tap spacing

tx/rx: 1 km / 75 m  
fc=10 kHz, B=5 kHz



uniform  
tap spacing

30 ms @ 5 ksps =  
150 symbols.

## Implications:

- reduce complexity and noise via **sparse** channel estimation.
- greater B → longer response (# symbols), but better resolution in both time and delay.

win-win 😊

...respect the physics of the channel, and ...



# Motion-induced time-variation: the Doppler effect

$$\begin{aligned} t &\rightarrow t+at \\ f &\rightarrow f+af \end{aligned}$$

time dilation/compression  
frequency offset

$$a=v/c$$

$v \sim \text{m/s}$   $\longrightarrow$  with or without intentional motion  
 $c=1500 \text{ m/s}$   
 $a \sim 10^{-4}$   $\longrightarrow$  comparable only to LEO satellite systems

Implications: explicit synchronization is necessary.

Time variation:

- inherent  $\rightarrow$  Doppler spreading
- motion-induced  $\rightarrow$  Doppler shifting (and spreading)

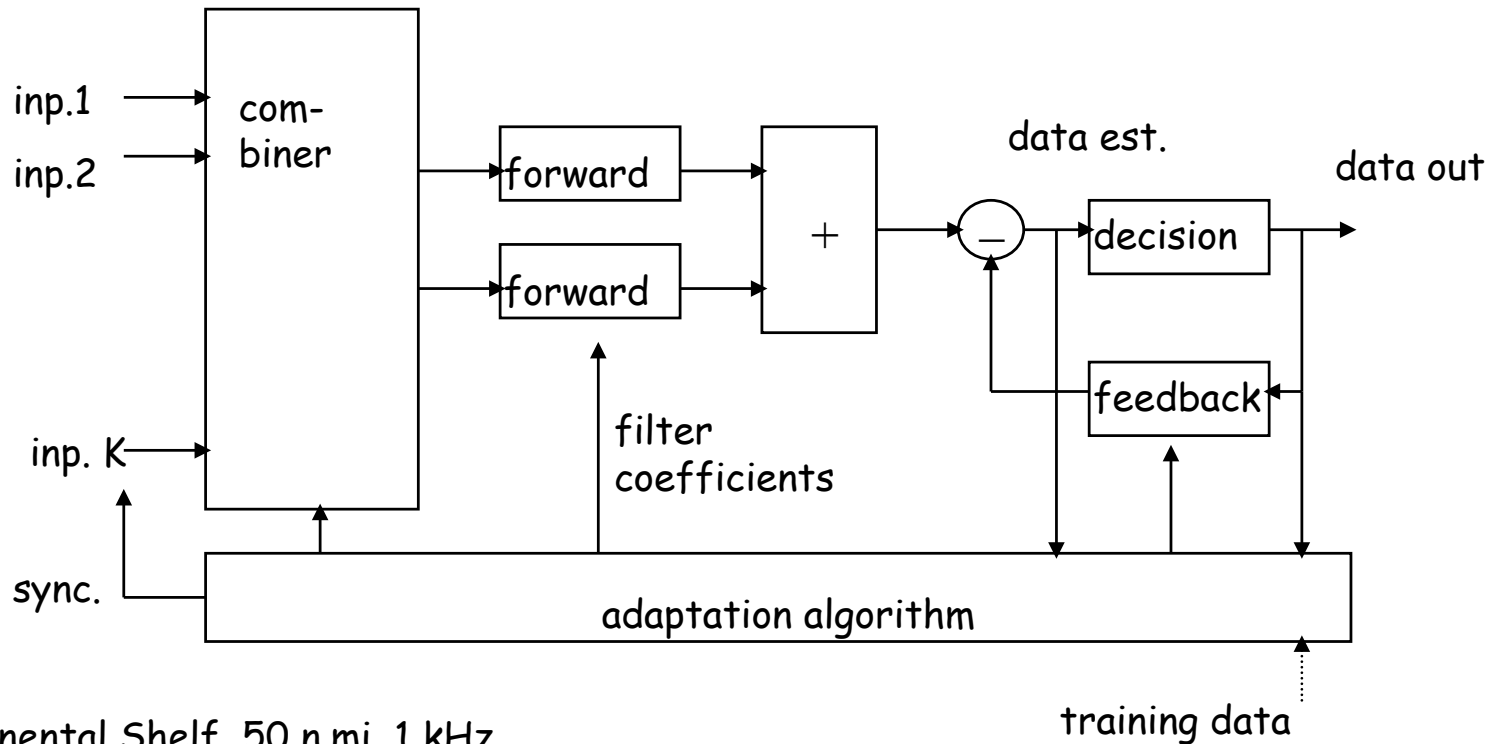
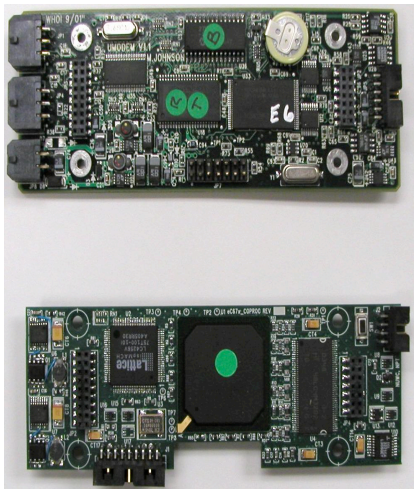
adaptive channel estimation (slow)

synchronization (fast)

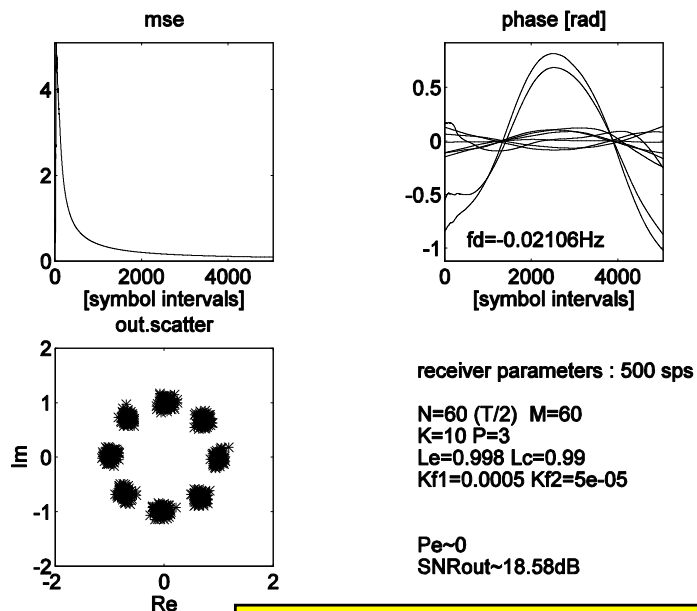
tacking  $\theta(t)$  vs.  $e^{j\theta(t)}$

...respect the physics of thy channel ...

# Single-carrier systems



Ex. New England Continental Shelf, 50 n.mi, 1 kHz



"the faster the better"

## Current achievements:

### Point-to-point (2/4/8PSK; 8/16/64QAM)

- medium range (1 km-10 km ~ 10kbps)
- long range (10 km - 100 km ~ 1kbps)
- basin scale (3000 km ~ 10bps)
- vertical (10 m~150 kbps, 3 km~15 kbps, 10 km~5 kbps)



### Mobile communications

AUV to AUV at 5 kbps

### Multi-user communications

five users, ~ kbps in 5 kHz band



# CDMA underwater?

Conventional assumptions do not hold:

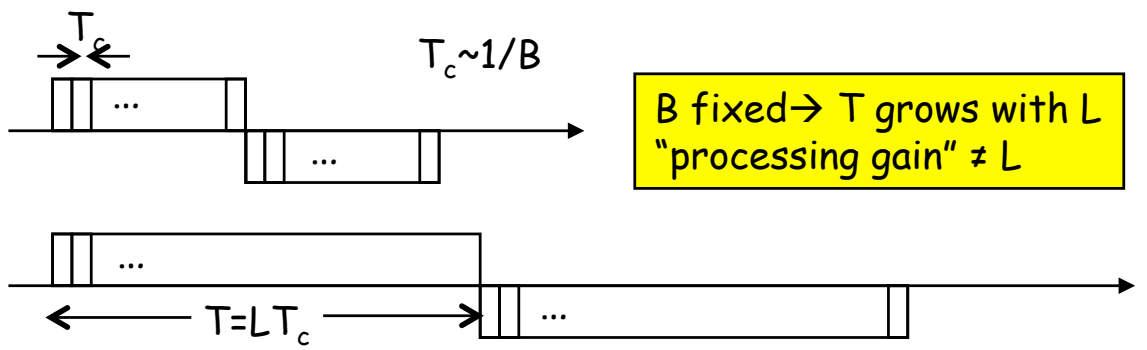
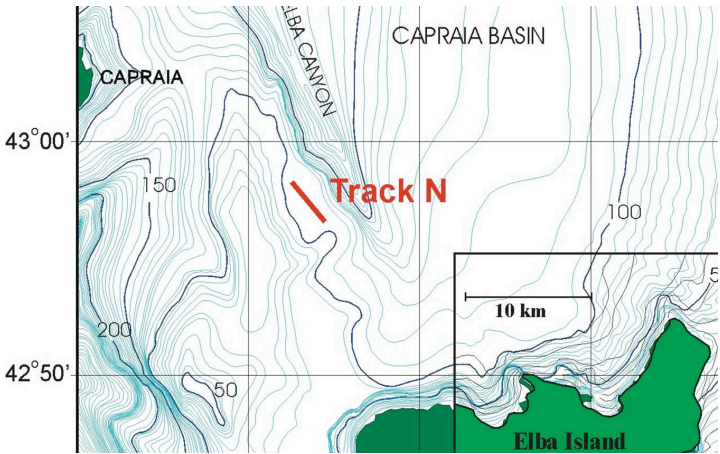
- ISI is not negligible
- channel is not constant over one symbol

Receiver design:

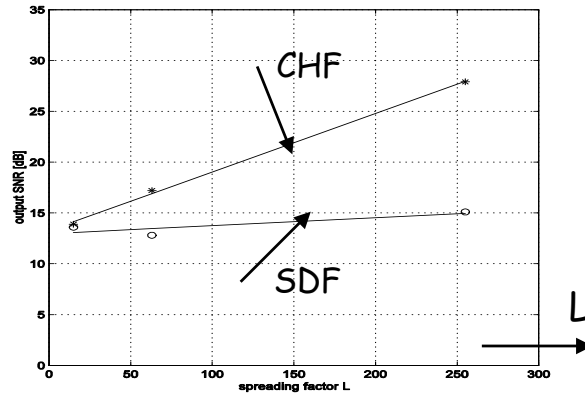
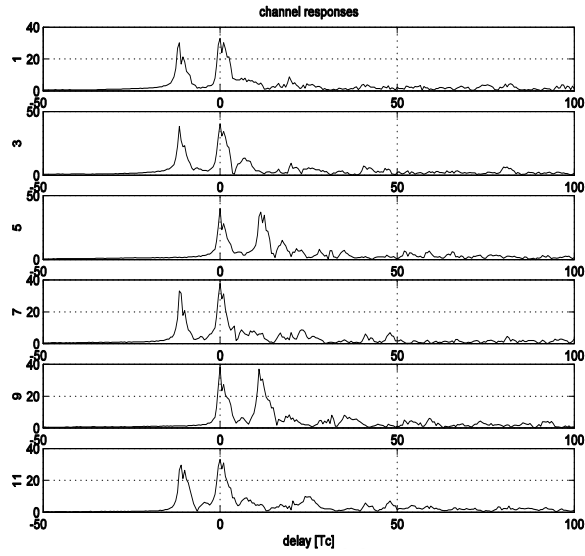
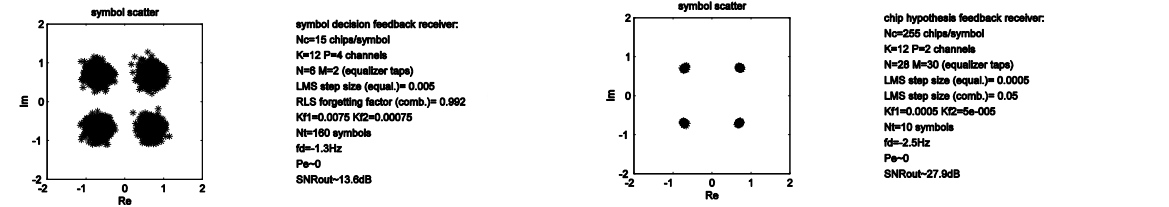
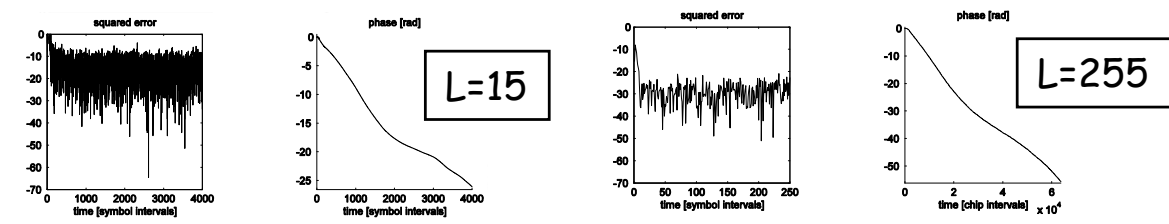
- chip-rate filtering
- chip-rate adaptation

Experiment:

- range: 2.5 km
- center frequency: 33 kHz
- chip rate: 19,200 chips/sec
- four users, up to 2.5 kbps
- spreading factor (15-255)



B fixed  $\rightarrow$  T grows with L  
"processing gain"  $\neq$  L



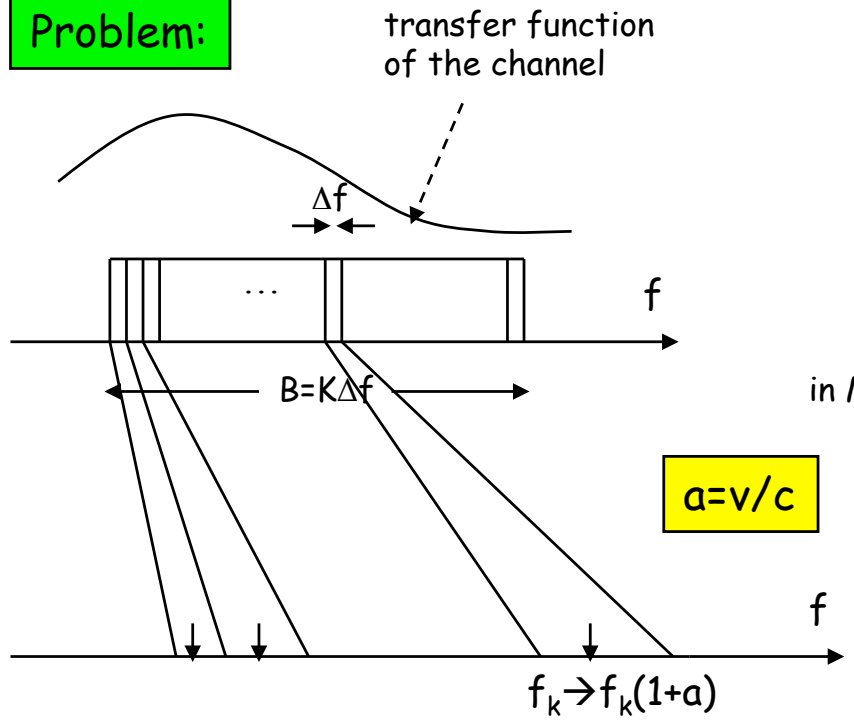
"chip hypothesis feedback" recovers processing gain.

Mobile experiments in 5 kHz band: direct sequence spread spectrum feasible at 15 knots.

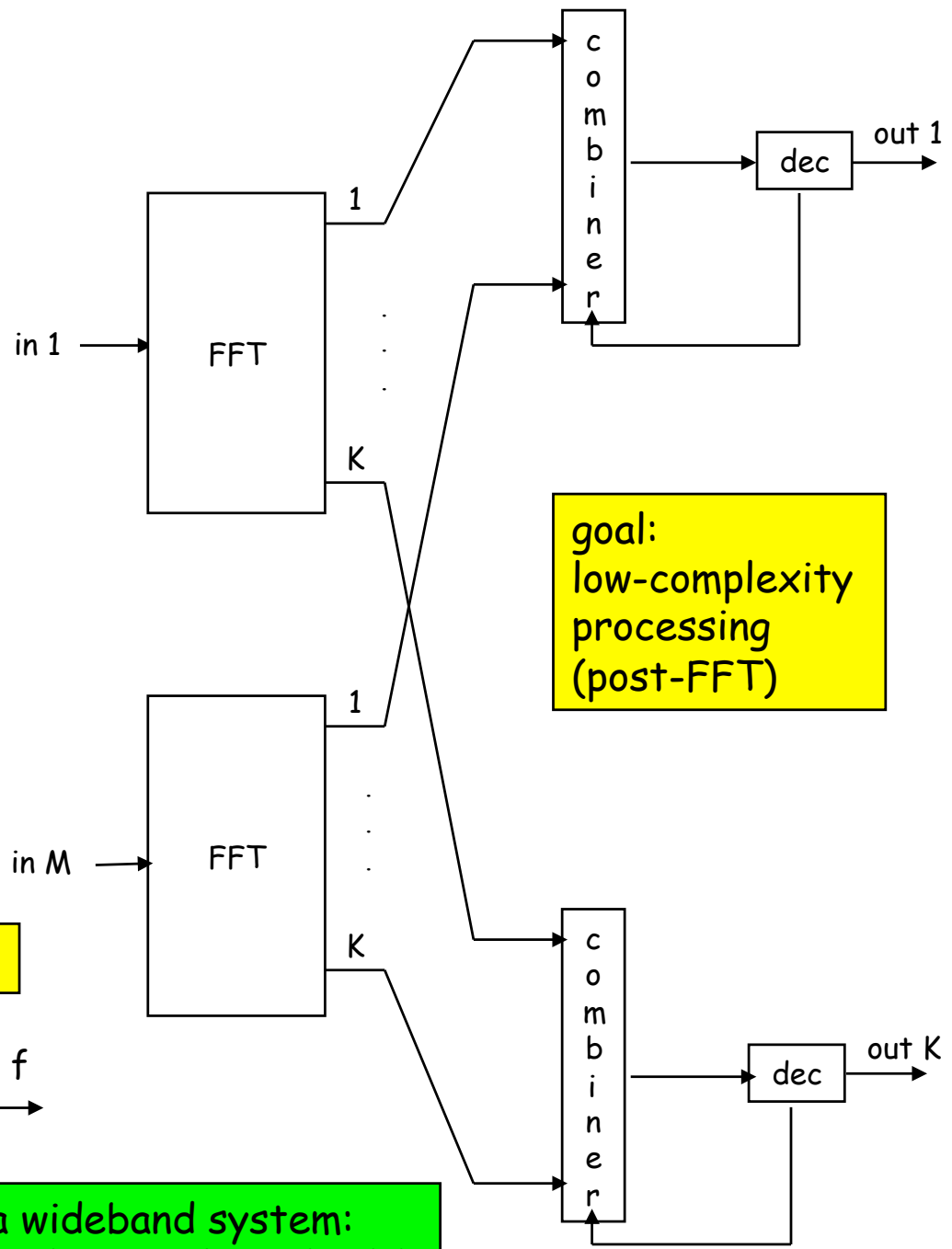
**Multi-carrier systems**

**OFDM:  
+equalization  
-frequency offset**

**Problem:**



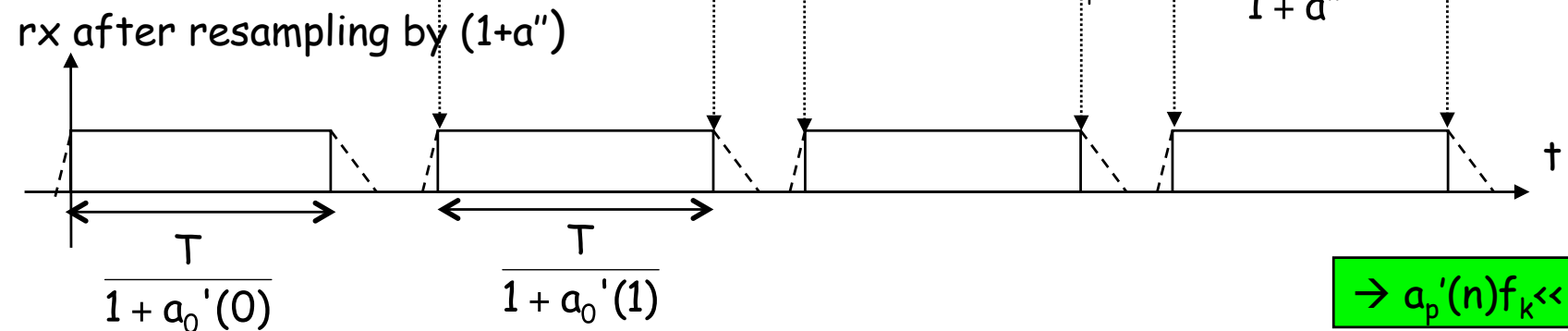
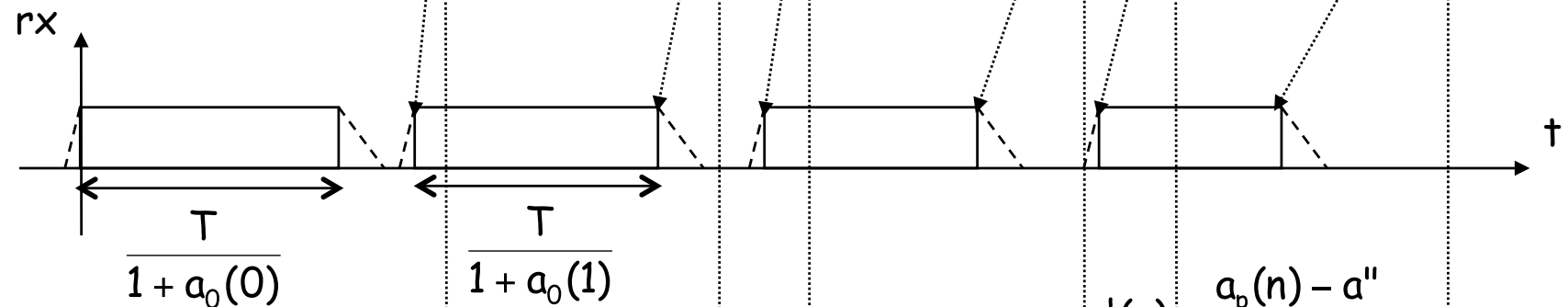
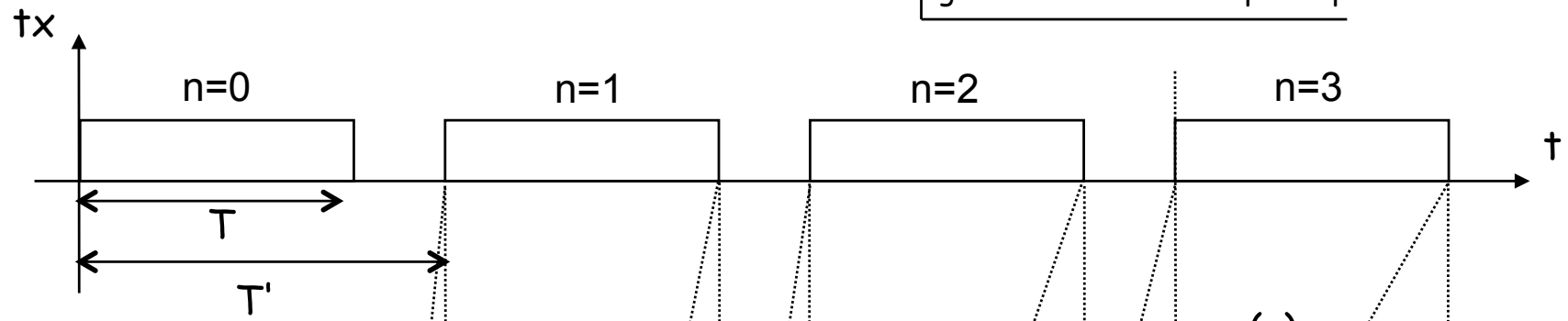
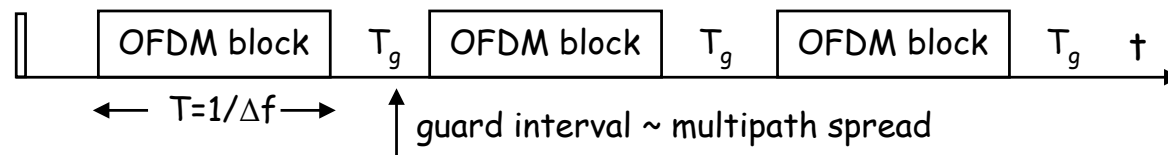
**Motion-induced Doppler distortion in a wideband system:  
non-uniform frequency shifting across the signal bandwidth**



**goal:  
low-complexity  
processing  
(post-FFT)**



Pre-processing  
(initial synchronization)



$$a_p'(n) = \frac{a_p(n) - a''}{1 + a''}$$

$\rightarrow a_p'(n)f_k \ll \Delta f$

**Trade-offs**

some numbers:  
 $T_{coh} \sim 0.1 \text{ ms}$ ;  $T_{mp} \sim 10 \text{ ms}$

$T=10 \text{ ms}$ ,  $B=10 \text{ kHz} \rightarrow K=100$   
 $T=50 \text{ ms}$ ,  $B=20 \text{ kHz} \rightarrow K=1000$

$$\frac{R}{B} = \frac{1}{1 + T_g B / K}$$

$\rightarrow$  want large  $K$   
 ... but this means small  $\Delta f$  / large  $T$ , i.e. more vulnerability to residual frequency offset / inherent time-variation

$\rightarrow$  "optimal" number of carriers: greatest for which post-FFT processing is still possible.

**Implications: have to estimate/track large number of phases.**

Buzzards Bay, 2.5 km, 24 kHz

**A simple approach to "Doppler" tracking**

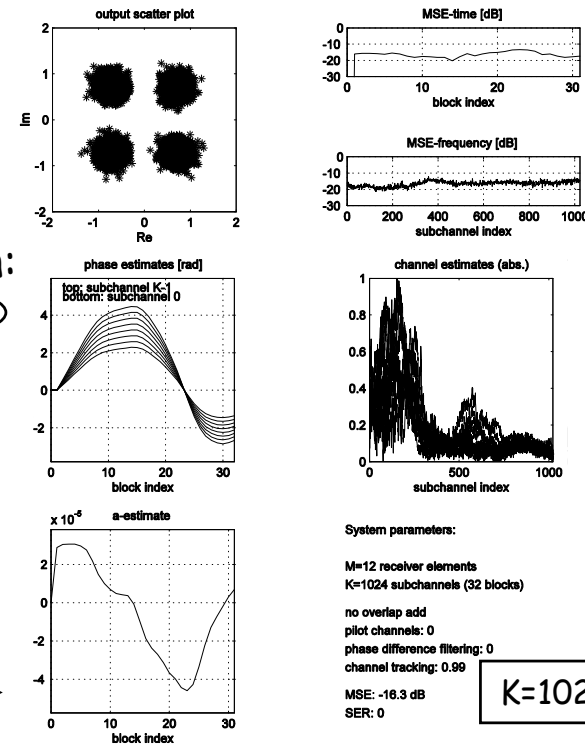
$$y_k(n) \sim \sum_l H_{k,l}(n) d_k(n) \sim H'_k(n) e^{j\theta_k(n)} d_k(n)$$

$$\theta_k(n) \sim 2\pi a' f_k n T' \sim \theta_k(n-1) + 2\pi a' f_k T'$$

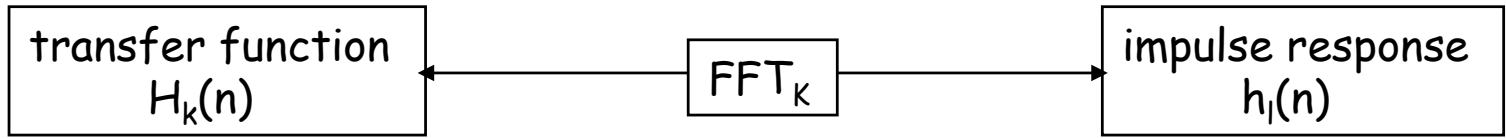
time-variation:  
 • phase offset  
 • ICI

- estimate the Doppler factor  $a'(n)$
- use this (single) estimate to compute all  $K$  phases

30 kbps @ minimal complexity



# OFDM: channel estimation



K coefficients  
(system parameter)

J (out of L) coefficients  
(channel parameter)

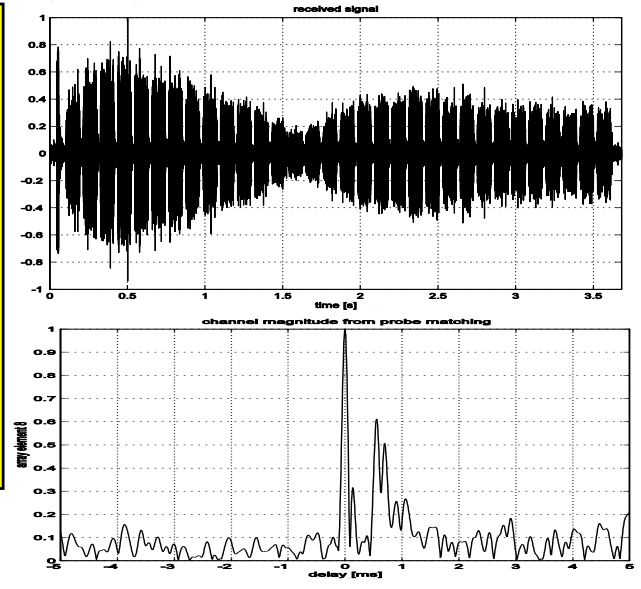
- non-adaptive: each block detected independently: need L pilots per block ( $\sim T_{mp} B$ )
- adaptive: each block detected using knowledge from previous block

channel sparsifying: keep J strongest taps only.  $J/L$

data-aided: can use all K symbols per block.  $L/K$

$J/K$

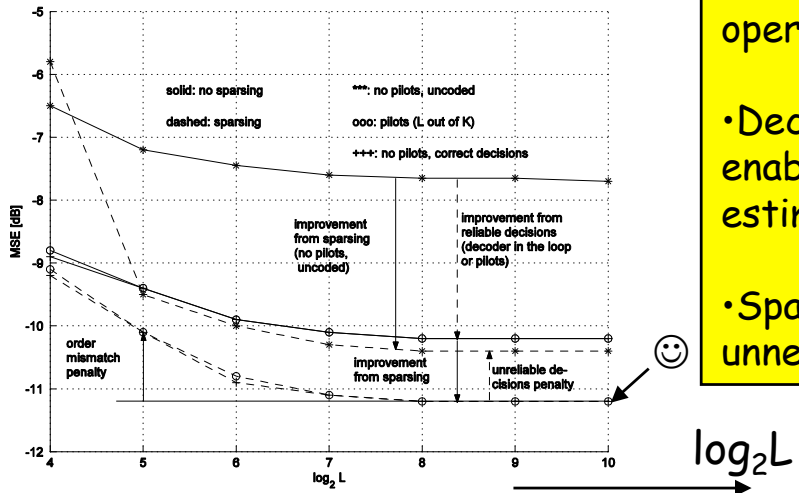
Panama City Beach, 1 km, 12 kHz



• Adaptive synchronization enables decision-directed operation (no null subcarriers)

• Decision-directed operation enables full-size channel estimation (low pilot overhead)

• Sparsifying eliminates unnecessary estimation noise.



Pushing performance limits: MIMO OFDM (for spatial multiplexing gain)

$$R/B = M_T / (1 + T_g B/K) \text{ symbols/sec/Hz}$$

Want:  $M_T$ ,  $K$  as large as possible.

$$(M_T \leq K/L)$$

$$R/B \leq \frac{K^2}{LK + L^2} \sim \frac{K}{L}$$

Increasing  $M_T$  increases cross-talk between channels, size of the estimator; MIMO channel estimation becomes more difficult.

Increasing  $K$  increases block duration ( $T=K/B$ ); ICI arises.

Work in progress: MIMO channel estimation, ICI equalization, pulse-shaped MCM, ...  
Experiment: 4-tx, Martha's Vineyard, 1 km, 10 kHz (nudging 10 bps/Hz)

Q: What is the performance limit? Does it "depend on the weather?"

## Open problems

channel: statistical characterization  
(for simulation, performance bounds)

tx: adaptive modulation / power control (channel state prediction)  
spectrum shaping, coding,...

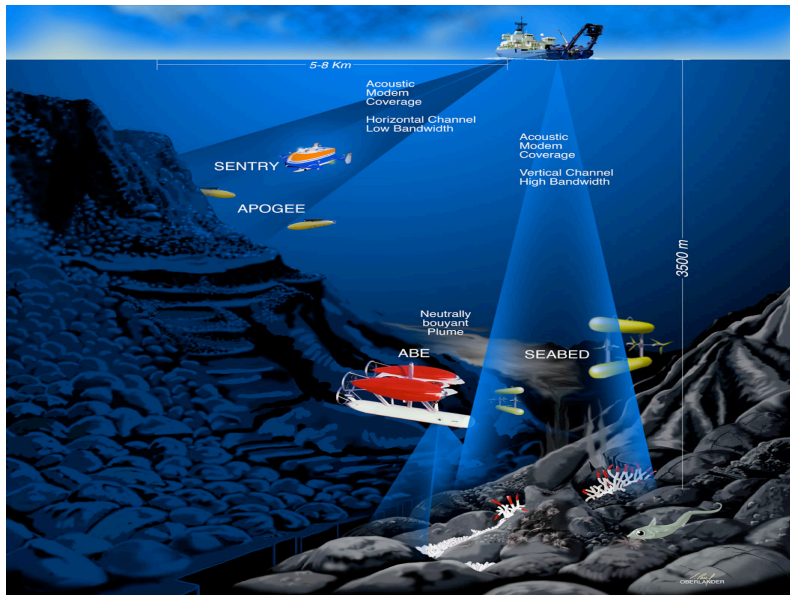
rx: adaptive receivers (single- and multi-carrier; single- and multi-input)  
model-based processing (e.g., path-specific Doppler)

networks: efficient and scalable protocols on all layers  
topologies, architectures ("typical applications?")  
capacity?

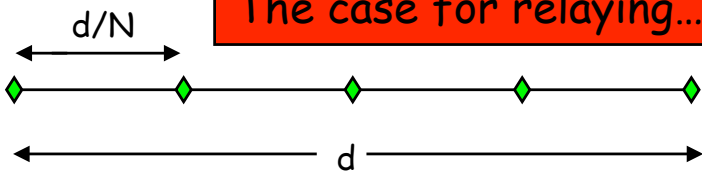
system integration and optimization:  
from data compression to navigation (and back)



# Underwater networks



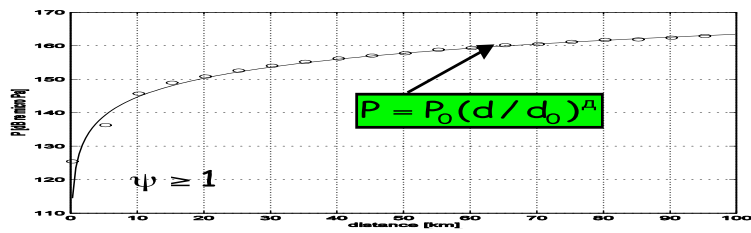
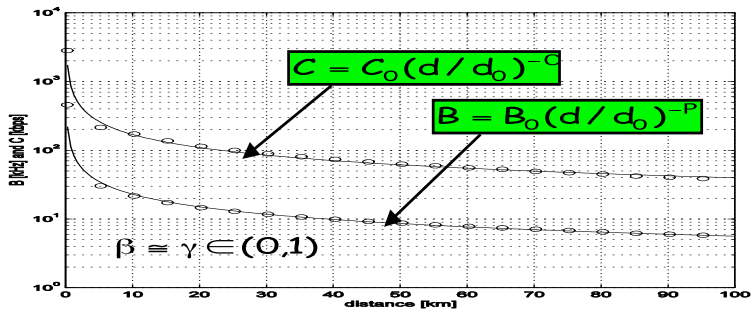
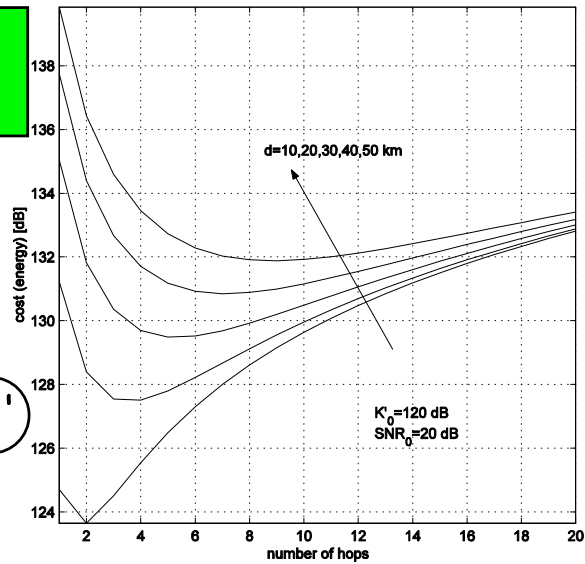
# The case for relaying...



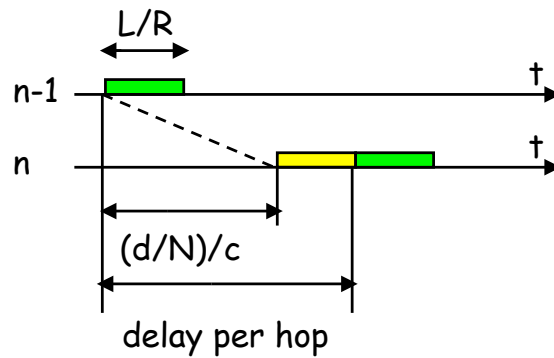
power and bandwidth improve with # hops

$$E_N(d) = P_N(d) / C_N(d) = NP(d/N) / C(d/N)$$

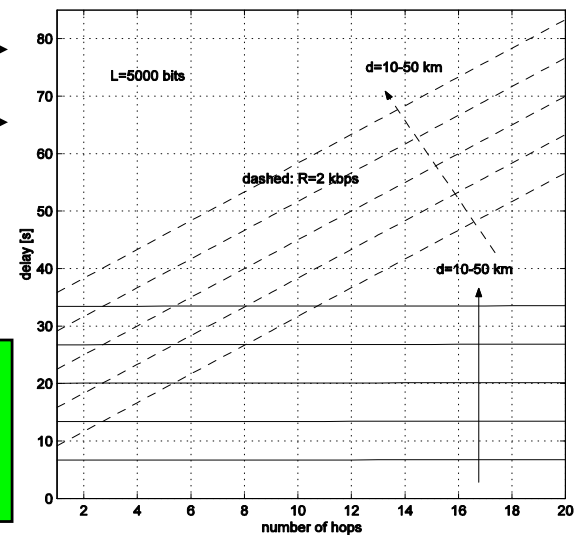
$$K'(N) = E_N(d) + (N - 1)K_0' \rightarrow \text{min. w.r.t. } N$$



capacity depends on distance



delay penalty negligible if bit rate adjusted to distance.



... is the case for signal processing.