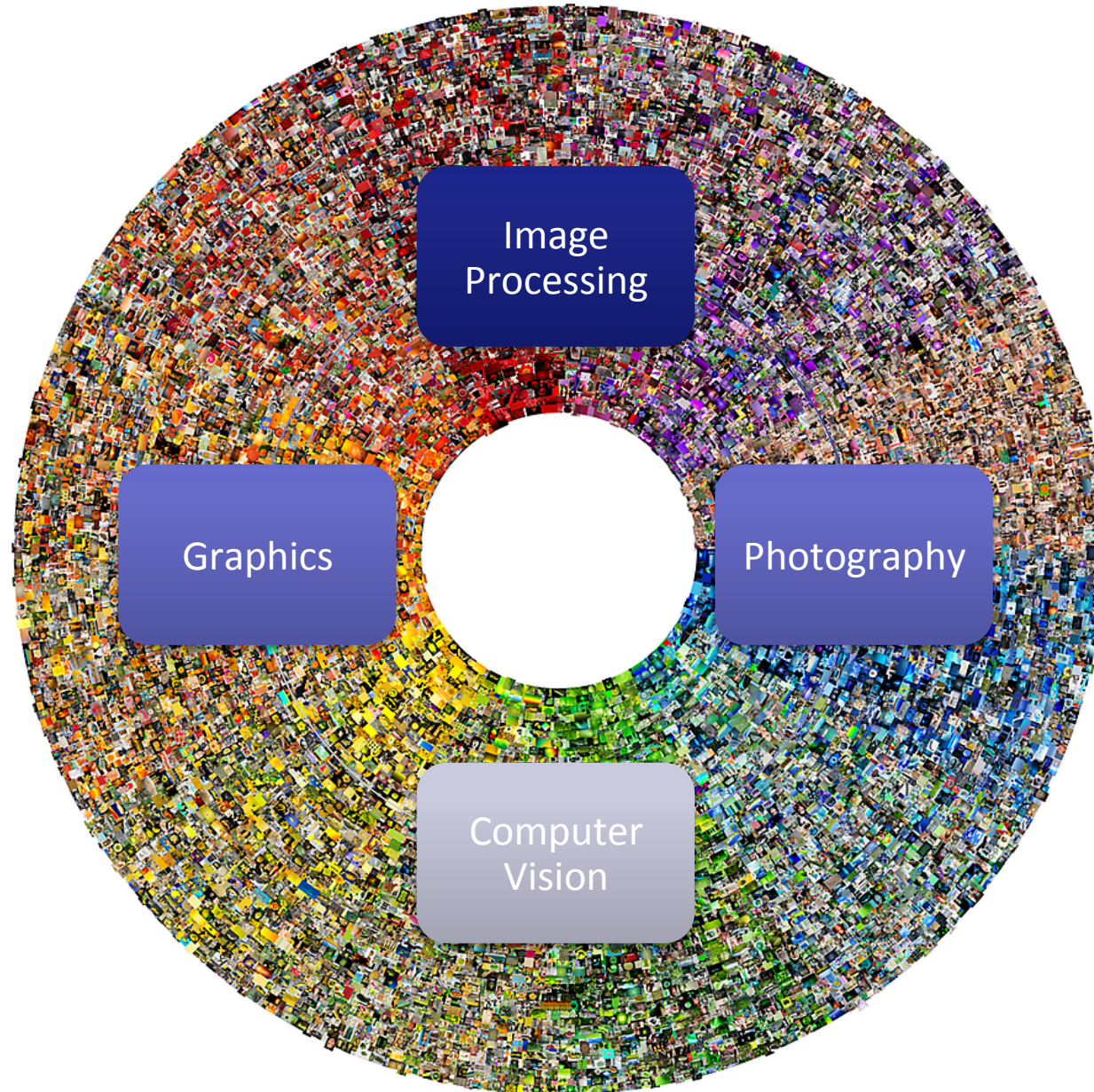


Computational Imaging:

From Photons to Photos

Peyman Milanfar

What is Computational Imaging?



Long and fascinating history



Harold "Doc" Edgerton (1903 – 1990)

“Stopping Time”



Dual Aims of Computational Imaging

Capture what I see (Photography)

- Take a nice picture (noise, dynamic range, etc.)
- Make me a better photographer.
- Do it with my simple camera.

Let's have a look

Sensors: Form vs. Function

\$500



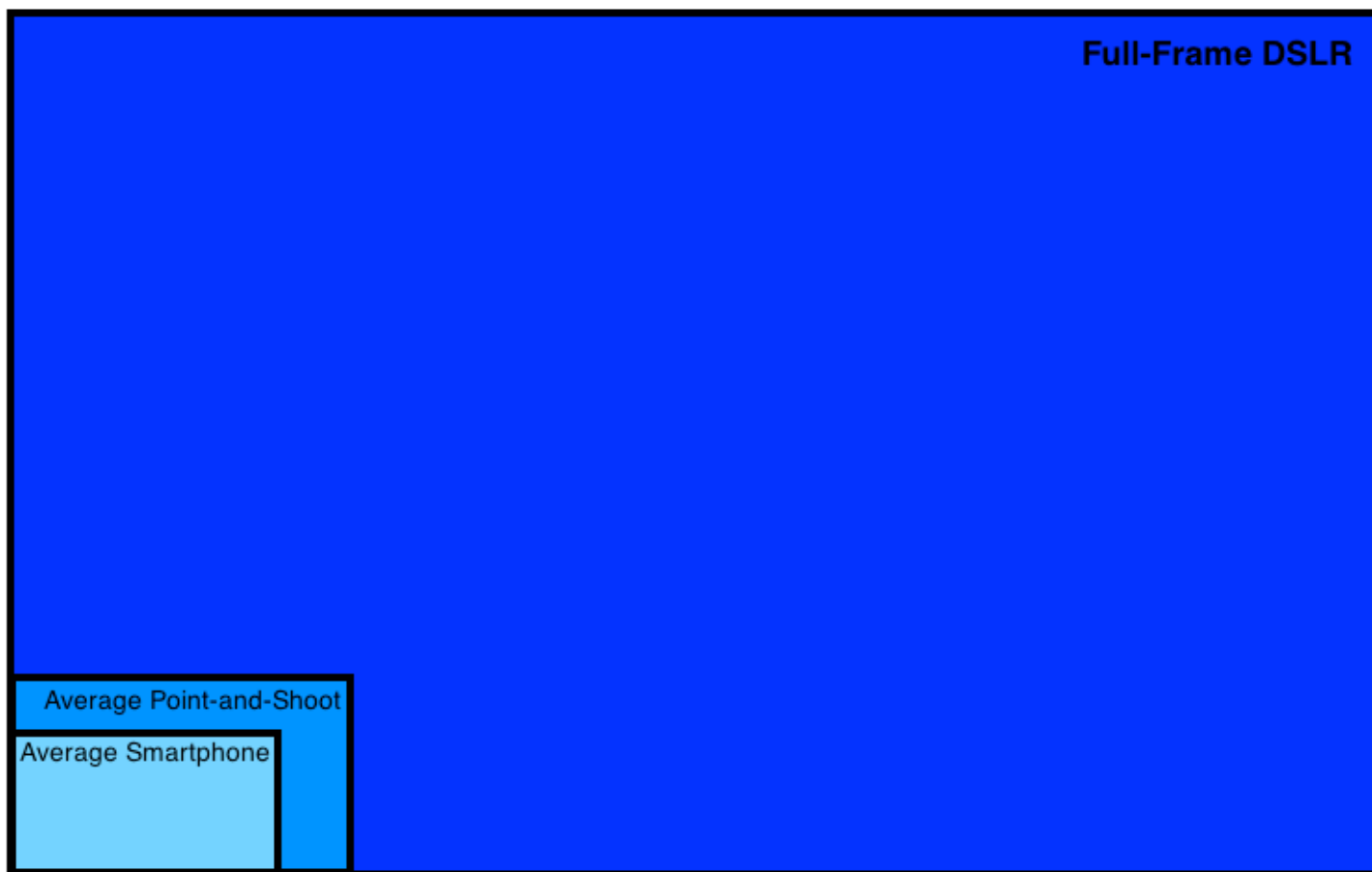
\$5



Mobile phone camera

Can these two ever be equally good at taking pictures?

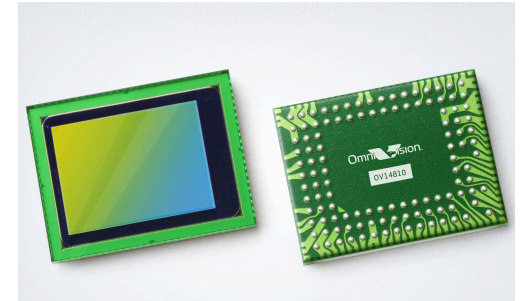
Sensor Sizes in Popular Devices





Physical Limitations → Opportunities

- Optics won't get a lot better.
- Pixels can't get much smaller.
 - Limited by optical wavelengths
- Sensor won't get much larger
 - Limited by cost and form factor
- Need:
 - Better Capture Protocols
 - Clever Algorithms



Both are from Nexus 5



Standard shot



With Lens Blur

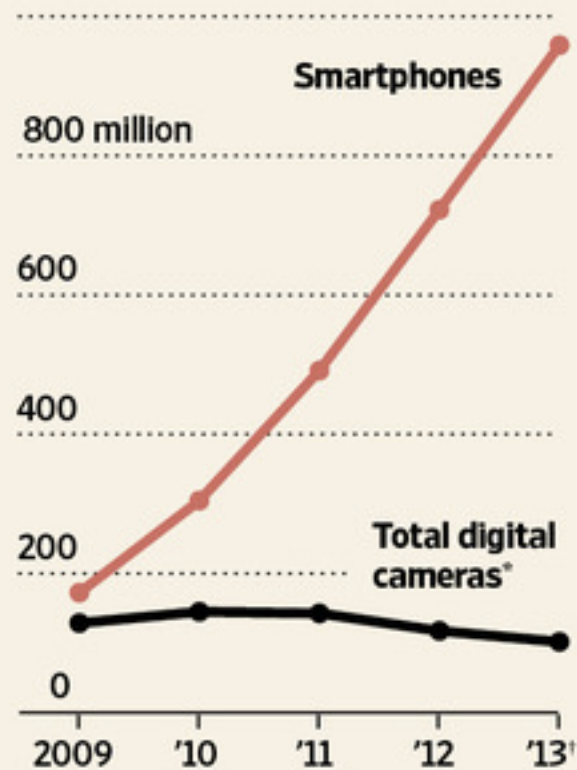


BUSINESS INSIDER

Mobile Imaging is Totally Dominant

Shift in Focus

The global smartphone market has skyrocketed while digital cameras have foundered.



*Includes compact, mirrorless and single-lens reflex cameras †Forecast

Source: IDC
The Wall Street Journal



2015 -- Paris



2015 -- Moscow



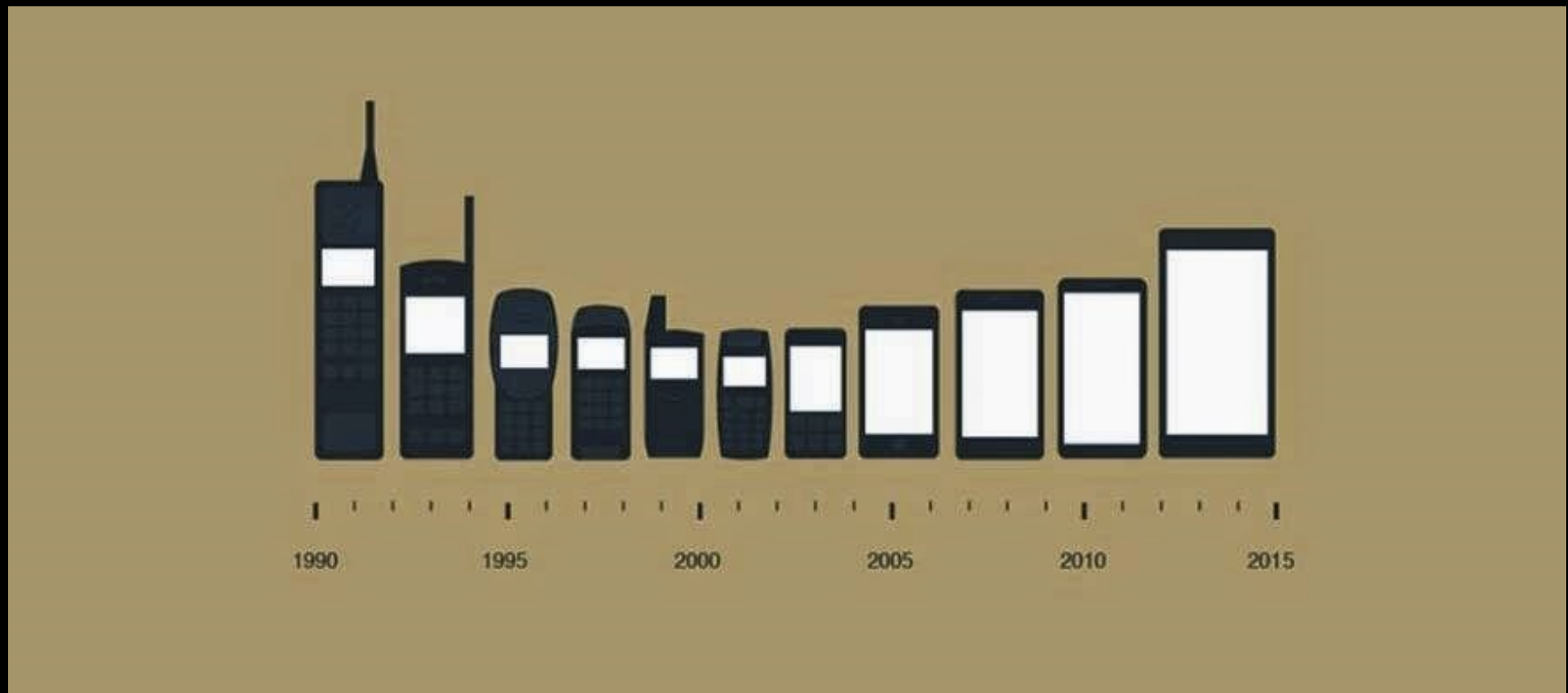
2015 -- Sydney



1,000,000,000,000

Roughly a **trillion** photos shared on
social media (in 2014)

Evolution of the (Smart)phone



Dual Aims of Computational Imaging

Capture what I see/like (Photography)

- Take a nice picture. (noise, dynamic range, etc.)
- Make me a better photographer.
- Do it with my simple camera.

Capture what I can't see (Science, Military)

- See in the dark
- View fast, slow, small, or faint phenomena
- Detect, magnify subtle changes

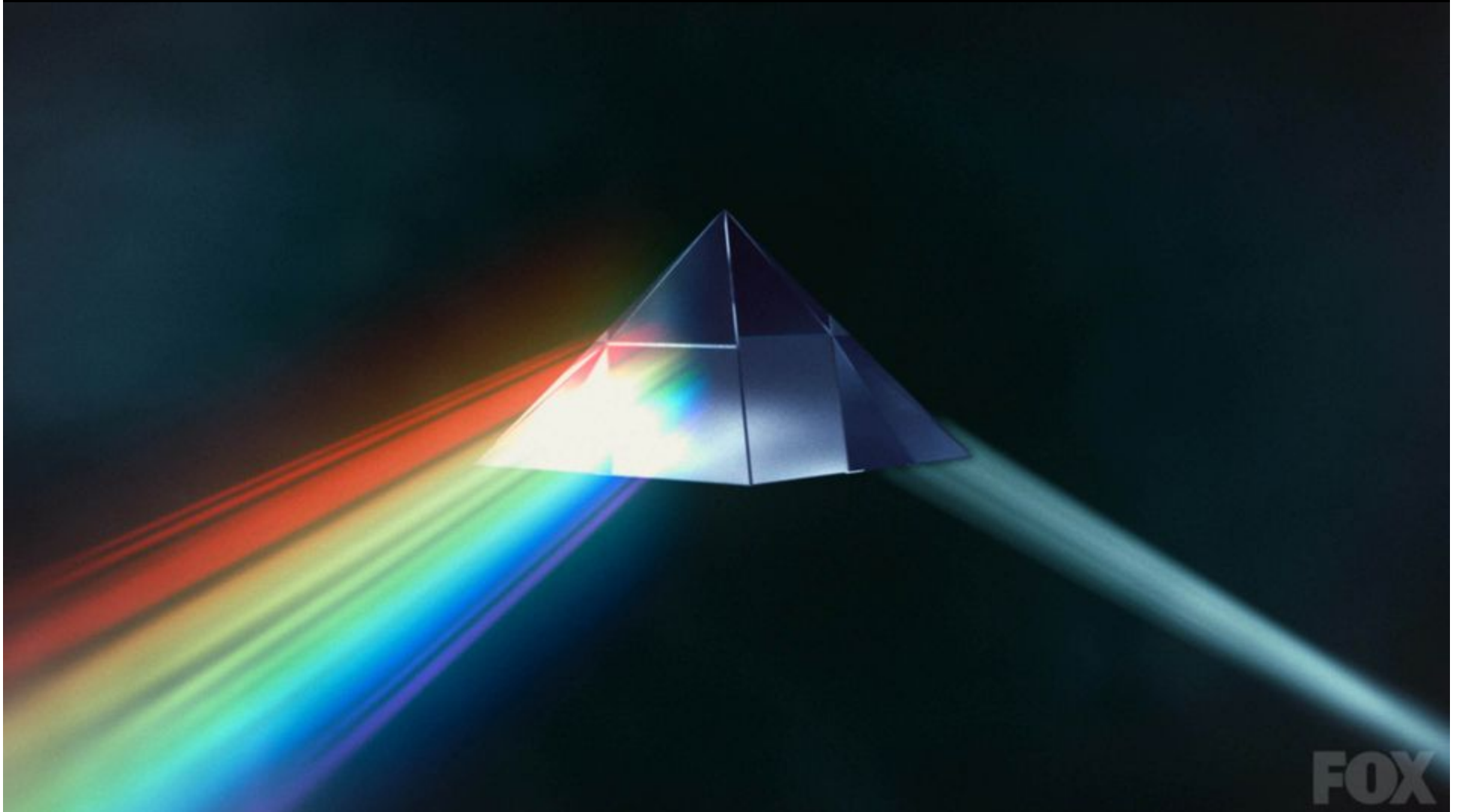
Yosemite Valley, California

At night



(Jesse Levinson Canon 10D, 28mm f/4, 3 min, ISO 100, 4 image pano)

Can't "see" most of nature that surrounds us

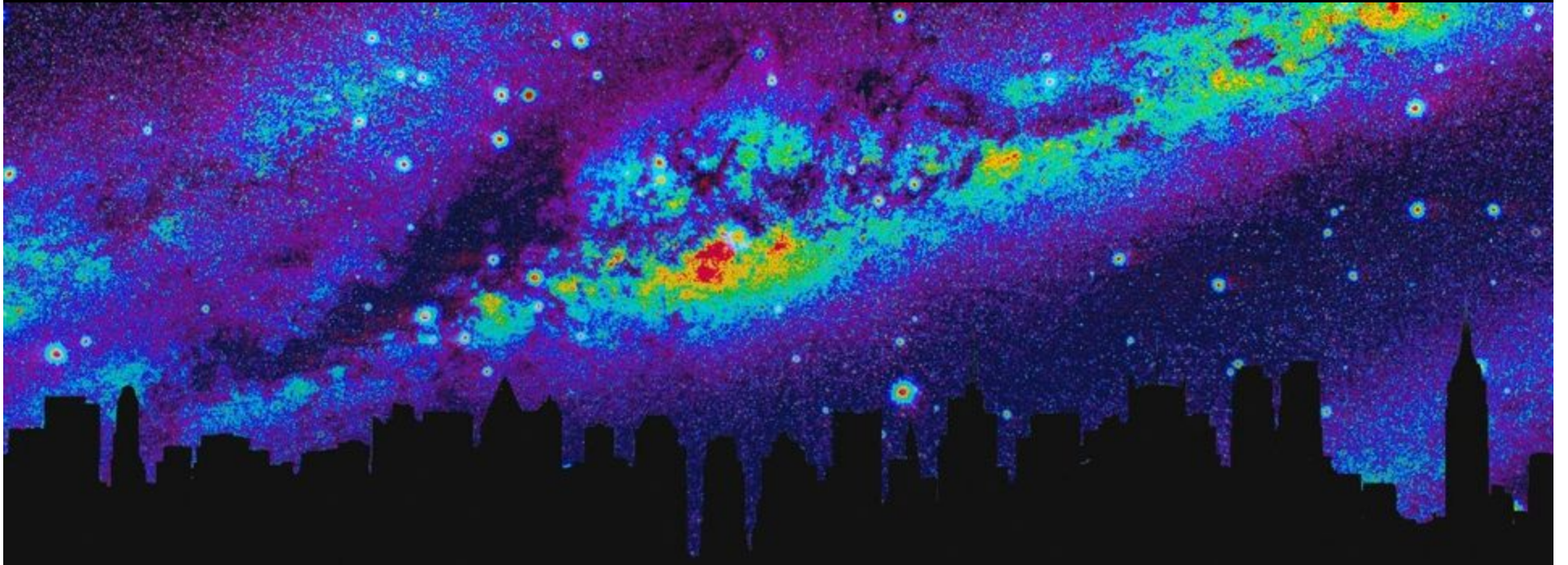


FOX



FOX

Infrared



FOX

Gamma-ray



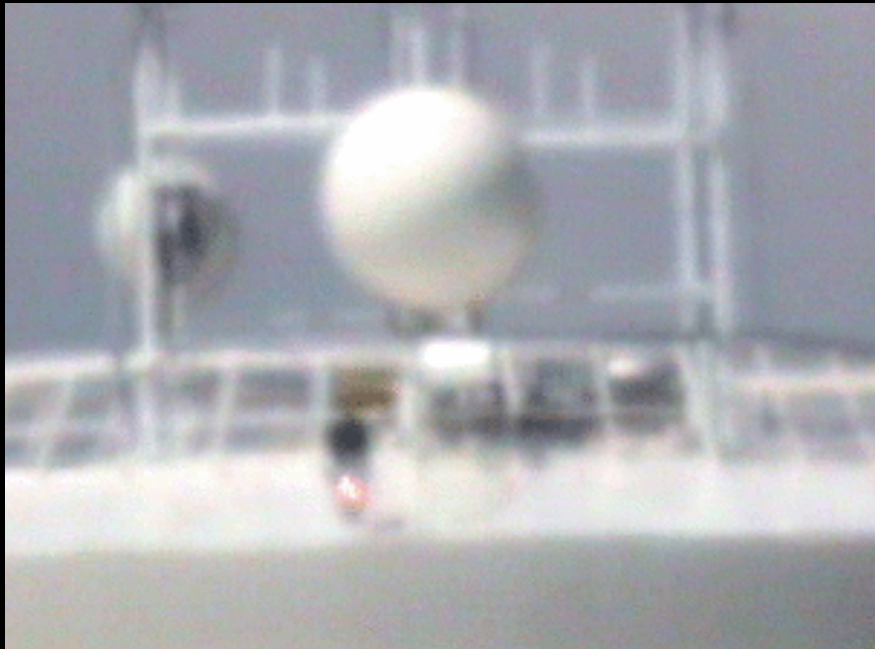
FOX

X-ray

Seeing Far Away

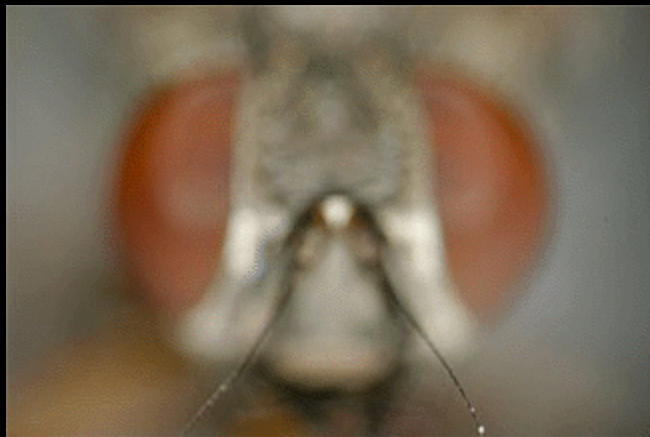
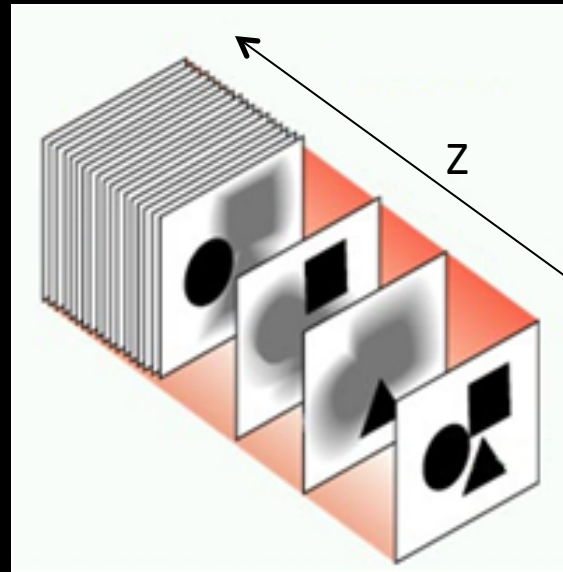


Seeing Far Away

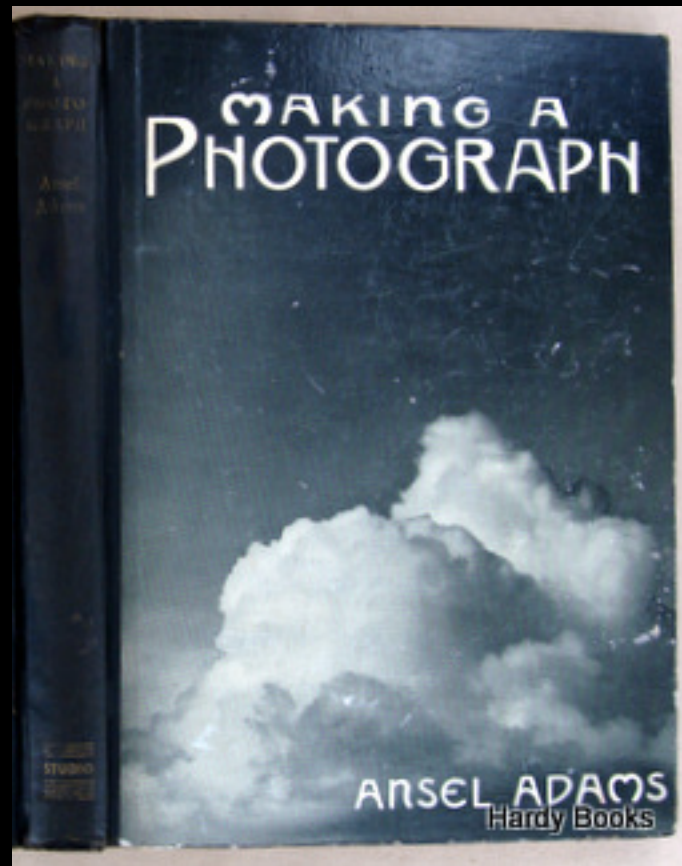
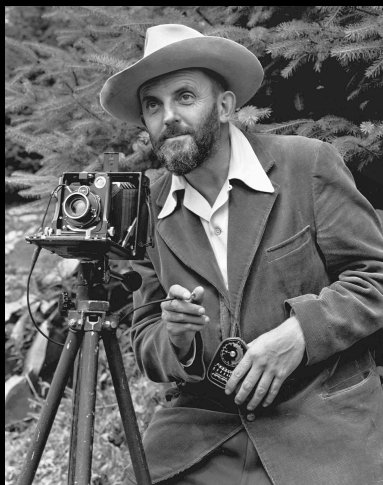


Top part of a water tower imaged at a (horizontal) distance of 2.4 km

Seeing Small Things



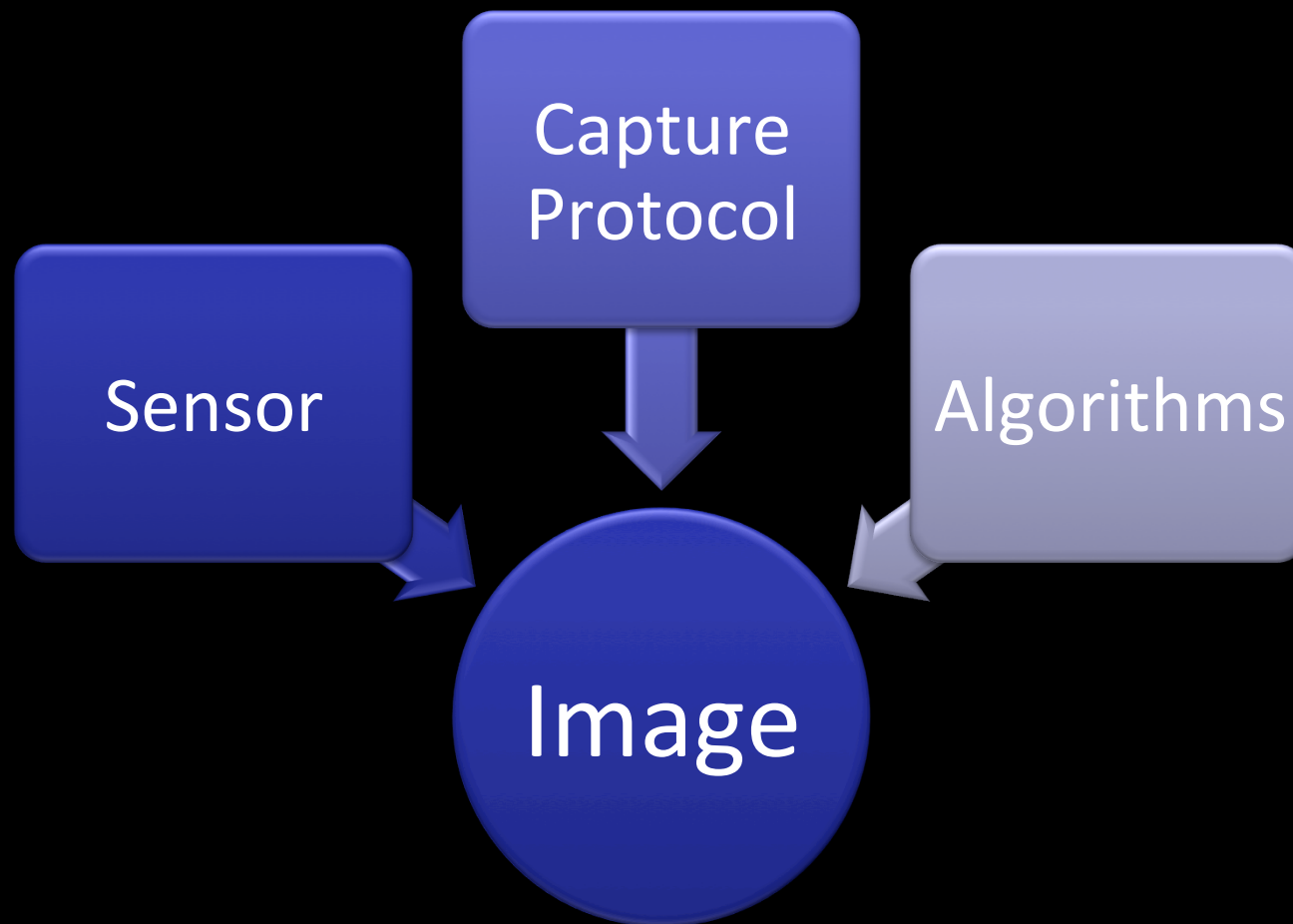
How Do We Make a High Quality Image?



Ansel Adams' first book, published 1935

How Do We Make a High Quality Image?

- Integration of Sensor and Computation plays a key role in the image formation process.



Computational Photography on Android

devCam

Main	Interface	Capture Designs	Capture Output	Directories
Example Applications		devCam JSONs	devCam and MATLAB	Device Database

devCam

Parameterized Camera Control for Algorithm Development and Testing

devCam is an app for parameterized image capture using Android devices. devCam makes it simple to capture complicated sets of photographic exposures with user-defined values for standard photographic settings. It is designed to give the user as much control as the camera allows, making use of the camera2 API (requires Lollipop, Android 5.0+) to give the user manual control over the following (if the device is capable):

- Exposure time
- ISO
- Aperture
- Focal Length
- Focus Distance

devcamera.org

<https://youtu.be/92fgcUNCHic?t=29m56s>

Standard Burst Photography

Locked: Exposure, Focus



HDR Burst Photography

Locked Focus
Variable Exposure



Focal Sweep Photography

Locked Exposure
Variable Focus



Part 2:

A general filtering framework

The Black Box

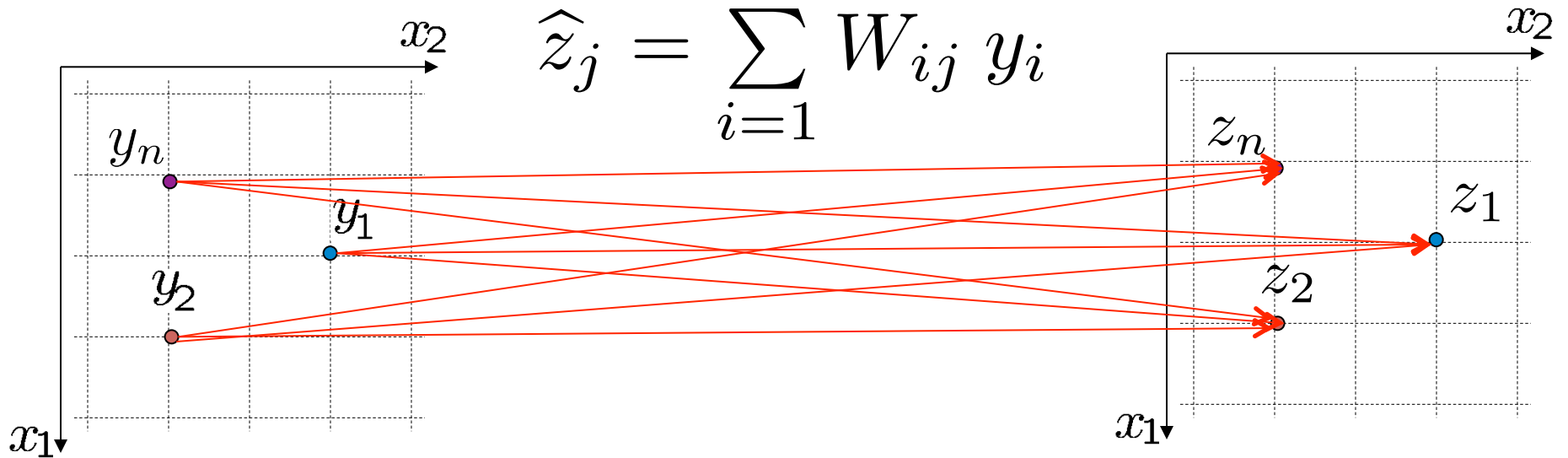


Input image

Output image

$$\hat{z}_j = \mathbf{f}(y_1, \dots, y_n)$$

$$\hat{z}_j = \sum_{i=1}^n W_{ij} y_i$$

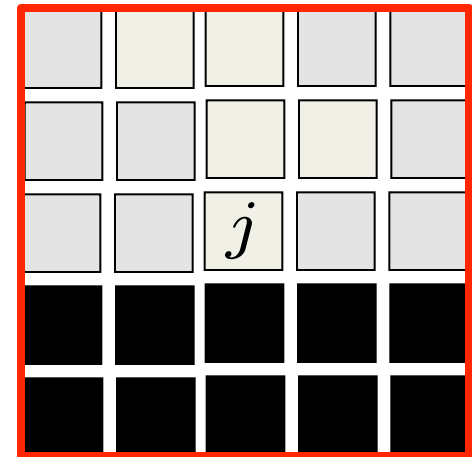


How to design the black box

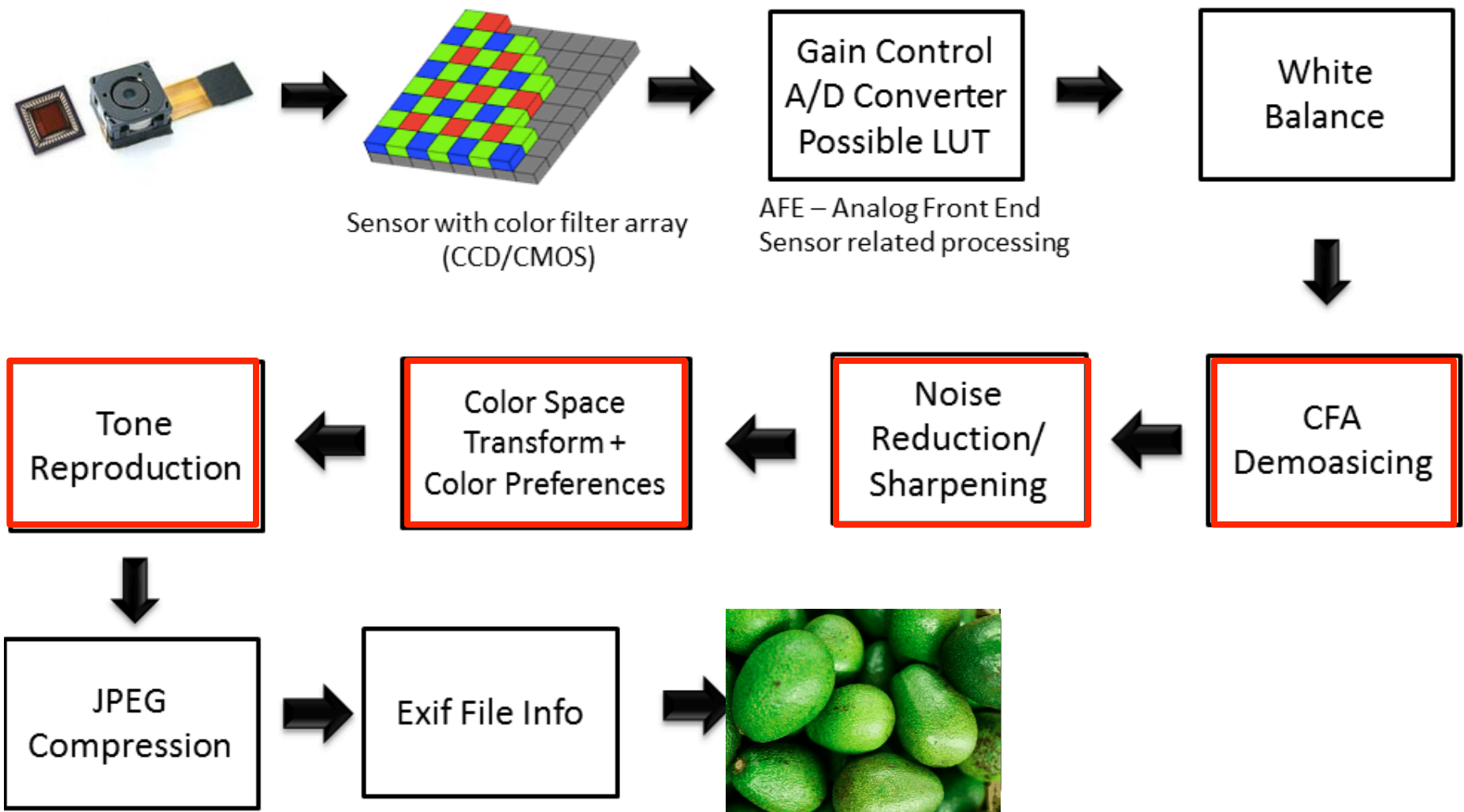
$$\hat{z}_j = \sum_{i=1}^n W_{ij} y_i$$



$y_i \in$

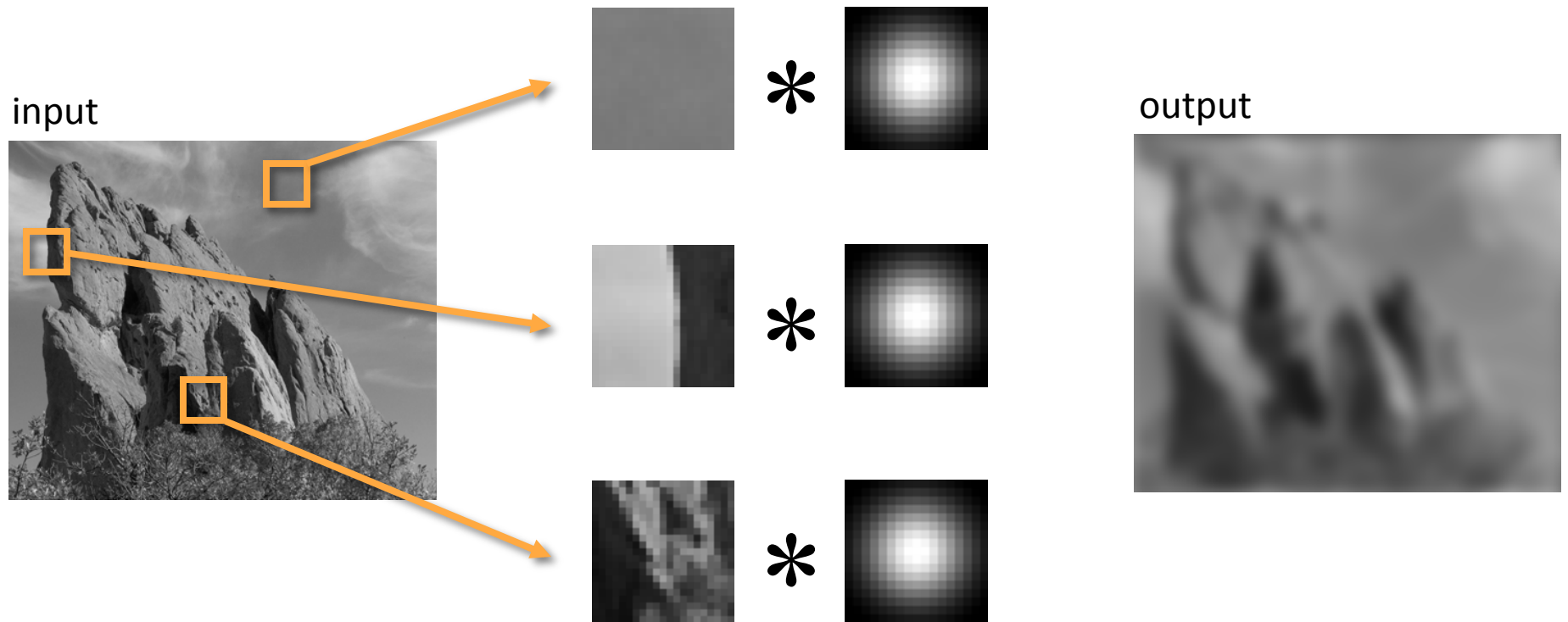


Model for Many Parts of Pipeline



Same weights everywhere

$$\hat{z}_j = \sum_{i=1}^n W_i y_i$$



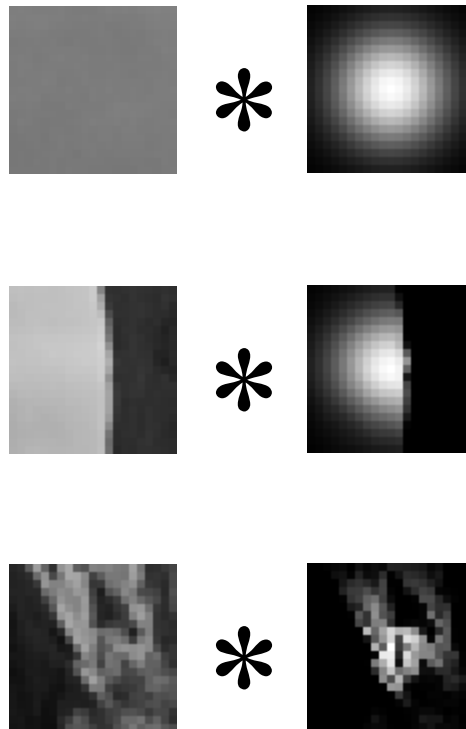
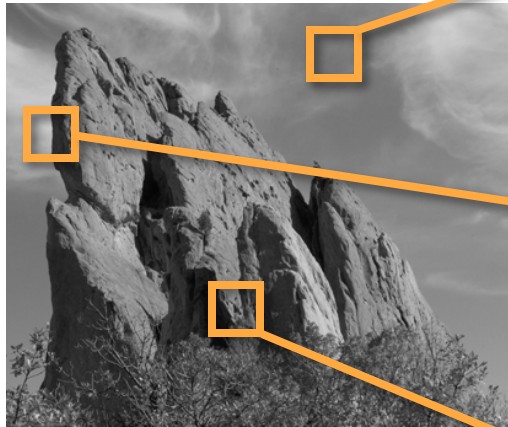
Same Gaussian kernel everywhere.

Data-adaptive weights

$$\hat{z}_j = \sum_{i=1}^n W_{ij} y_i$$

↖

input



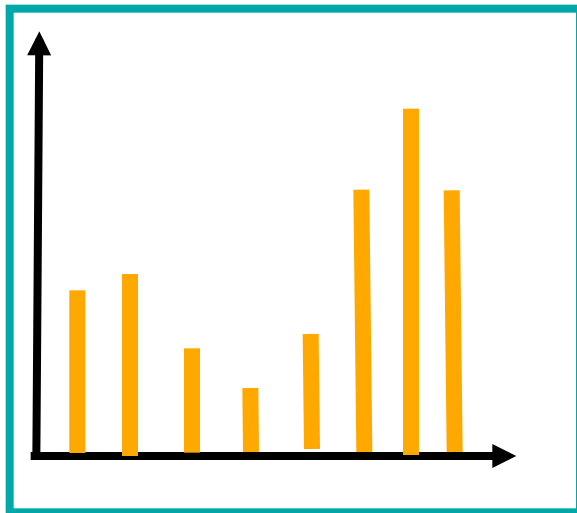
output



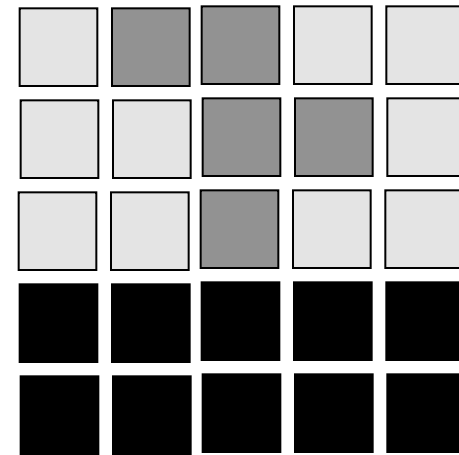
The kernel shape depends on the image content.

Method 1: Consider the histogram

Histogram



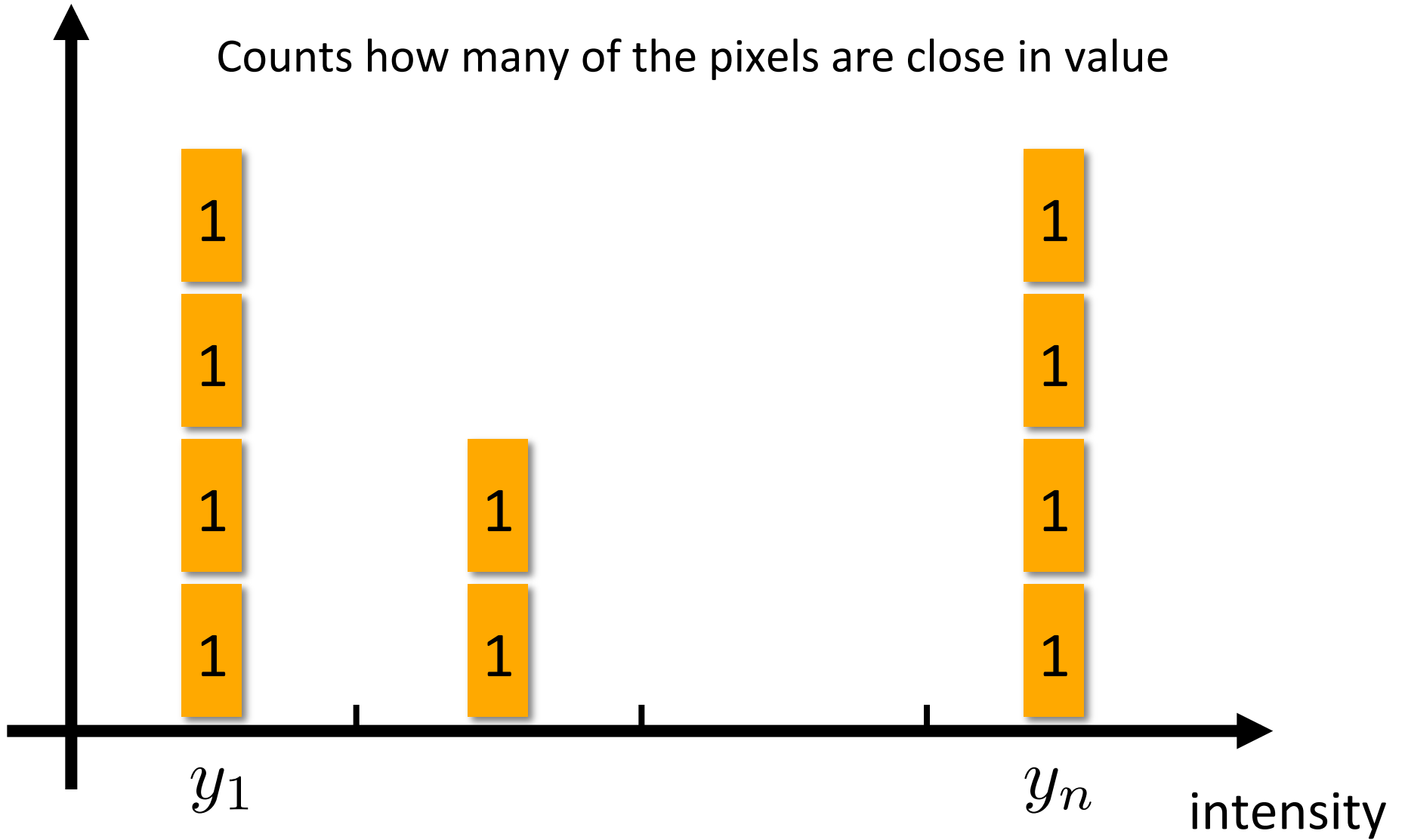
Y_i



Just for illustration – we don't really make the histogram.

pixels

Counts how many of the pixels are close in value

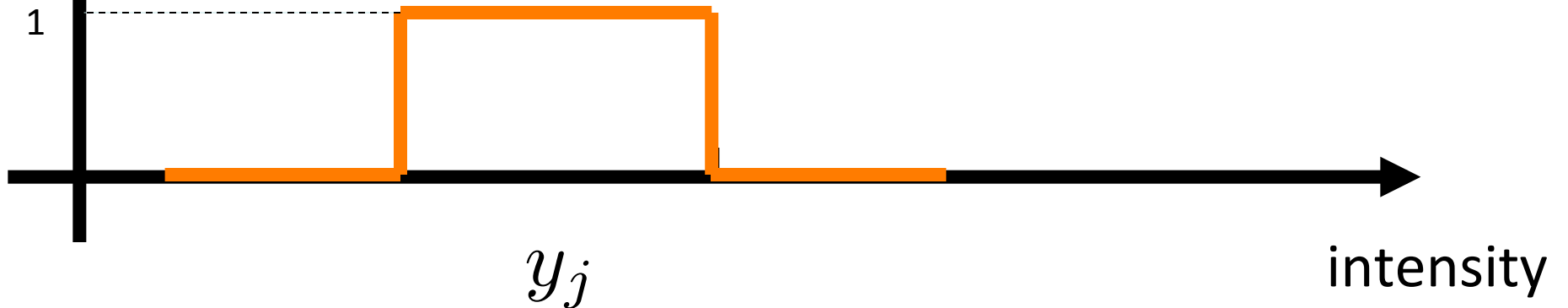


pixels

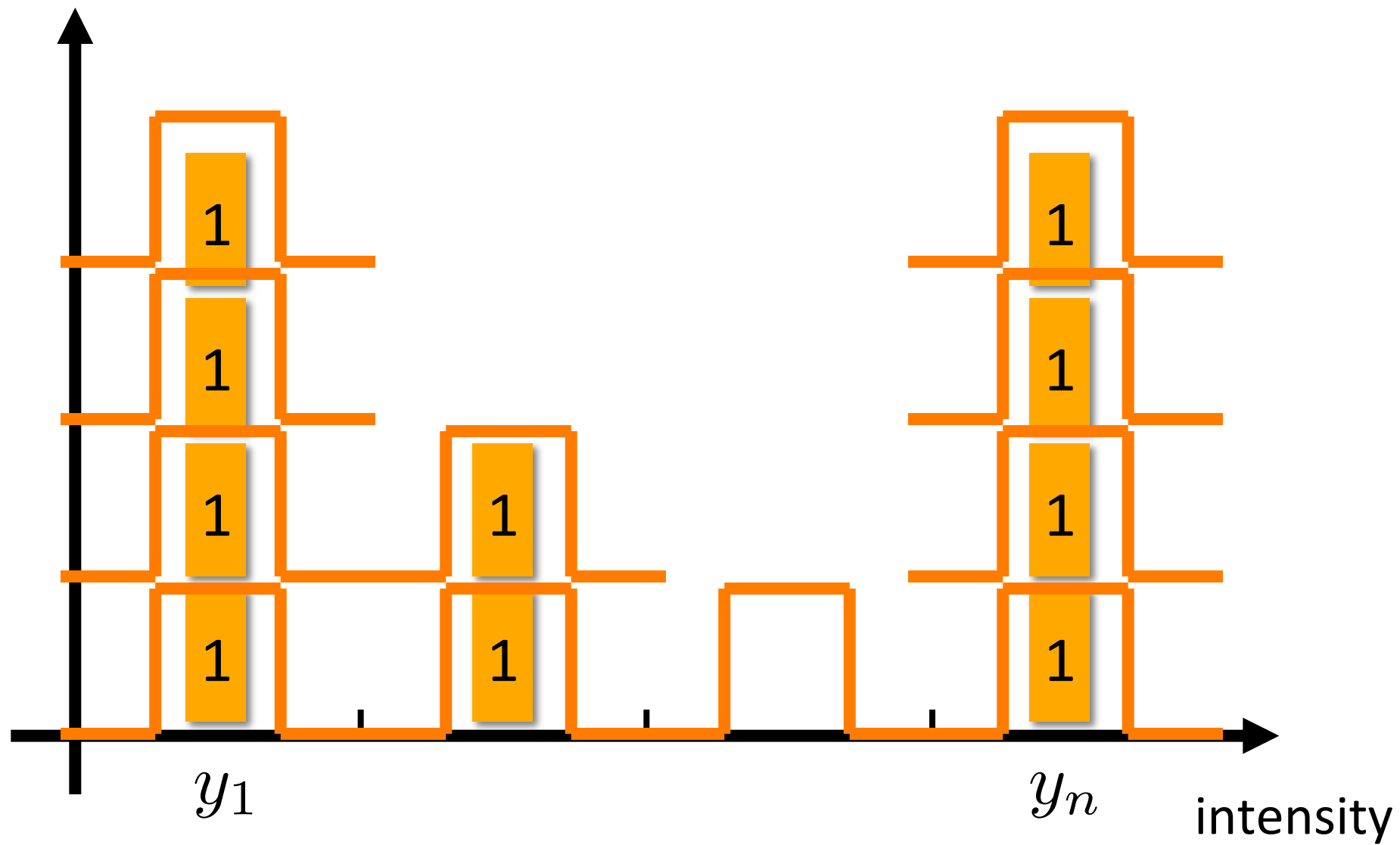
Counts how many of the pixels are close in value to y_j

$$H(y_j) = \sum_{i=1}^n K(y_i - y_j)$$

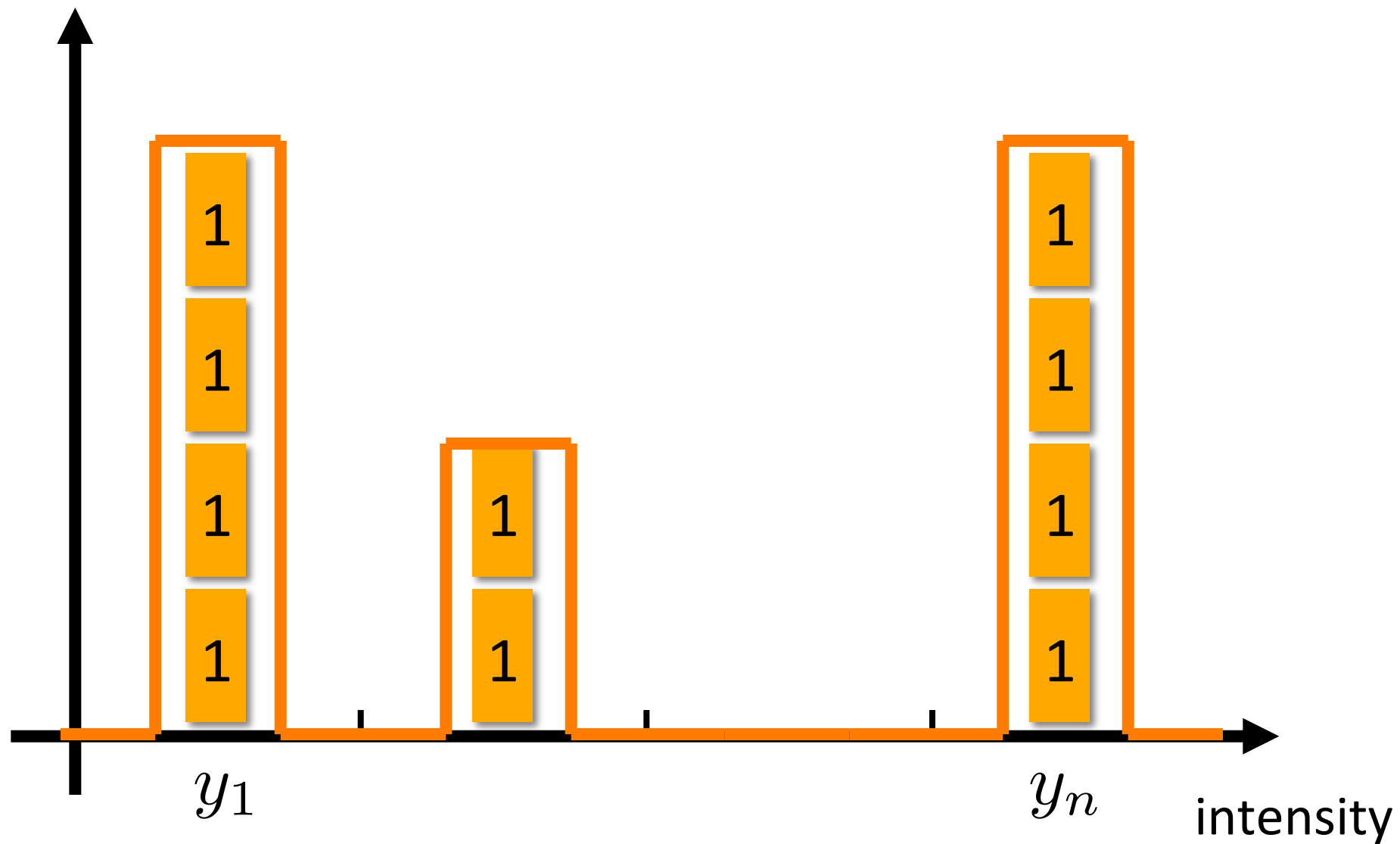
$K(\cdot)$



pixels



pixels



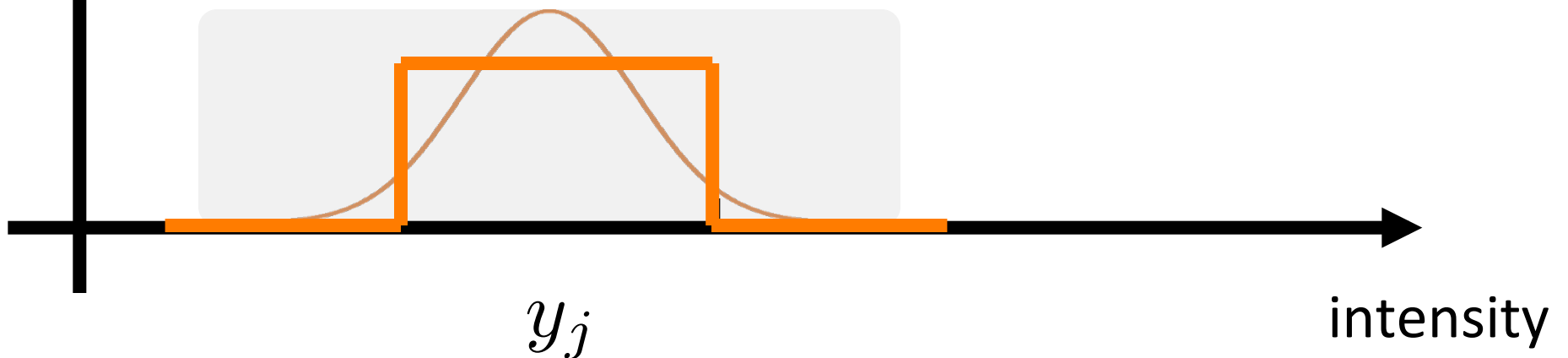
pixels

Why only the box function?

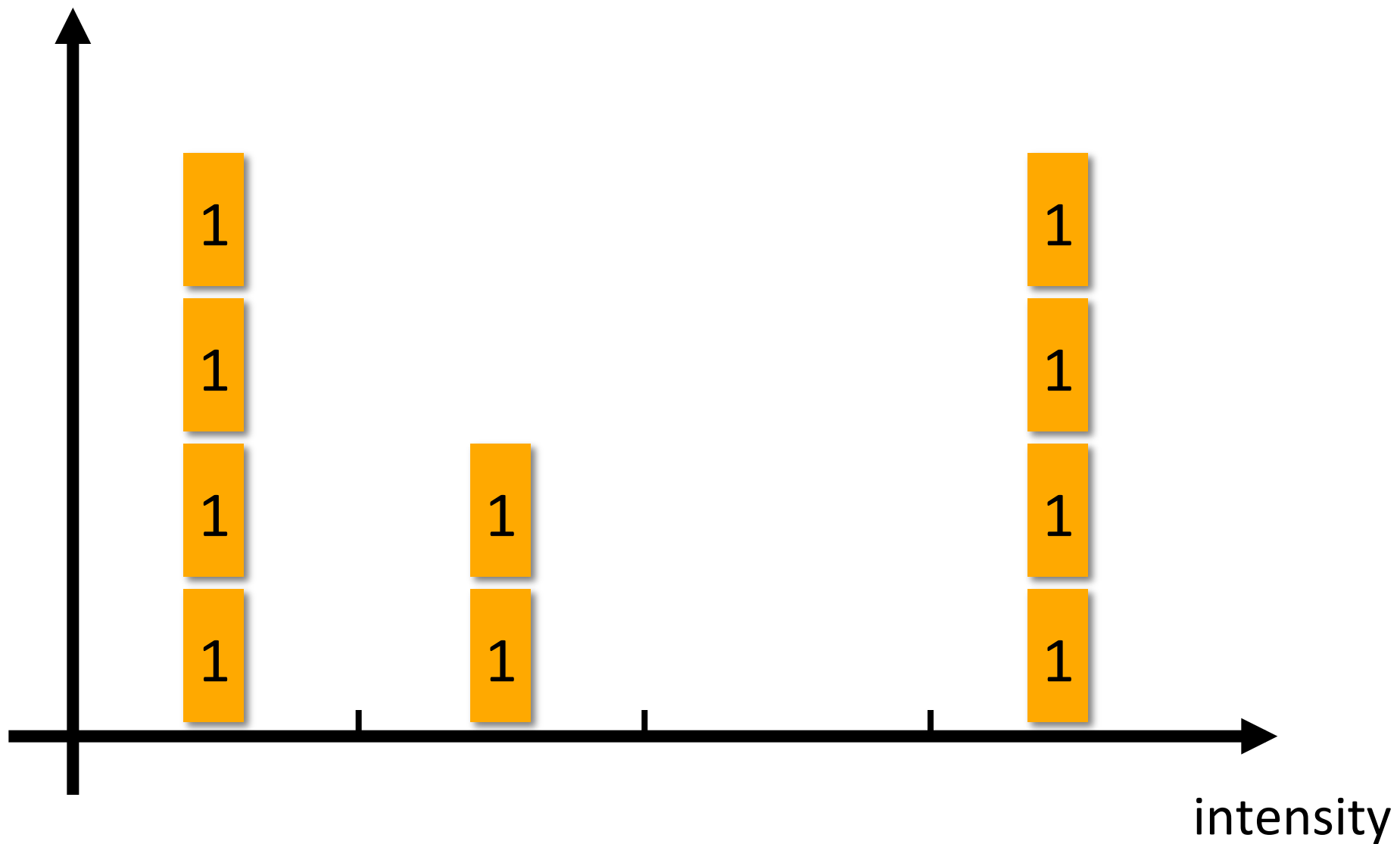
Soft count of how many of the pixels are close in value to y_j

$$H(y_j) = \sum_{i=1}^n K(y_i - y_j)$$

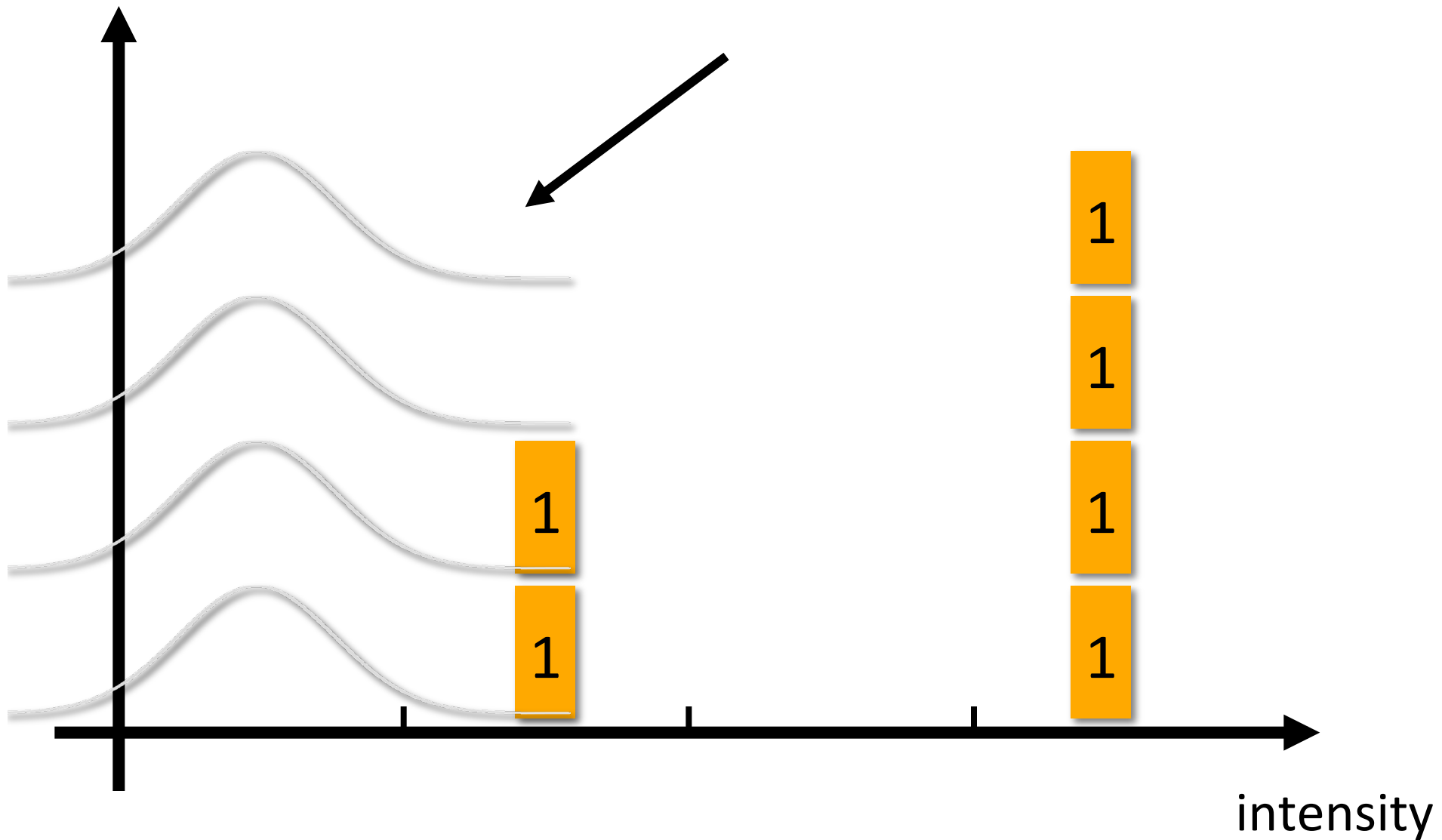
$K(\cdot)$: Symmetric



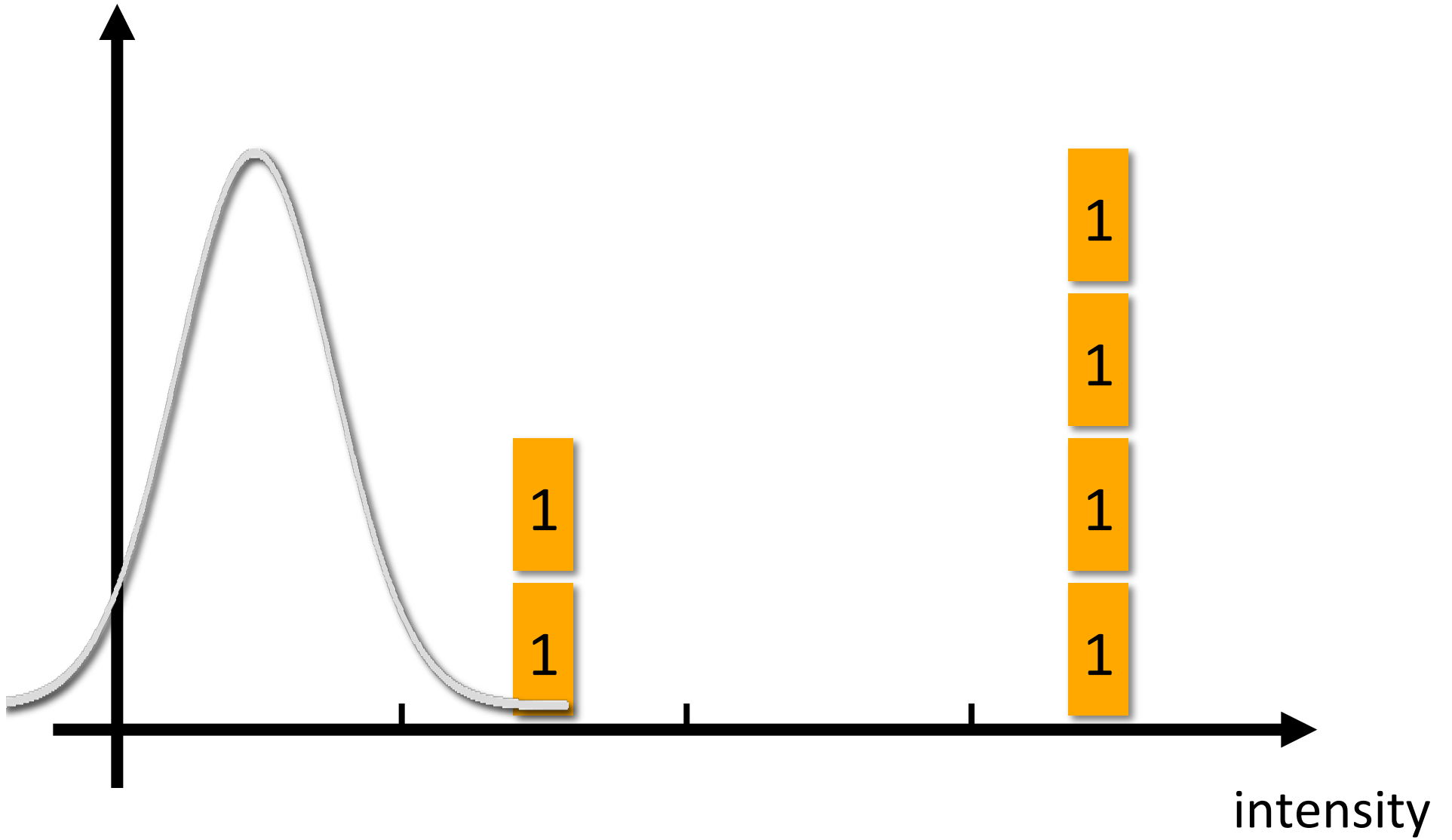
pixels



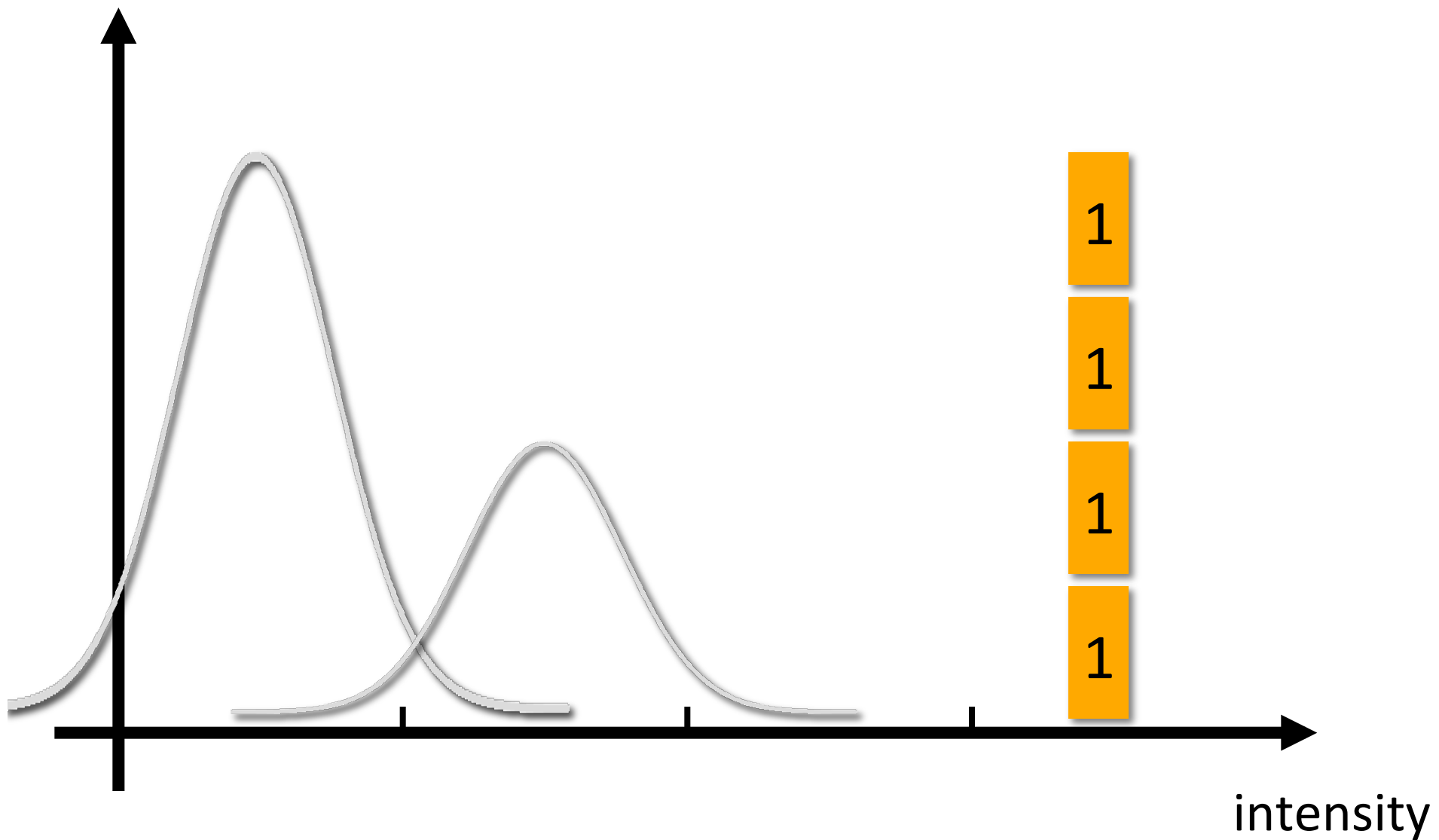
pixels



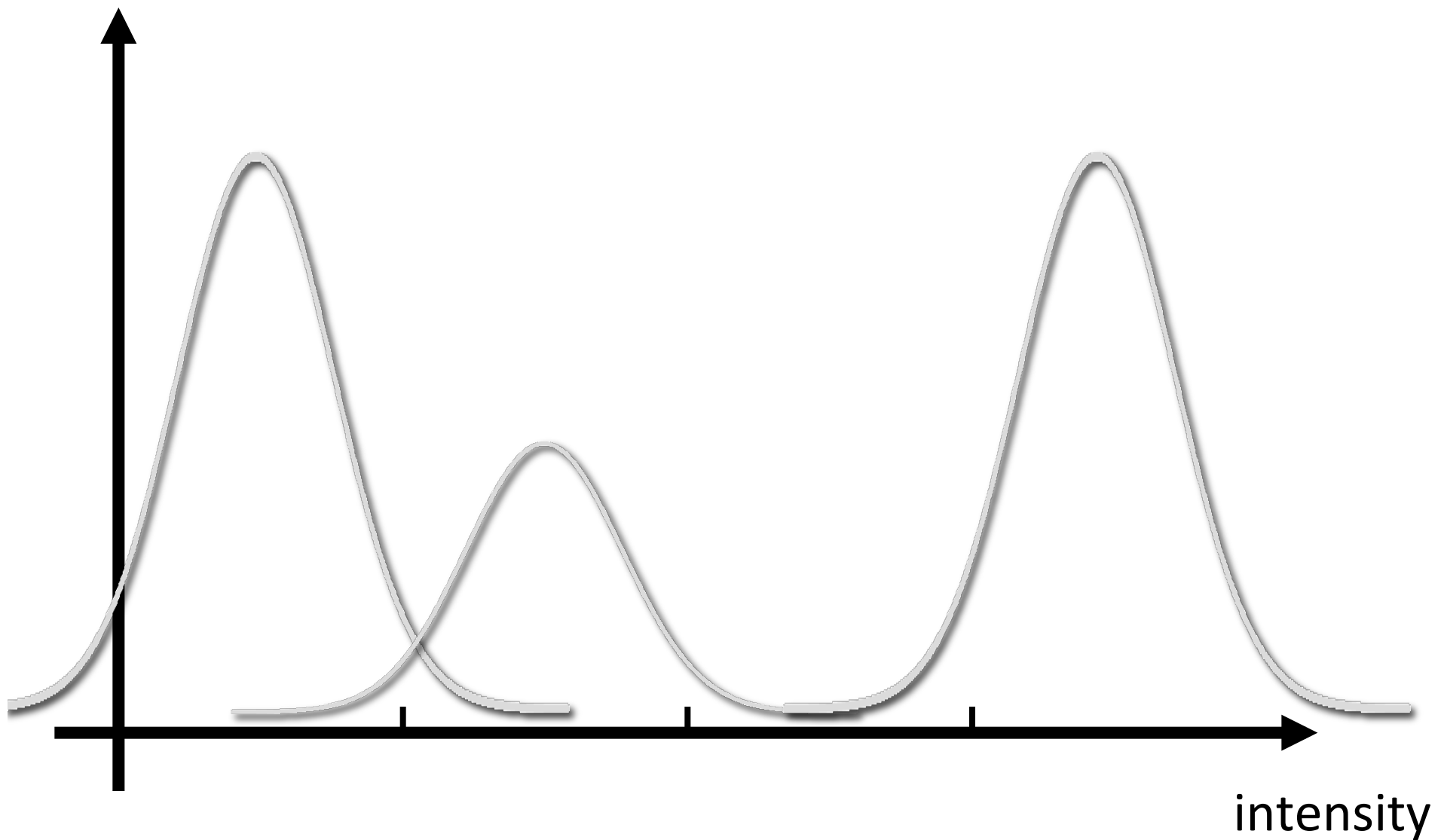
pixels



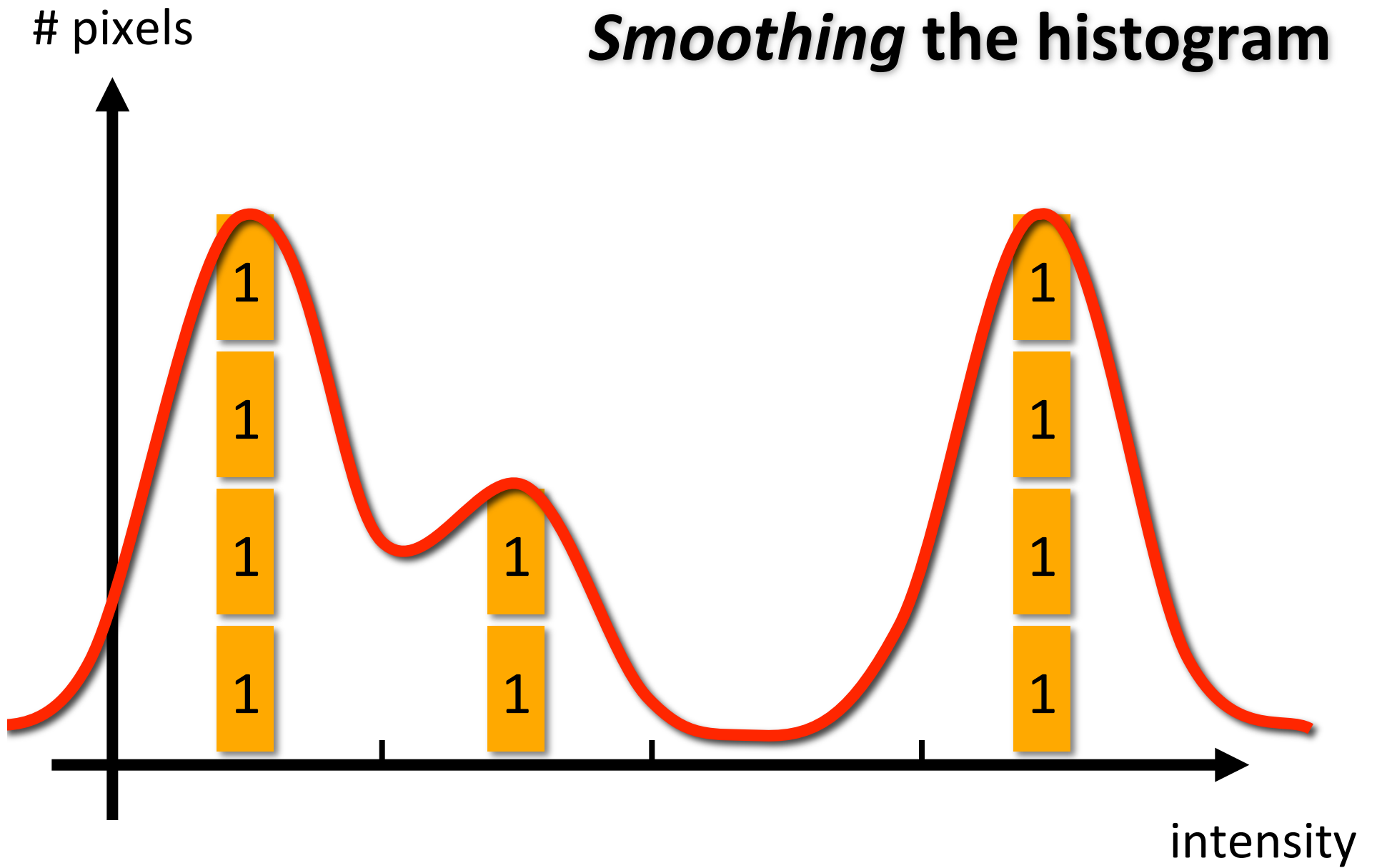
pixels



pixels



Smoothing the histogram

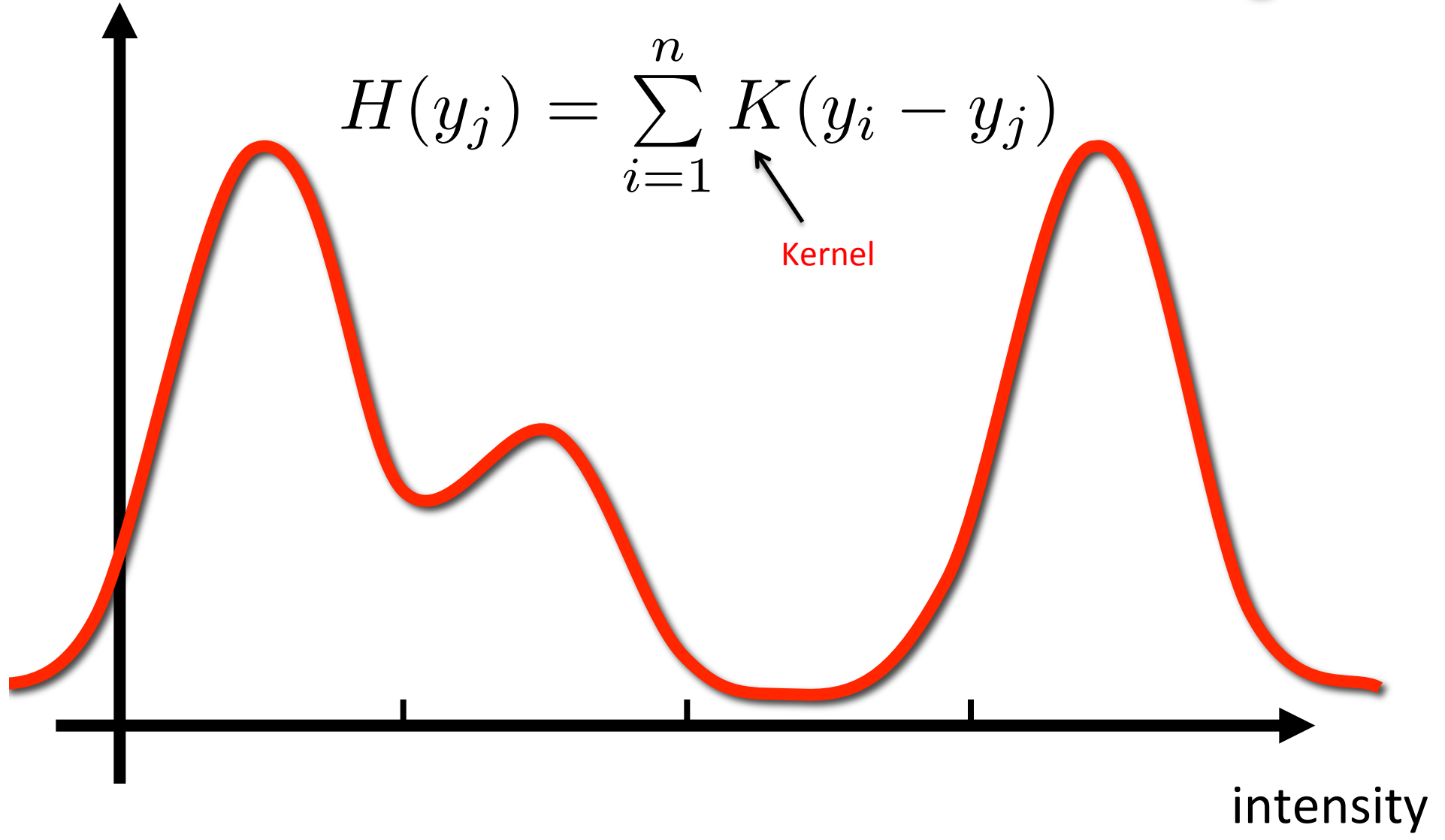


Smoothed histogram

pixels

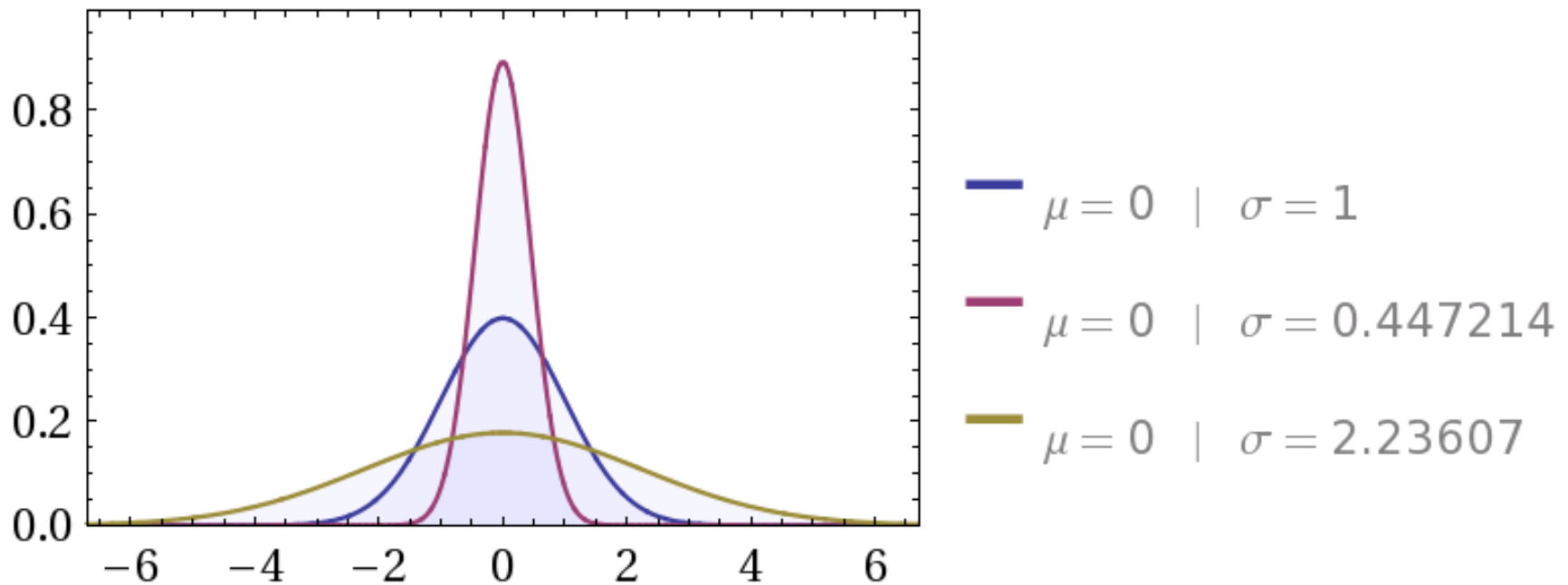
$$H(y_j) = \sum_{i=1}^n K(y_i - y_j)$$

Kernel



Choices for the kernel: Gaussian

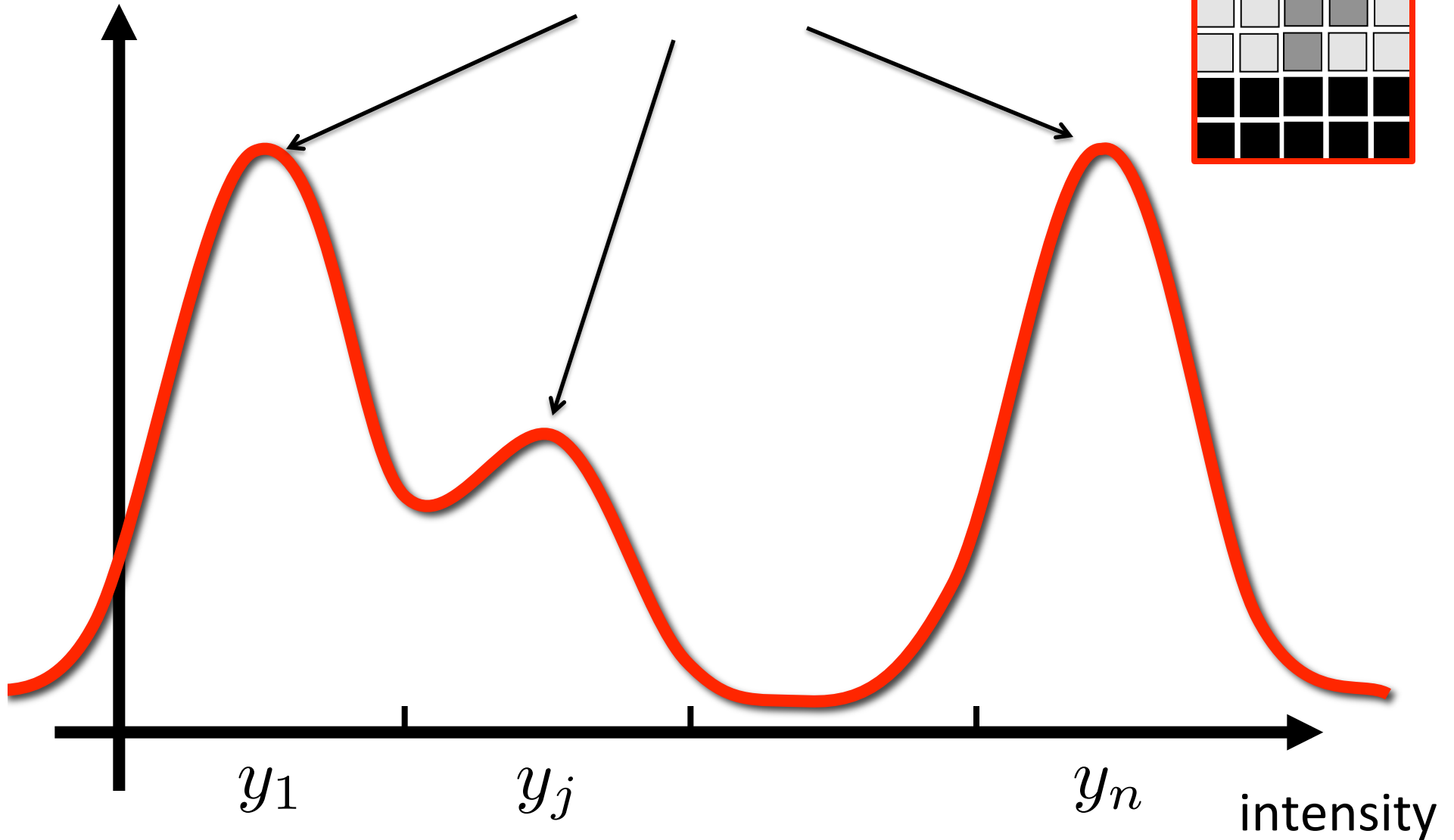
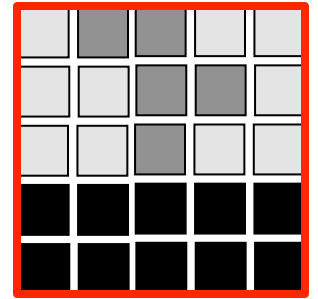
$$K(y_i - y_j) = \exp(-|y_i - y_j|^2 / \sigma^2)$$



Modes (peaks) of the Histogram

pixels

Peaks: How do we find them?



Mode Finding on the Histogram

Start with $H(y_j) = \sum_{i=1}^n K(y_i - y_j)$

Fix $y_j = t$

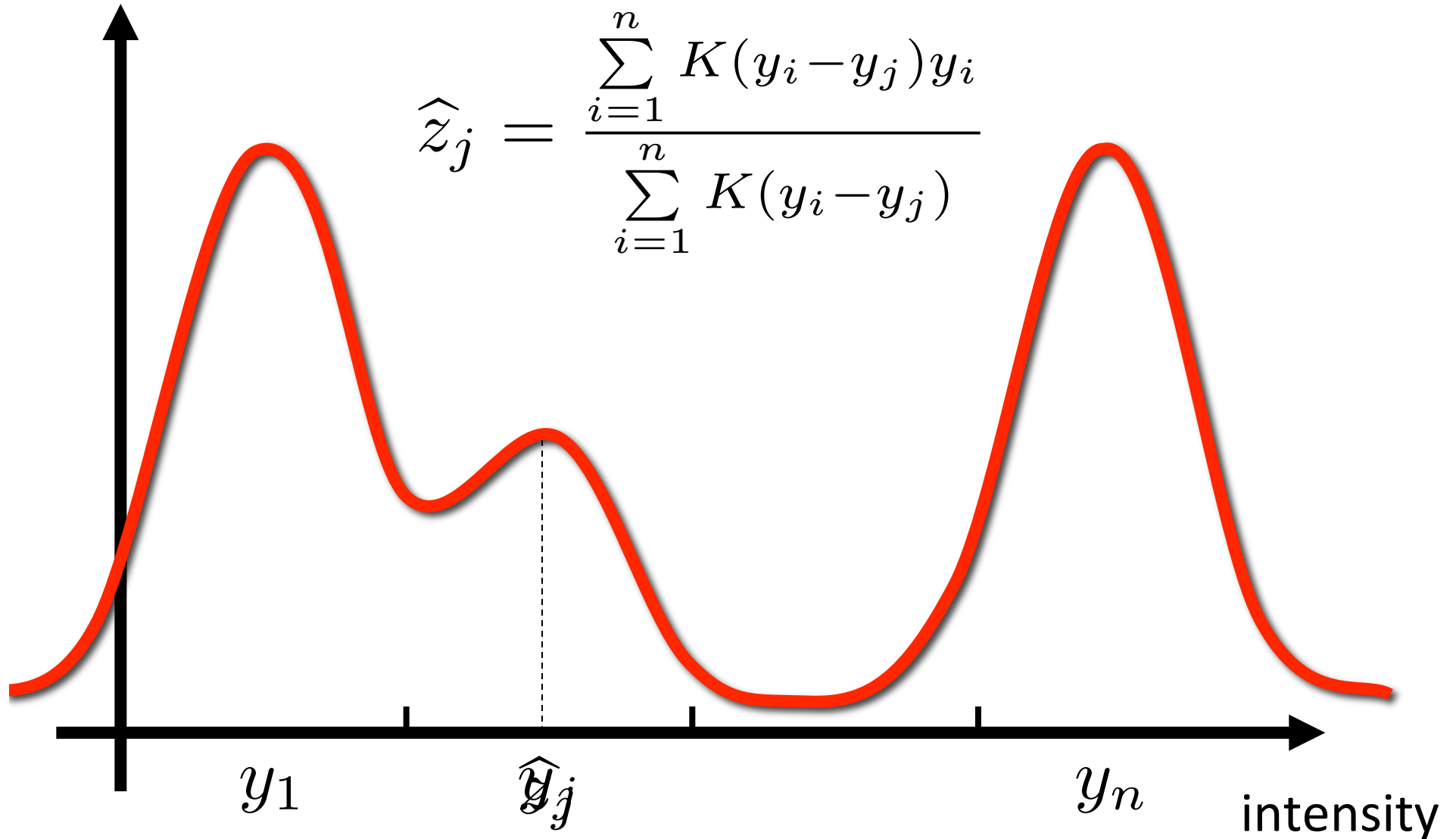
Differentiate and solve: $\frac{\partial H(t)}{\partial t} = 0$

$$\hat{z}_j = \frac{\sum_{i=1}^n K(y_i - y_j) y_i}{\sum_{i=1}^n K(y_i - y_j)}$$

(Assuming Gaussian Kernel, for now.)

Peak of the Histogram Nearest (in value) to y_j

pixels



Let's take a closer look

$$W_{ij} = \frac{K_{ij}}{\sum_i K_{ij}}$$

For each pixel, must normalize so the weights sum to 1.

$$\hat{z}_j = \sum_{i=1}^n W_{ij} y_i$$

Just a weighted average

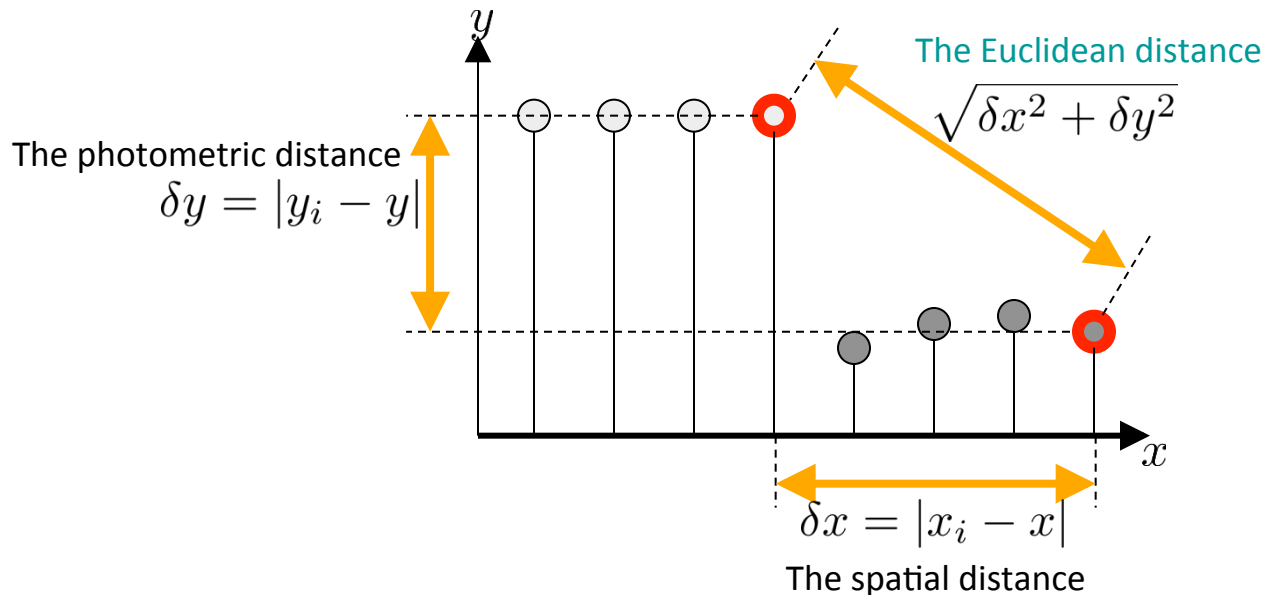
$$\sum_{i=1}^n W_{ij} = 1$$

Bilateral or non-local means kernels

Pixel values: $K(y_i - y_j) = \exp(-|y_i - y_j|^2 / h_y^2)$

Pixel positions: $K(x_i - x_j) = \exp(-|x_i - x_j|^2 / h_x^2)$

$$K_{ij} = K(y_i - y_j) K(x_i - x_j)$$



Faster Normalized Filtering

$$\hat{z}_j = \frac{\sum_{i=1}^n K_{ij} y_i}{\sum_{i=1}^n K_{ij}}$$

$$\hat{z}_j = \frac{\sum_{i=1}^n K_{ij} y_i}{\sum_{i=1}^n K_{ij} 1}$$

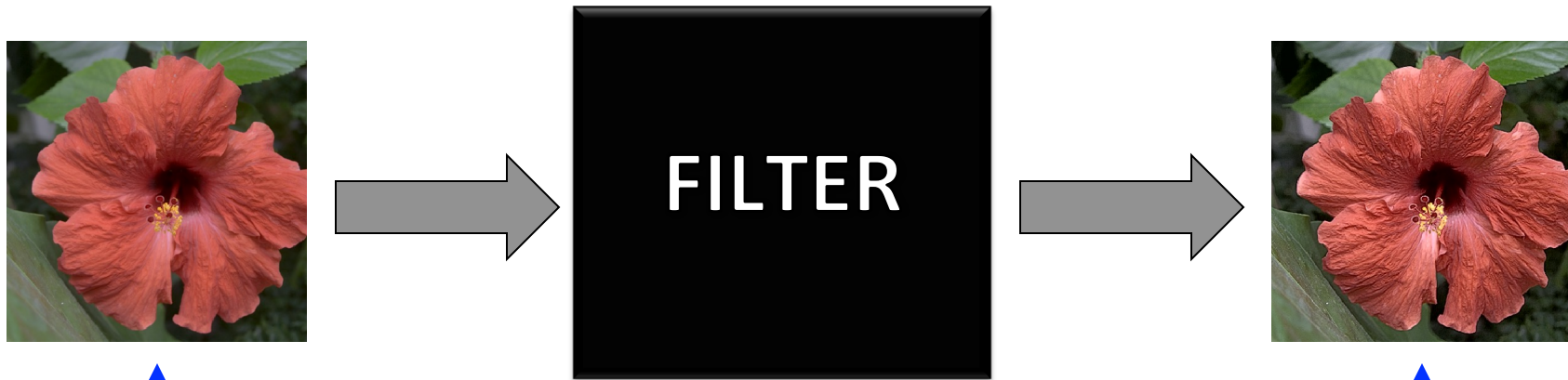
Filter once

Filter twice

$$\hat{z}_j = \frac{\sum_{i=1}^n K_{ij} y_i}{d_j}$$

Divide Pixel-wise

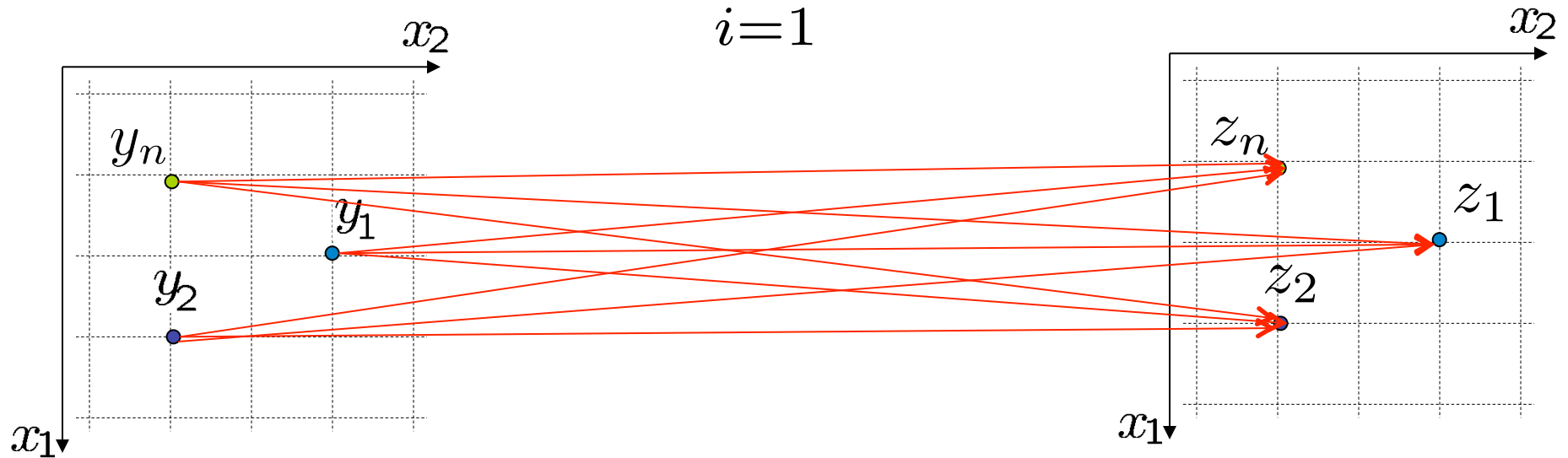
The Black Box



Input image

Output image

$$\hat{z}_j = \sum_{i=1}^n W_{ij} y_i$$



Global (or Local) Filters

Each output pixel $\longrightarrow \hat{z}_j = \sum_{i=1}^n W_{ij} y_i \longleftarrow$ All input pixels

$$\mathbf{w}_j^T = [W_{1j}, W_{2j}, \dots, W_{nj}]$$

$$\mathbf{W} = \begin{bmatrix} \mathbf{w}_1^T \\ \mathbf{w}_2^T \\ \vdots \\ \mathbf{w}_n^T \end{bmatrix}$$

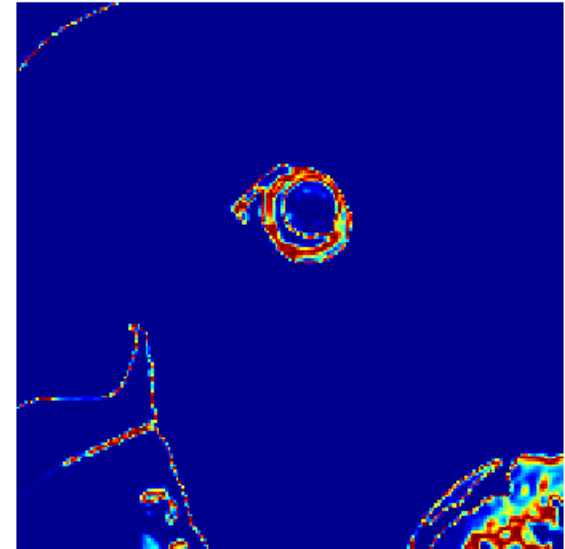
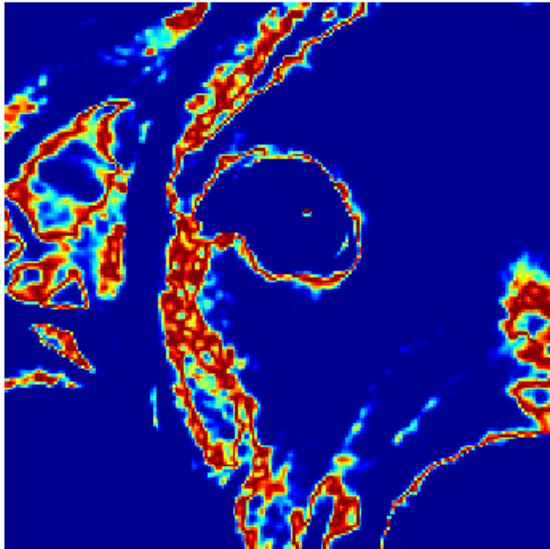
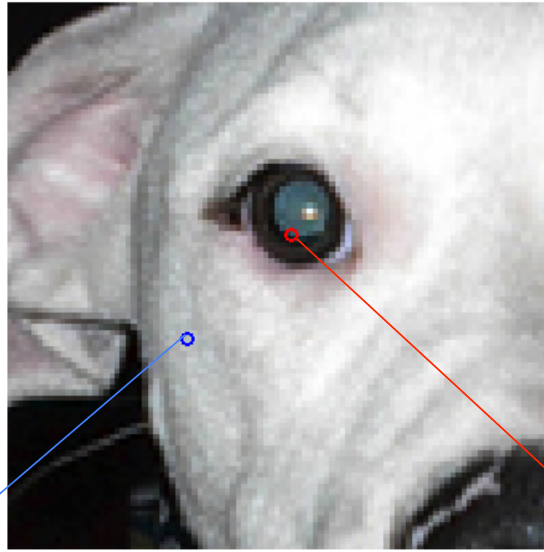
rows

$$\hat{\mathbf{z}} = \mathbf{W} \mathbf{y}$$

Data-dependent matrix

Image scanned into a vector

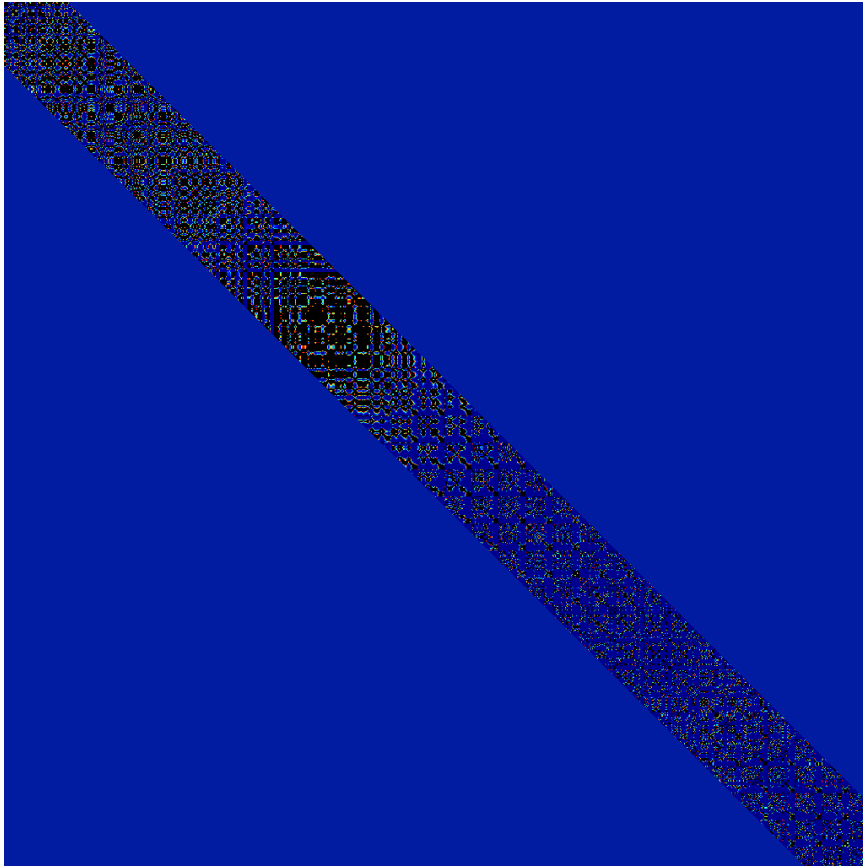
Global Affinities



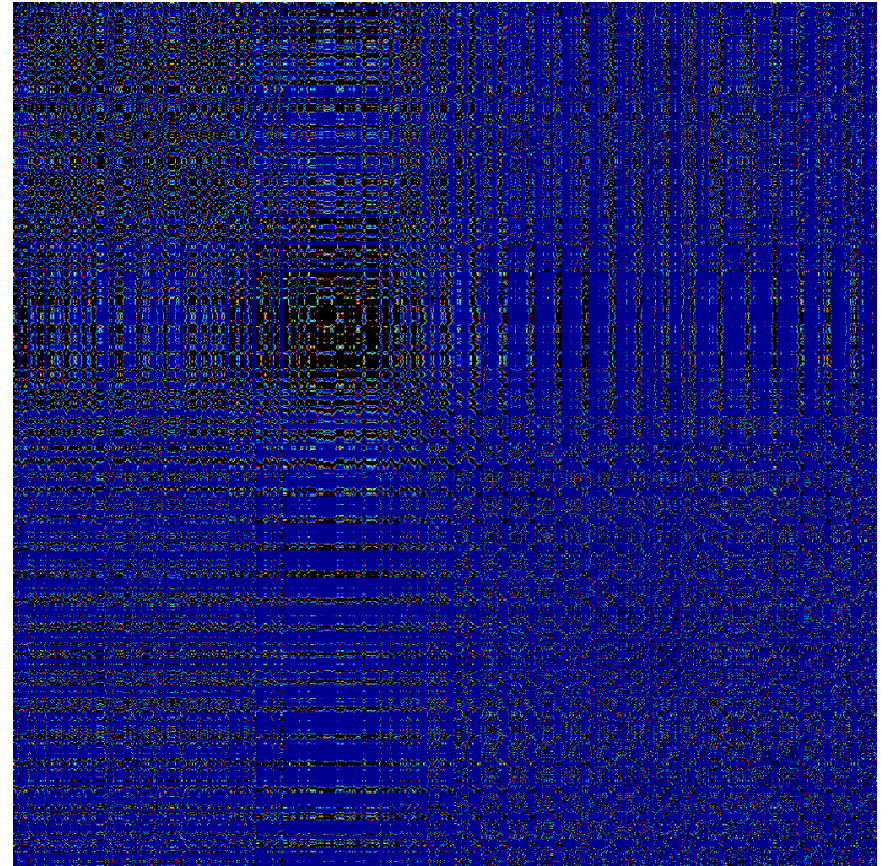
Local vs. Global Filter Matrix W

Local Filters

Global Filters



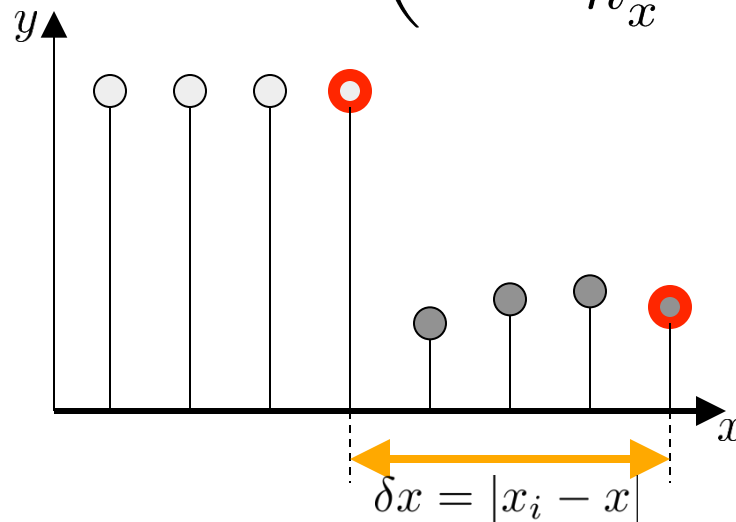
Sparse, but high-rank



Dense but low-rank

Choice of Kernels

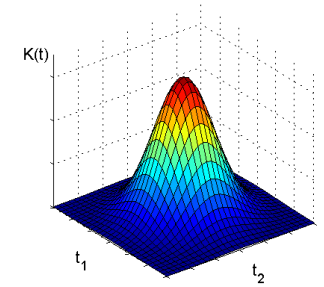
$$K(x_i - x_j) = \exp\left(\frac{-\|x_i - x_j\|^2}{h_x^2}\right)$$



The spatial distance



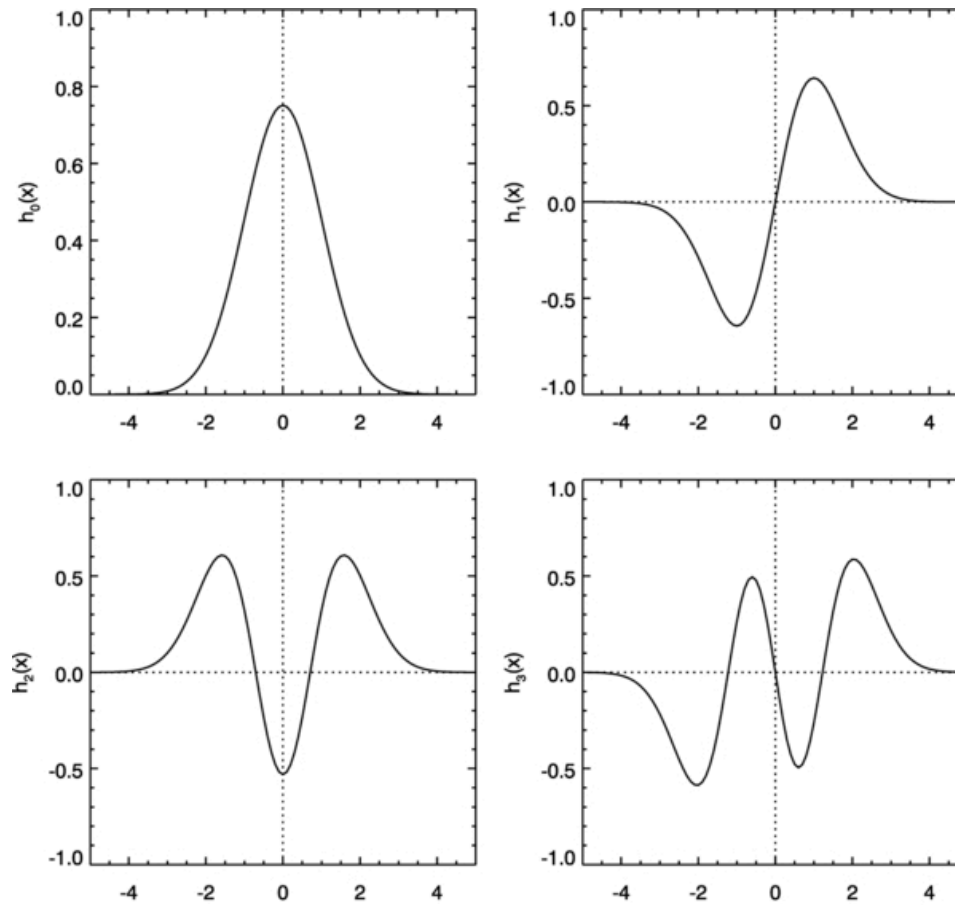
$$K(x_i - x)$$



- Classical Gaussian Linear Filters

Eigenvectors of Linear Gaussian Kernel

Hermite-Gauss functions

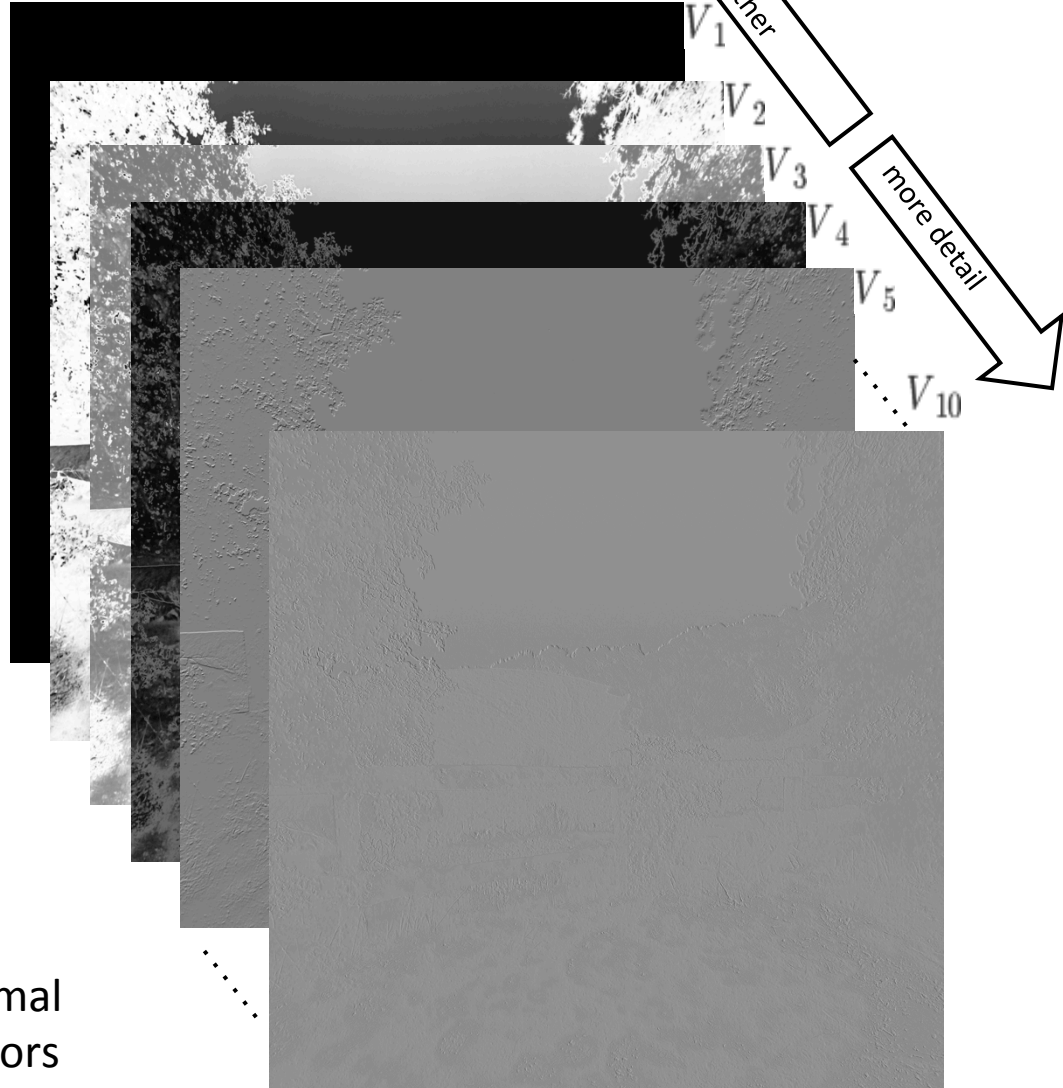


Eigenvectors of Linear Gaussian Kernel

Hermite-Gauss functions

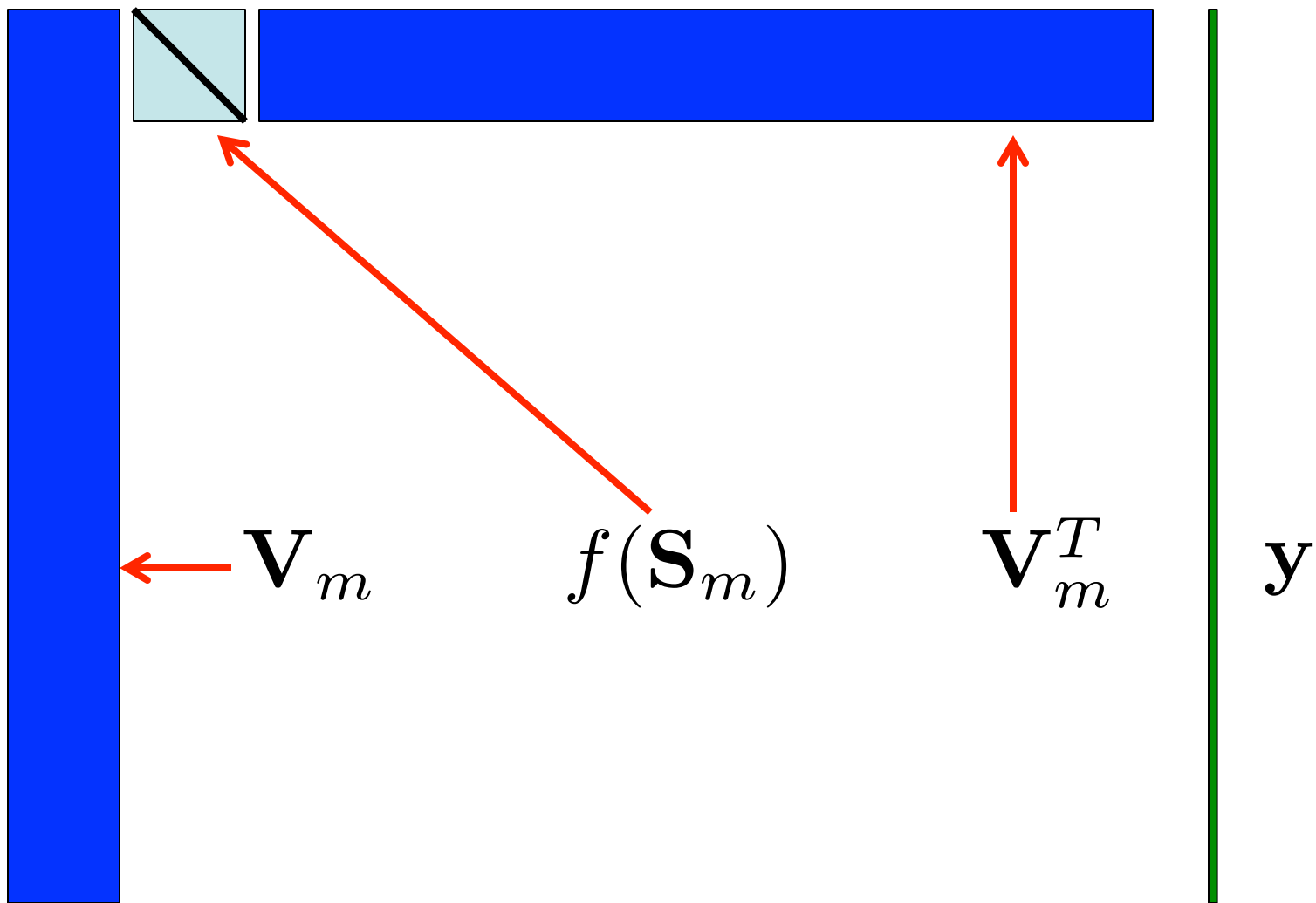


Filter Eigenvectors



Orthonormal
eigenvectors

Spectral Filtering in Lower Dimension



Low-light imaging



Denoised/Sharpened



Local Laplacian Filter



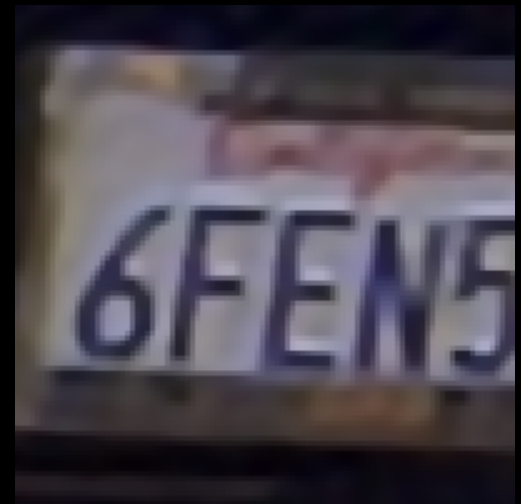
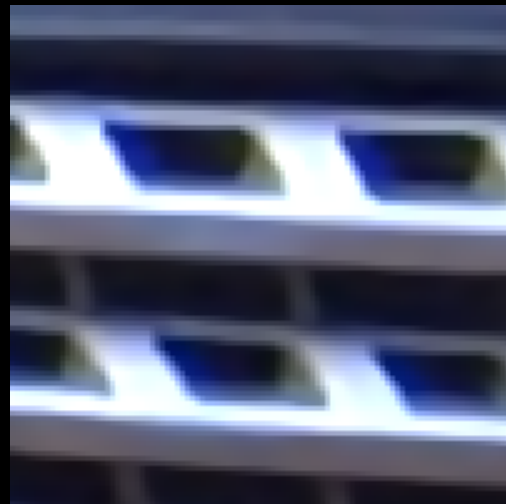
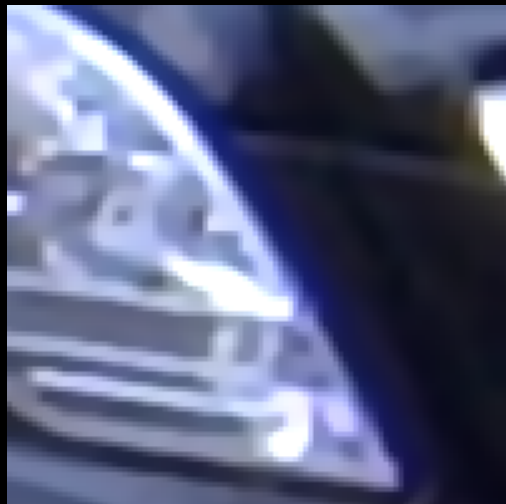
Multi-frame Upscaling/Zoom





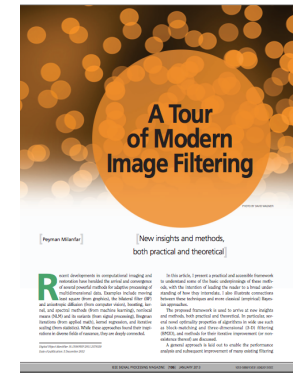
Fused 4 images, denoised and upscaled by 4x





Relevant Papers

- “A Tour of Modern Image Filtering”, P. Milanfar, IEEE Signal Processing Magazine, no. 30, pp. 106–128, Jan. 2013
- “A General Framework for Regularized, Similarity-based Image Restoration”, A. Kheradmand, and P. Milanfar, IEEE Trans on Image Processing, vol. 23, no. 12, Dec. 2014
- “Global Image Denoising”, H. Talebi, and P. Milanfar, IEEE Trans on Image Processing, vol. 23, no. 2, pp. 755-768, Feb. 2014
- “Nonlocal Image Editing”, H. Talebi, and P. Milanfar, IEEE Trans on Image Processing, vol. 23, no. 10, Oct. 2014



<http://milanfar.org>