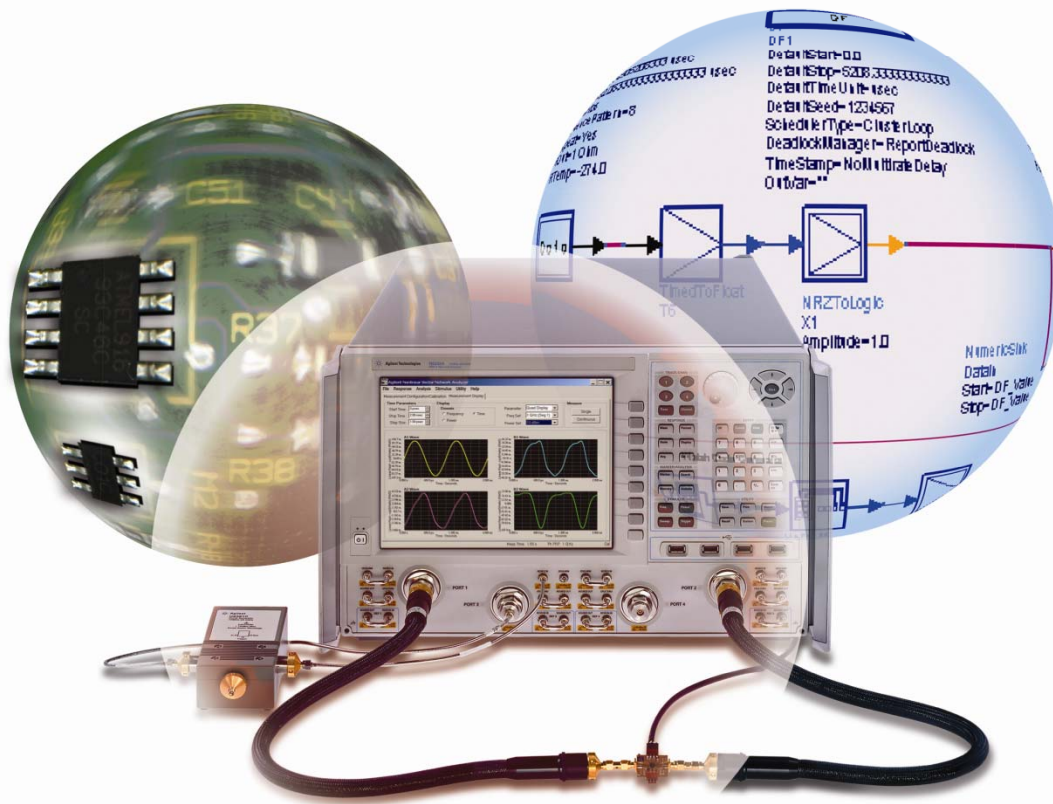


# X-parameters\*:

A new paradigm for measurement, modeling, and design of nonlinear microwave & RF components



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Santa Rosa, CA USA

IEEE MTT-S DML Lecture #2  
Bergen, Norway  
May 7, 2010

\* X-parameters is a trademark of Agilent Technologies, Inc.

# Key Contributors

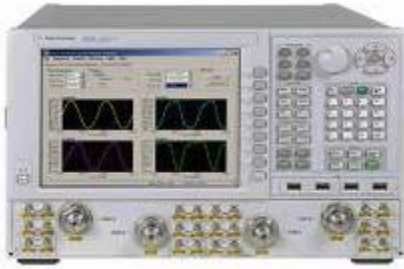
- Keith Anderson
- Loren Betts
- Radek Biernacki
- Chad Gillease
- Daniel Gunyan
- John Harmon
- Jason Horn
- Yuchen Hu
- Masaya Iwamoto
- Mihai Marcu
- Troels Nielson
- Greg Peters
- Mark Pierpoint
- Jack Sifri
- Mary Lou Simmermacher
- Gary Simpson
- Franz Sischka
- Darlene Solomon
- Tina Sun
- Yee Ping Teoh
- Dan Thomasson
- Jan Verspecht
- Kenn Wildnauer
- Jianjun Xu
- Yoshiyuki Yanagimoto

# Outline

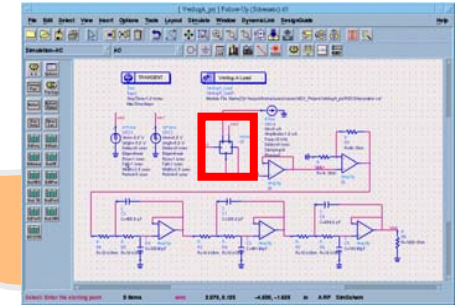
- Introduction: X-parameter Basics
- Survey of X-parameter benefits and applications
- Summary
- References and Links

# X-Parameters: Mainstream Nonlinear Interoperable Technology

Agilent Nonlinear Vector Network Analyzer



Electronic design automation software

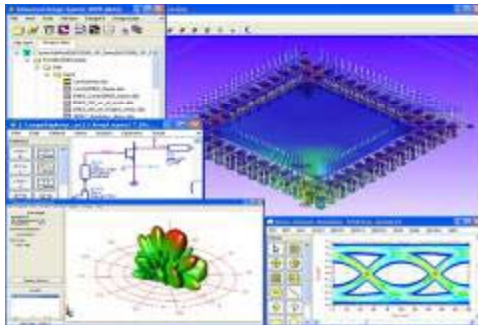


Nonlinear Measurements

Nonlinear Simulation & Design

Nonlinear Modeling

Customer Applications



$$B_{pm} = X_{pm}^F(A_{11}) + X_{pm,qn}^S(A_{11})P^{m-n}A_{qn} + X_{pm,qn}^T(A_{11})P^{m+n}A_{qn}^*$$

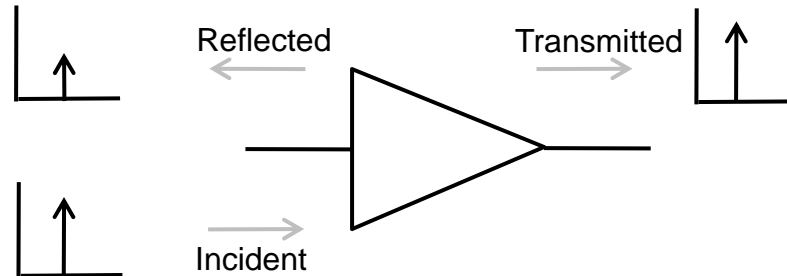
# S-parameters Solve All Small-Signal Problems

But devices must operate linearly

Measure



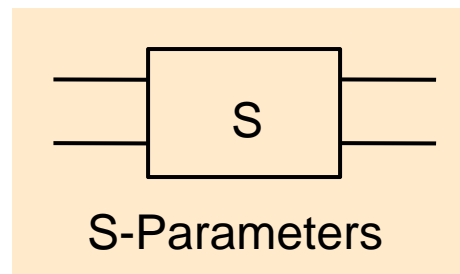
Agilent Vector Network Analyzer



Model

$$B_1 = S_{11}A_1 + S_{12}A_2$$

$$B_2 = S_{21}A_1 + S_{22}A_2$$



S-Parameters

Design

S-PARAMETERS

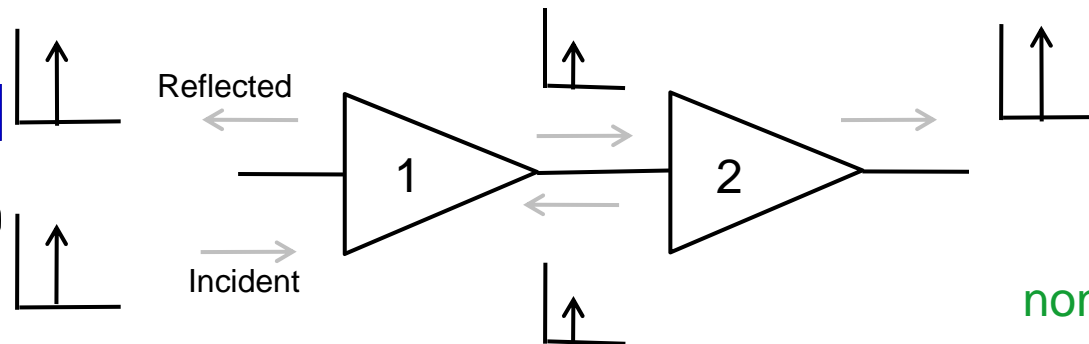
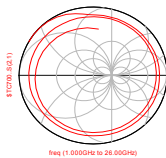
S\_Param

SP1

Start=1.0 GHz

Stop=10.0 GHz

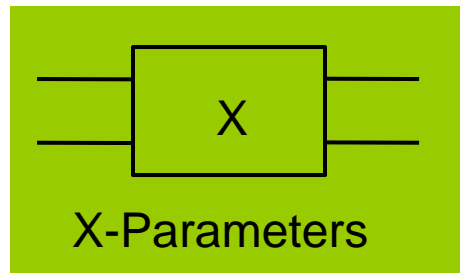
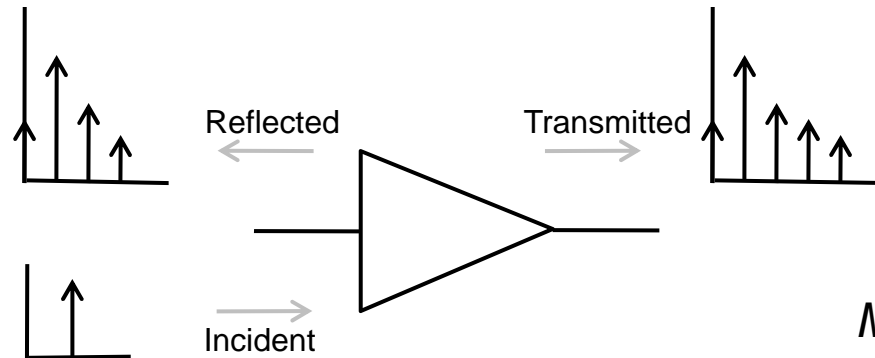
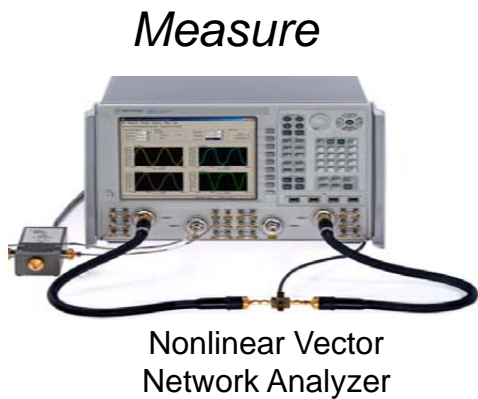
Step=0.1 GHz



What about large-signal nonlinear problems?

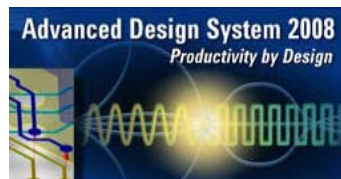
# X-parameters Solve Nonlinear Problems

Same use model as S-parameters, *but much more powerful*

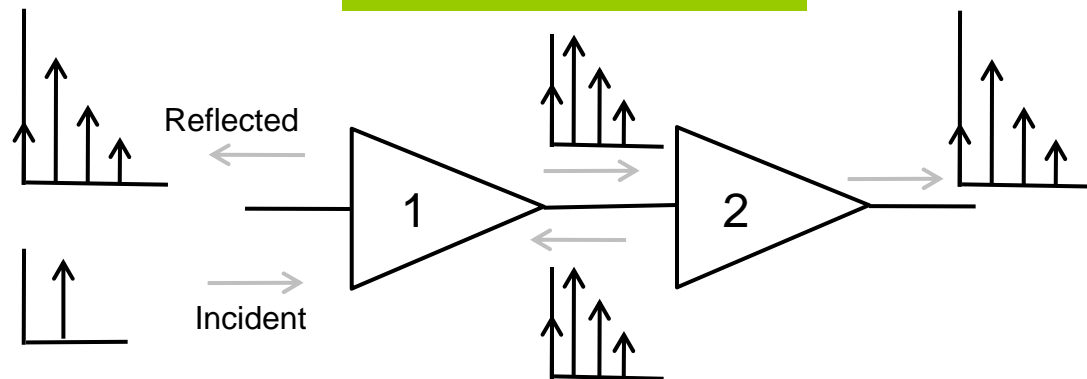


*Model*

$$B_{pm} = X_{pm}^F (|A_{11}|) P^m + X_{pm,qn}^S (|A_{11}|) P^{m-n} A_{qn} + X_{pm,qn}^T (|A_{11}|) P^{m+n} A_{qn}^*$$



EDA Software





# Capturing the imagination of the industry

Solves real-world problems now

Interoperable characterization, modeling, and design solutions

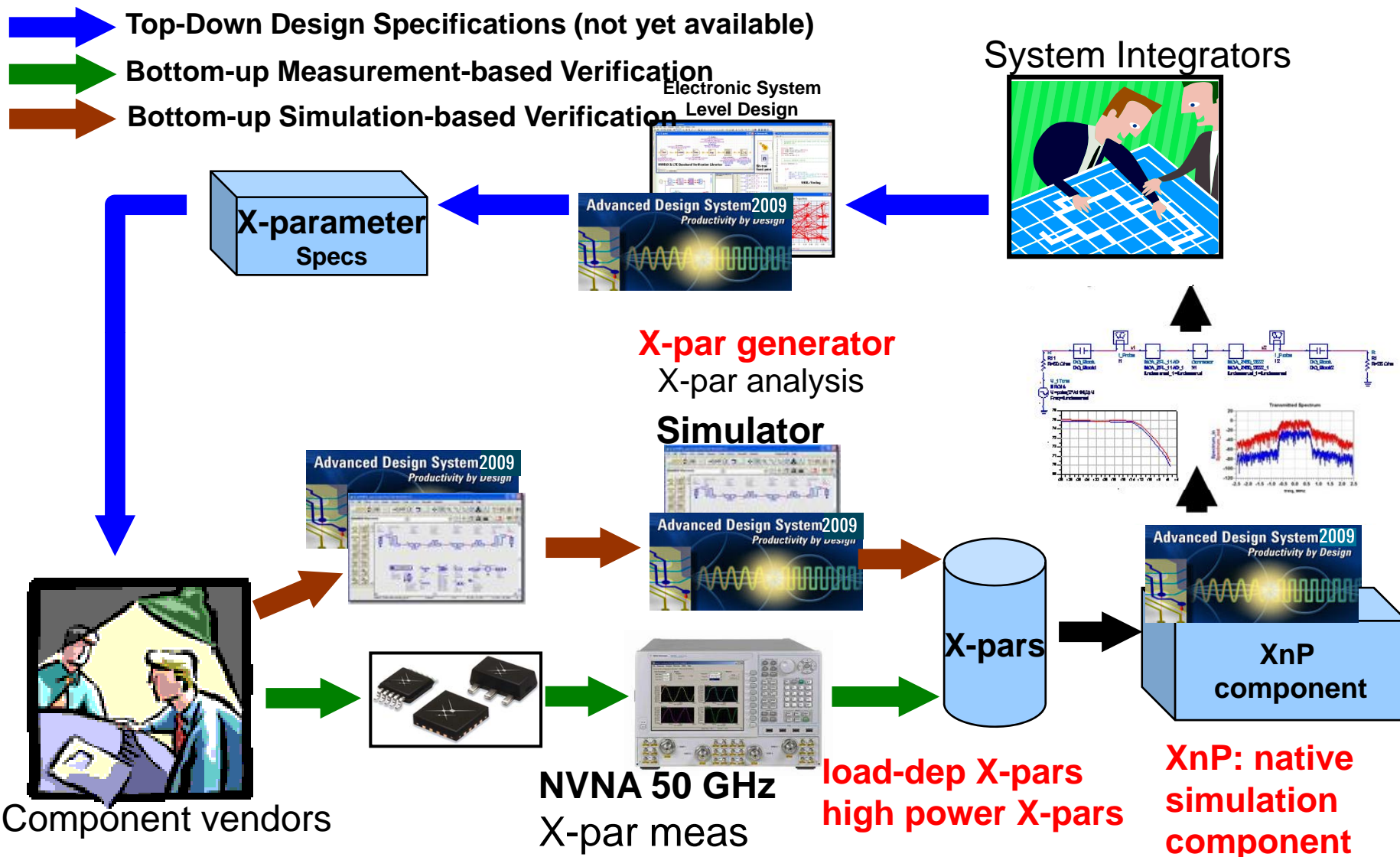
Potential to do for nonlinear components and systems what S-parameters do for linear components and systems

Changing the way the industry works

Continuous wave of innovations and award-winning research

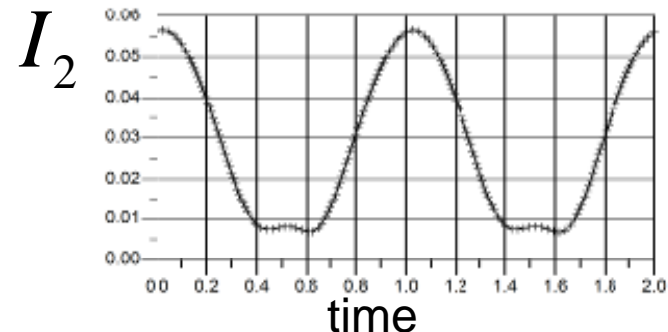
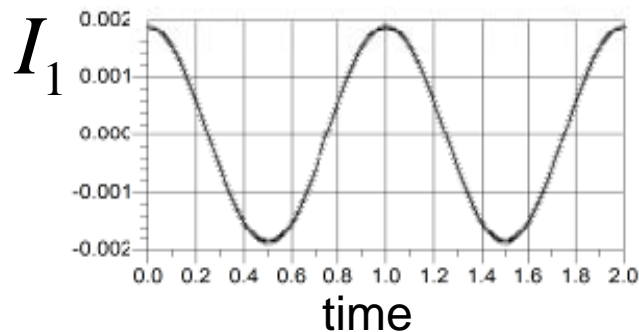
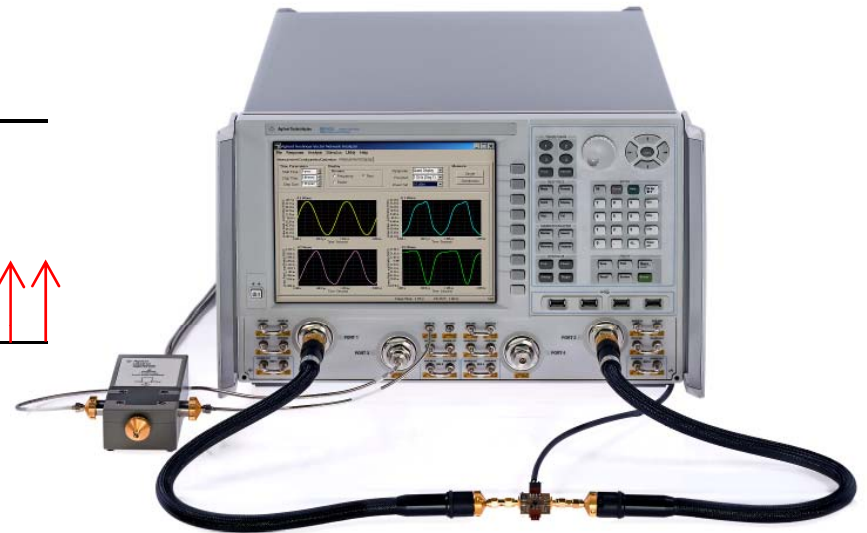
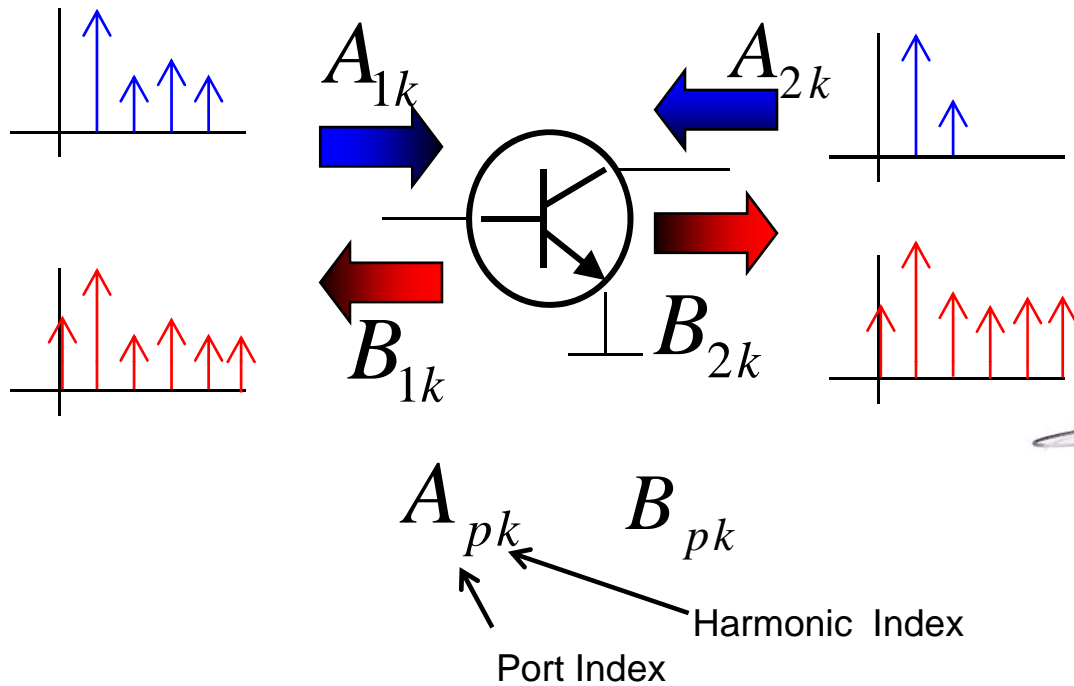


# X-parameters: Hierarchical Design and Validation





# Introduction: NVNA measurements complex spectra and waveforms

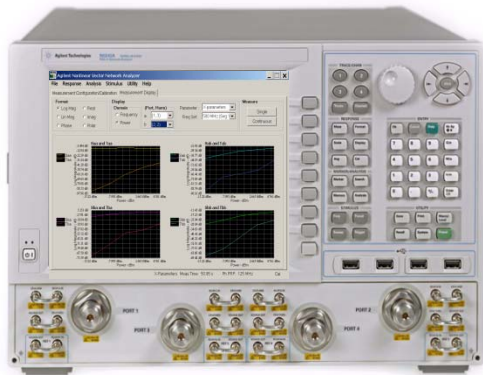


# Measurement-Based Modeling & Design Flow

“X-parameters enable predictive nonlinear design from NL data”

NVNA

Nonlinear Measurements

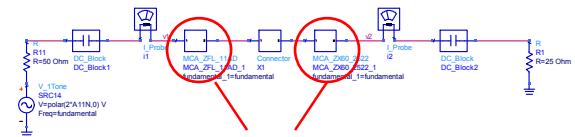


Data File

Drag and drop

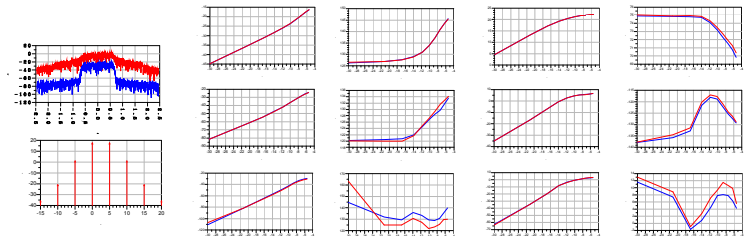
ADS

Simulation and Design



X-parameter blocks

X-parameters enable accurate nonlinear simulation under small to moderate mismatch. (See later for large mismatch)



allowing prediction of component behavior in complicated nonlinear circuits.

IMD / ACPR exact in narrow-band limit

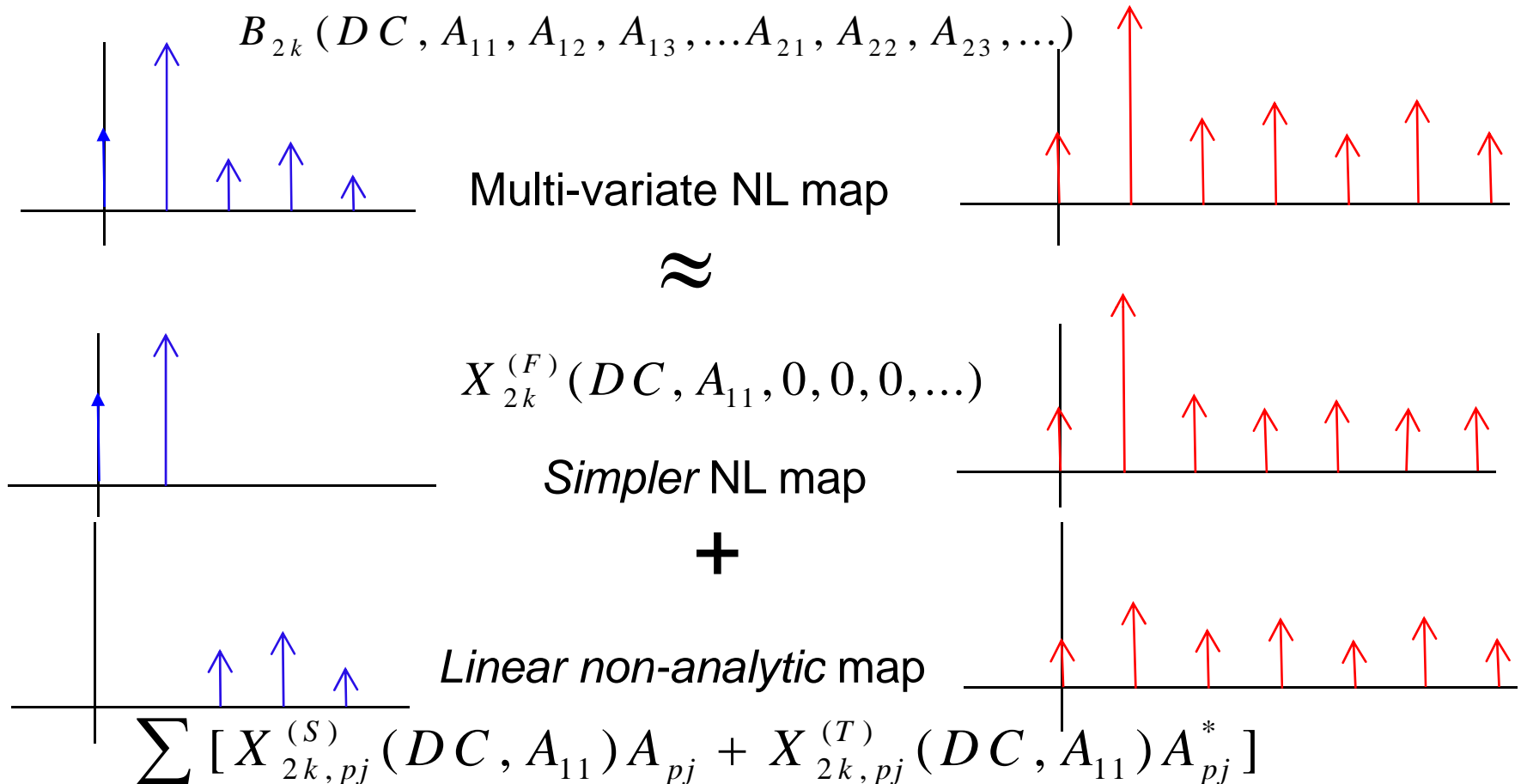


“X-parameters: the same use model as S-parameters *but much more powerful*”

# X-parameter Concept: Linearized Spectral Map around a Large-Signal Operating Point (LSOP)

Incident Port 1

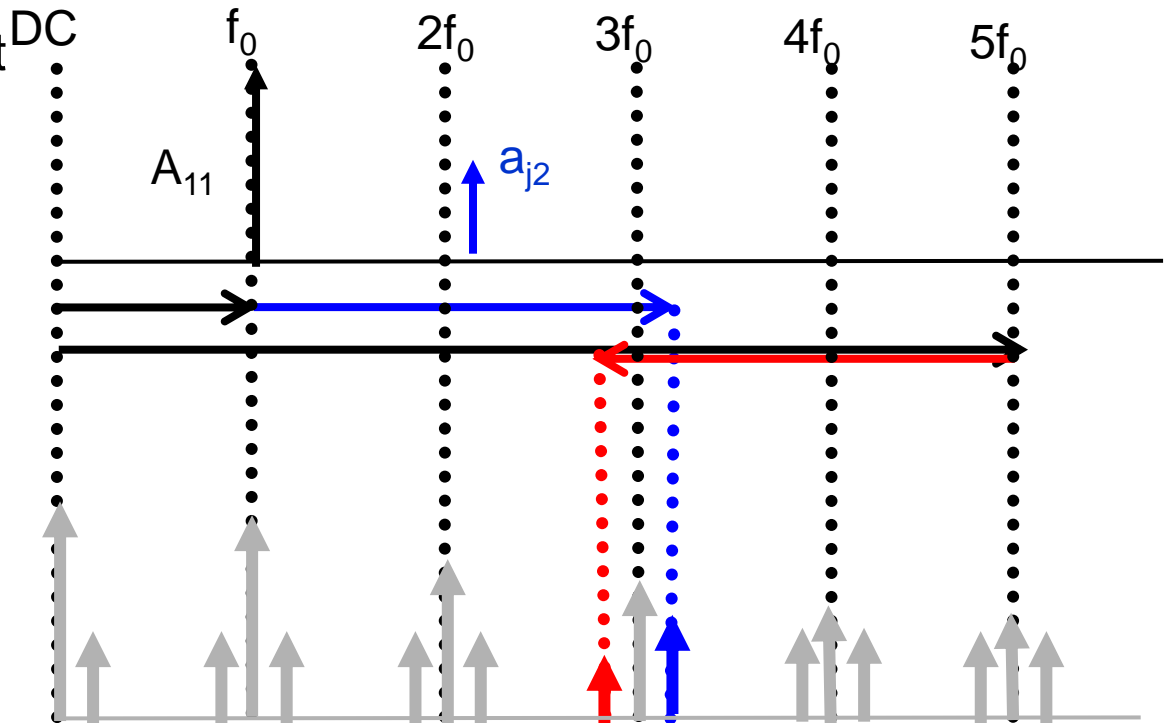
Scattered Port 2



X-pars include exact nonlinear mapping to totally linear (S-pars) & everything in between  
*Trade simplicity for accuracy.*

# X-parameters: What they are & where they come from

- Scattering of multiple incident large-amplitude waves.
- Can be simplified according to linear or nonlinear dependence on inputs (simplicity vs accuracy)
- Measured on NVNA or generated in simulator
- Rules for computing the response to general signals given extracted X-parameters



$$X_{i3,j2}^{(T)} a_{j2}^* \quad X_{i3}^{(F)} \quad X_{i3,j2}^{(S)} a_{j2}$$

$$5f_0 - f_1 \quad 3f_0 \quad f_0 + f_1$$

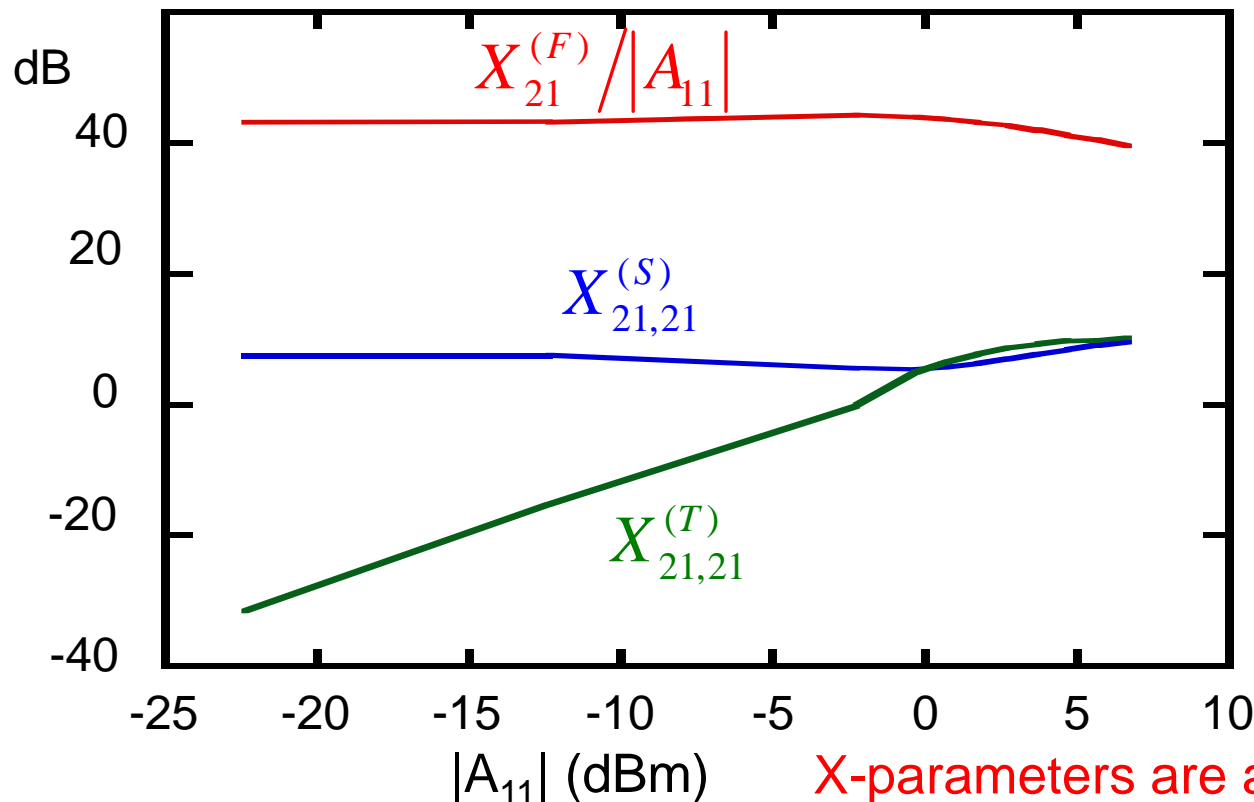
$$B_{e,f} = X_{ef}^{(F)}(|A_{11}|)P^f + \sum_{g,h} X_{ef,gh}^{(S)}(|A_{11}|)P^{f-h} \cdot a_{gh} + \sum_{g,h} X_{ef,gh}^{(T)}(|A_{11}|)P^{f+h} \cdot a_{gh}^* \quad P = e^{j\varphi(A_{11})}$$

# Simplest X-parameters for a Power Amplifier

$$B_{11}(|A_{11}|) = X_{11}^{(F)}(|A_{11}|)P + X_{11,21}^{(S)}(|A_{11}|)A_{21} + X_{11,21}^{(T)}(|A_{11}|)P^2 A_{21}^*$$

$$B_{21}(|A_{11}|) = X_{21}^{(F)}(|A_{11}|)P + X_{21,21}^{(S)}(|A_{11}|)A_{21} + X_{21,21}^{(T)}(|A_{11}|)P^2 A_{21}^*$$

X-parameters reduce to (linear) S-parameters in the appropriate limit



$$X_{11}^{(F)} / |A_{11}| \xrightarrow{|A_{11}| \rightarrow 0} S_{11}$$

$$X_{21}^{(F)} / |A_{11}| \xrightarrow{|A_{11}| \rightarrow 0} S_{21}$$

$$X_{11,21}^{(S)}(|A_{11}|) \xrightarrow{|A_{11}| \rightarrow 0} S_{12}$$

$$X_{21,21}^{(S)}(|A_{11}|) \xrightarrow{|A_{11}| \rightarrow 0} S_{22}$$

$$X_{11,21}^{(T)}(|A_{11}|) \xrightarrow{|A_{11}| \rightarrow 0} 0$$

$$X_{21,21}^{(T)}(|A_{11}|) \xrightarrow{|A_{11}| \rightarrow 0} 0$$

X-parameters are a *superset* of S-parameters

# X-parameter Experiment Design & Identification [1,14]

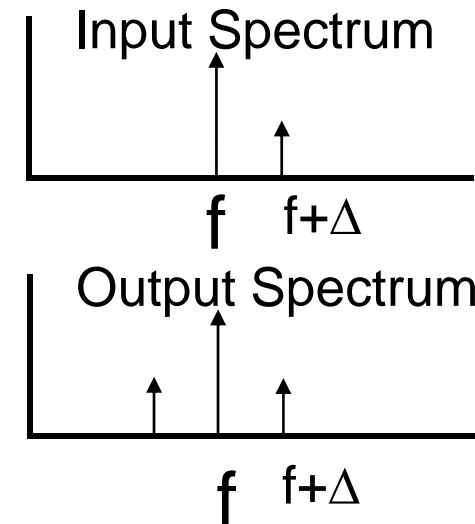
Stimulate port 1 with large tone at freq.  $f$   
Stimulate port 2 with small tone at freq.  $f + \Delta$   
Measure response at three different frequencies  
Take limit as  $\Delta$  goes to zero

$$X_{21}^{(F)} = B_{21}(f, |A_{1,1}|) P^{-1}$$

$$X_{21,21}^{(S)} = \frac{B_{21}(f + \Delta, |A_{11}|)}{A_{21}(f + \Delta)}$$

$$X_{21,21}^{(T)} = \frac{B_{21}(f - \Delta, |A_{11}|)}{A_{21}(f + \Delta)} e^{2j\phi(A_{11} - A_{21})}$$

Similarly for harmonics



*Optimal and orthogonal*  
experiment design and model  
identification



# X-Parameters and the Harmonic Jacobian [1]

X-parameters are the “modeling analog” of HB analysis  
 Write model equations in language native to simulator algorithms

From 1-tone HB analysis  $X_{pm}^{(F)}(|A_{11}|) = B_{pm} P^{-m}$

$$X_{pm,qn}^{(S)}(|A_{11}|) = P^{-m+n} \left. \frac{\partial B_{pm}}{\partial A_{qn}} \right|_{A_{11}, A_{12}=0, \dots, A_{21}=0, \dots}$$

$$X_{pm,qn}^{(T)}(|A_{11}|) = P^{-m-n} \left. \frac{\partial B_{pm}}{\partial A_{qn}^*} \right|_{A_{11}, A_{12}=0, \dots, A_{21}=0, \dots}$$

from *known Jacobian of 1-tone HB analysis*.

Jacobian comes from I-V and  $G_{ij}$ ,  $C_{ij}$  from element constitutive relations

Never need 2-tone HB analysis. Faster, guaranteed spectrally linear

Most of the terms in the required Jacobian *are known ahead of time*

$$B_{e,f} = X_{ef}^{(F)}(|A_{11}|)P^f + \sum_{g,h} X_{ef,gh}^{(S)}(|A_{11}|)P^{f-h}A_{gh} + \sum_{g,h} X_{ef,gh}^{(T)}(|A_{11}|)P^{f+h}A_{gh}^*$$

# X-Parameter: How they are measured:

## Experiment Design & Identification (2): Ideal Case

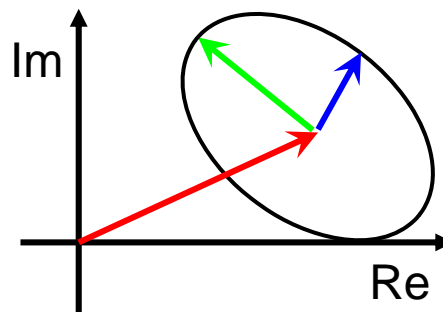
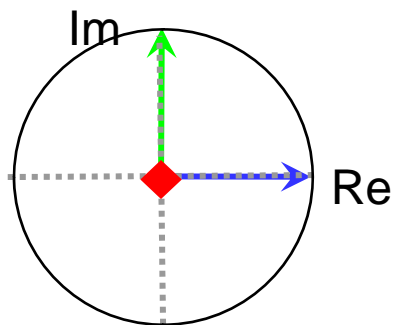
E.g. functions for  $B_{pm}$  (port p, harmonic m) given small extraction tones  $A_{qn}$  (port q, harmonic n)

$$B_{pm} = \underbrace{X_{pm}^{(F)}(|A_{11}|)}_{\text{red}} P^m + \underbrace{X_{pm,qn}^{(S)}(|A_{11}|)}_{\text{green}} P^{m-n} A_{qn} + \underbrace{X_{pm,qn}^{(T)}(|A_{11}|)}_{\text{blue}} P^{m+n} A_{qn}^*$$

Perform 3 independent experiments with fixed  $A_{11}$

input  $A_{qn}$

output  $B_{pm}$



$$B_{pm}^{(0)} = X_{pm}^{(F)}(|A_{11}|) P^n$$

$$B_{pm}^{(1)} = X_{pm}^{(F)}(|A_{11}|) P^m + X_{pm,qn}^{(S)}(|A_{11}|) P^{m-n} A_{qn}^{(1)} + X_{pm,qn}^{(T)}(|A_{11}|) P^{m+n} A_{qn}^{(1)}$$

$$B_{pm}^{(2)} = X_{pm}^{(F)}(|A_{11}|) P^m + X_{pm,qn}^{(S)}(|A_{11}|) P^{m-n} A_{qn}^{(2)} + X_{pm,qn}^{(T)}(|A_{11}|) P^{m+n} A_{qn}^{(2)*}$$

# X-parameter properties and benefits

Static nonlinearity (AM-AM) at any/all CW frequencies

High-frequency memory (AM-PM)

Large-signal output match (correct “Hot S22”)

Harmonics (even and odd) at input and output ports

PAE and DC currents / voltages at supply ports

**Cascadable:** distortion through chains of components

*Does for driven nonlinear systems what S-parameters do for linear systems*

**Hierarchical:** apply to one component or multiple (e.g. multi-stage amp)

**Transportable:** mismatch at fundamental and harmonics taken into account

Can be used to simulate some *long-term memory* affects

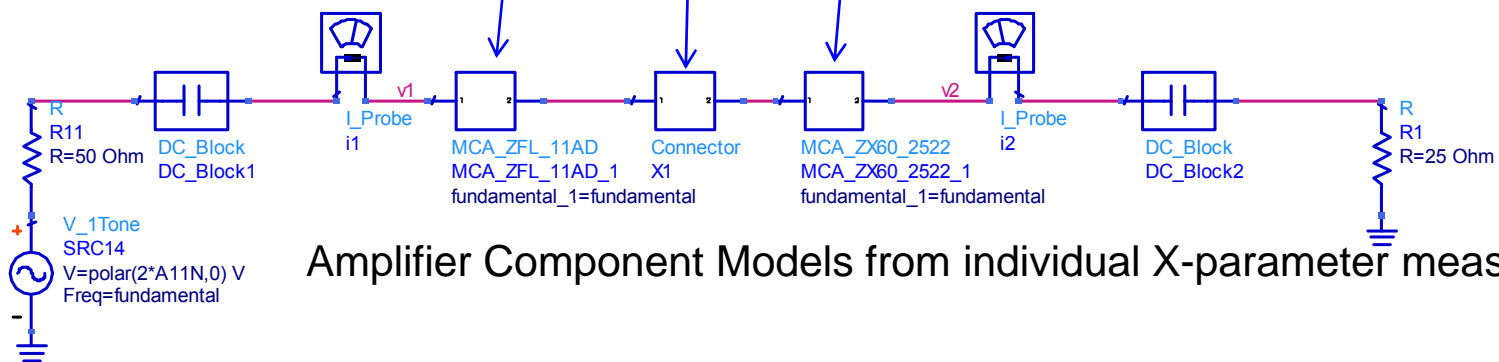
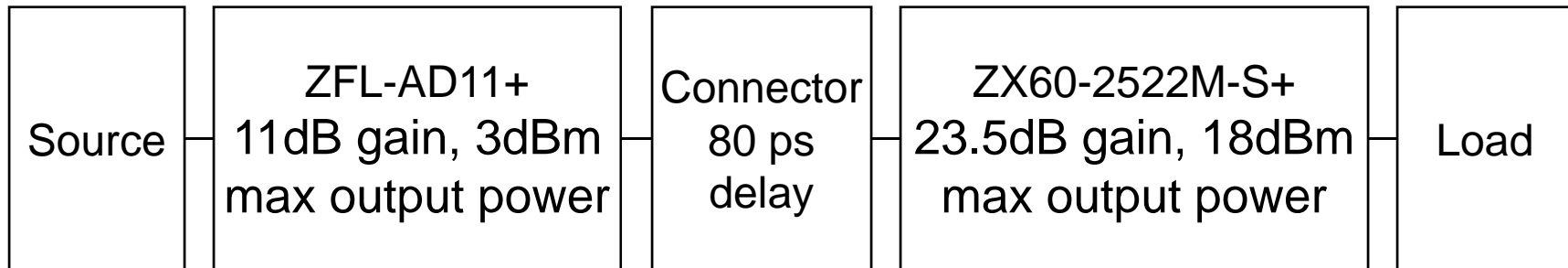
Can be *generated from Simulation and Measurement*

*Highly automated experiment design & model identification*

# Outline

- Introduction: X-parameter Basics
- Survey of X-parameter benefits and applications
  - Cascading nonlinear blocks
  - Integrating handset amplifier into cell phone (customer example)
  - Load-dependent X-parameters and their harmonic tuning capability
  - High power X-parameter measurements
  - X-parameter generation from detailed schematics in ADS
  - X-parameter simulation component (XNP) built-in to ADS
  - Dynamic X-parameters: Long-term memory research
- Summary
- References and Links

# Measurement-based nonlinear design with X-parameters



Amplifier Component Models from individual X-parameter measurements

# Results

## Cascaded Simulation vs. Measurement

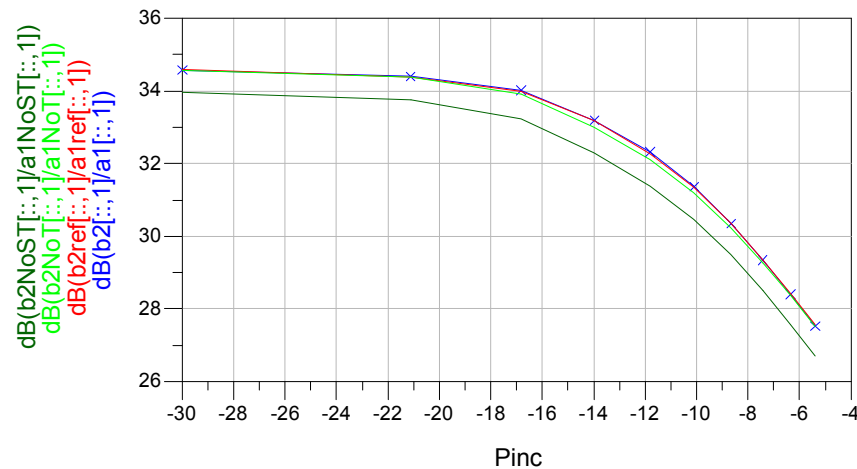
Red: Cascade Measurement

Blue: Cascaded X-parameter Simulation

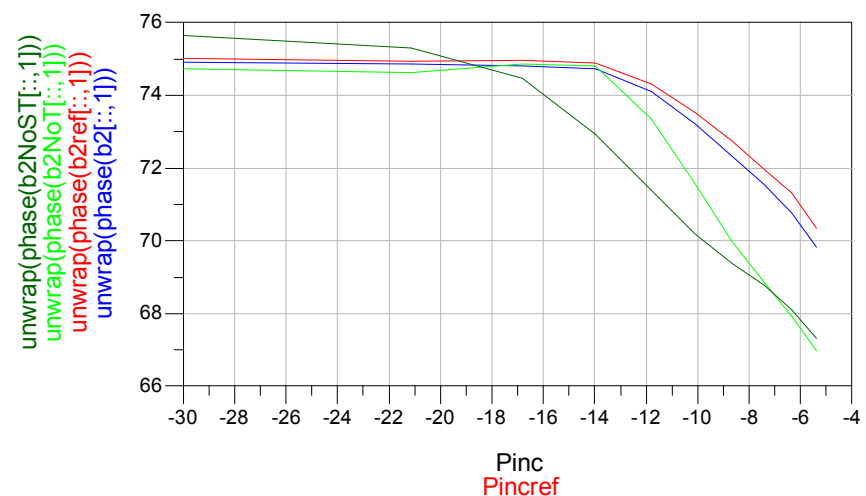
Light Green: Cascaded Simulation, No  $X^{(T)}$  terms

Dark Green: Cascaded Models, No  $X^{(S)}$  or  $X^{(T)}$  terms

### Fundamental Gain



### Fundamental Phase





# Results

## Cascaded Simulation vs. Measurement

Red: Cascade Measurement

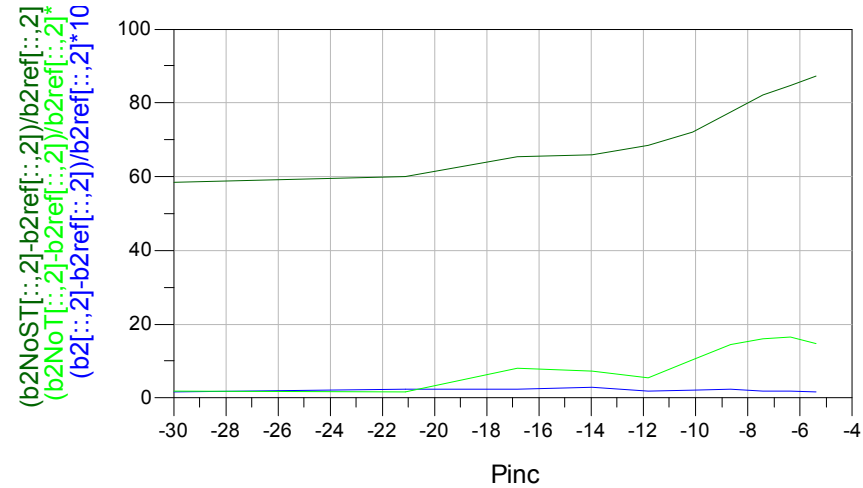
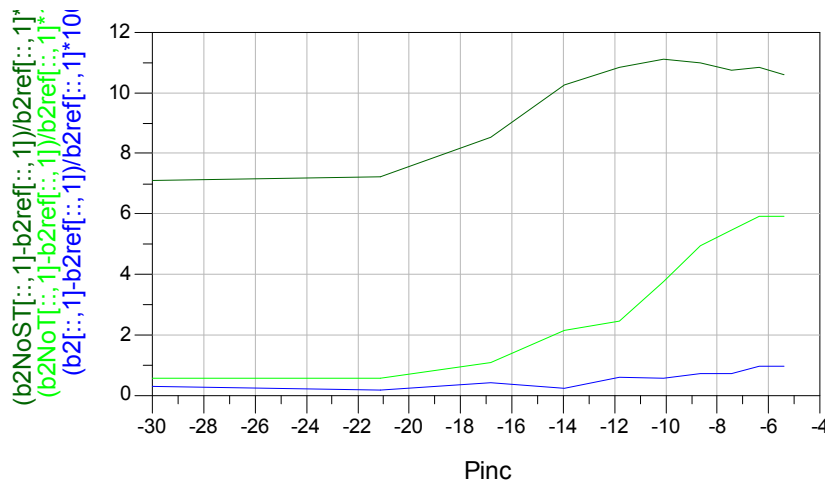
Blue: Cascaded X-parameter Simulation

Light Green: Cascaded Simulation, No  $X^{(T)}$  terms

Dark Green: Cascaded Models, No  $X^{(S)}$  or  $X^{(T)}$  terms

Fundamental % Error

Second Harmonic % Error



“X-parameters enable predictive nonlinear design from NL data”

# X-parameters solve key, real customer problems

## Example: GSM amp. and cell phone integration

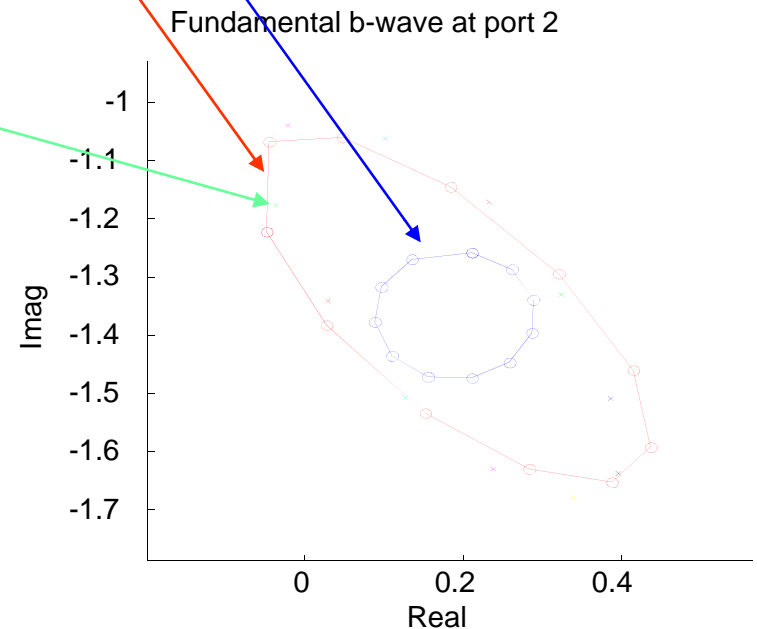
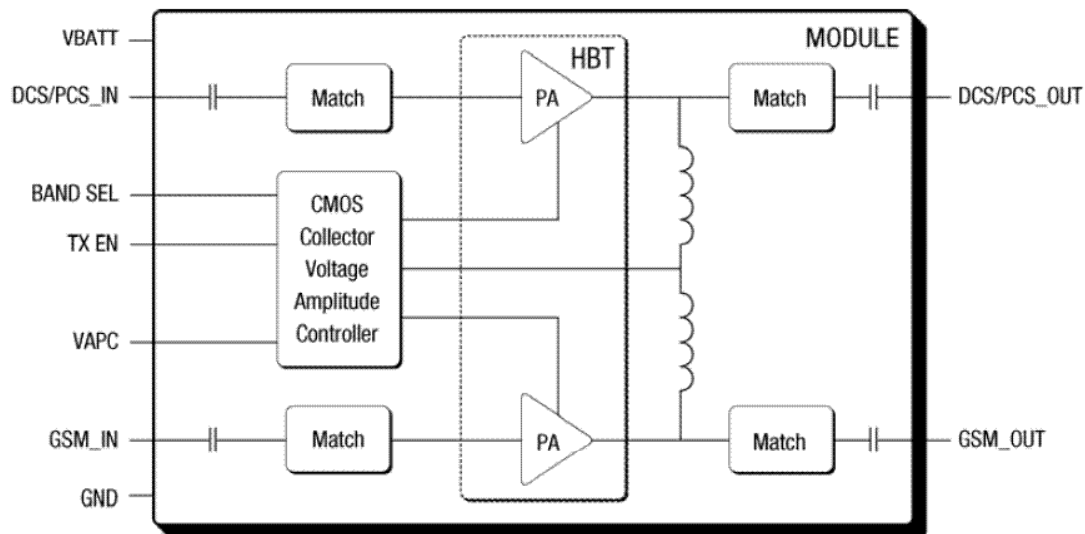
Horn et al *IEEE European Microwave Conference*, Amsterdam, October 2008

Blue circular shape Hot  $S_{22}$  prediction

Red Elliptical shape: X-parameter prediction

Measurements  
small colored crosses

Skyworks amp

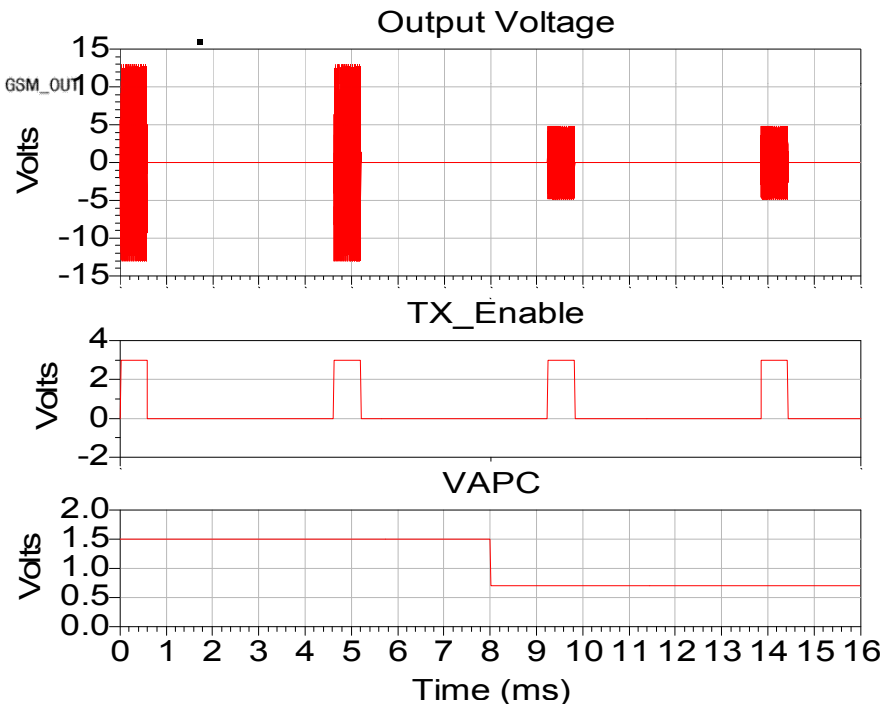
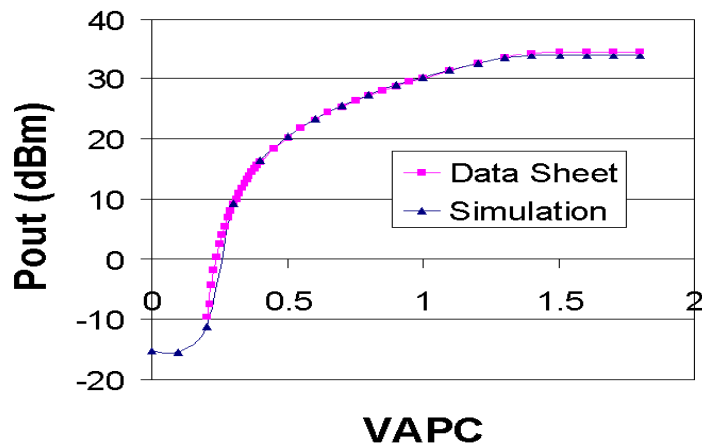
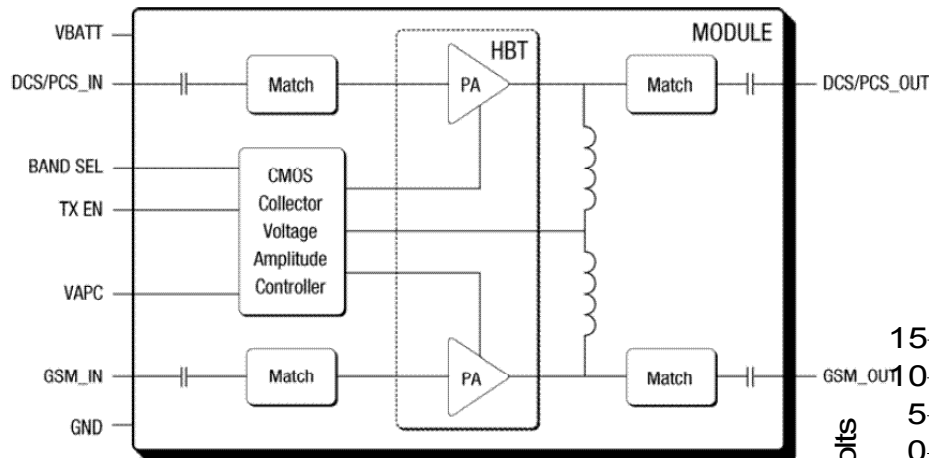


Allowed *Sony-Ericsson* to take into account second-harmonic mismatch on amp in system integration

“X-parameters predict output match under large input drive *Hot  $S_{22}$  does not*”

# Complete X-parameter Model of GSM Amplifier

“We didn’t think this was possible”  
 – Sony-Ericsson engineer  
 Joakim Eriksson, Ph.D  
 Unprecedented capability  
 Data acquisition 30x faster



*“X-parameters provide a nonlinear electronic interactive datasheet based on data”*

# Load-dependence of another GSM commercial Amp from X-parameters measured at only 50 ohms

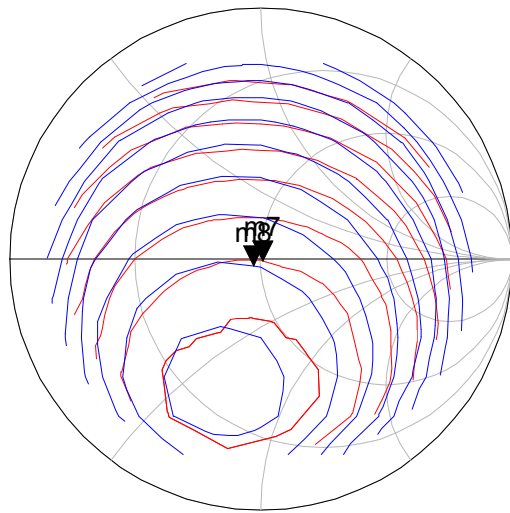
900 MHz  $V_{batt}=3.7$ ,  $V_{apc} = 1.4$

System Integrator wants to use X-parameters to compare performance among vendor parts within their system

Pout, 1dBm contour spacing

|  |  |
|--|--|
| m7<br>IndexPout2= 28.000<br>\$LPData.ZPout2=0.010 / -40.002<br>Pout2=34.364350<br>impedance = $Z_0 * (1.015 - j0.012)$ | m8<br>indep(m8)= 12<br>Pdel_contours_p=0.040 / -137.001<br>level=34.364350, number=1<br>impedance = $Z_0 * (0.942 - j0.051)$ |
|--|--|

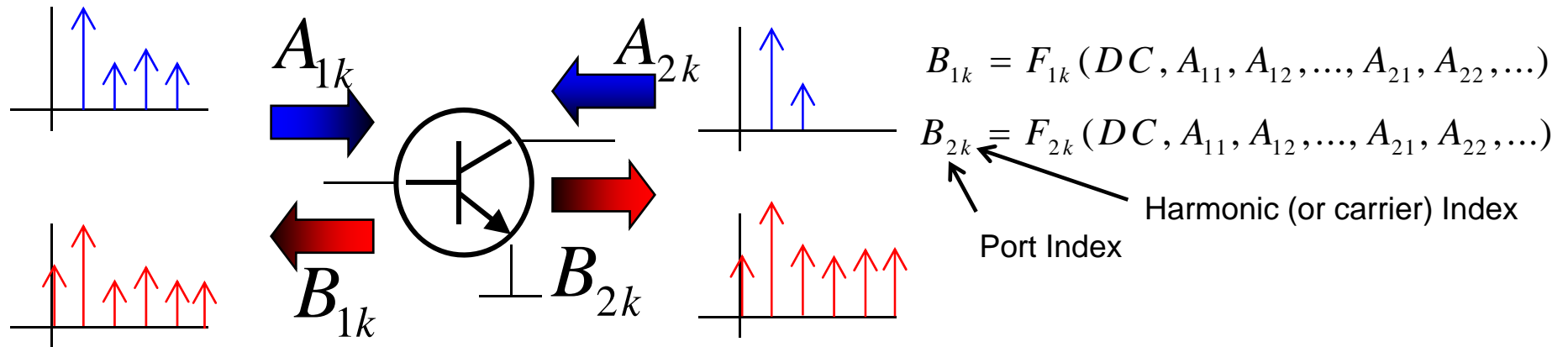
**Red:** LoadPull measurements  
**Blue:** Simulations using X-parameters *extracted in 50 ohms*



50 ohm X-parameters, predict performance well over a wide range of impedance

But what if we want even more accuracy?

# X-parameters with load-dependence



X-parameters allow us to **simplify** the general B(A) relations:  
 Trade efficiency, practicality, for generality & accuracy  
**Powerful, correct, and practical**

$$B_{e,f} = X_{ef}^{(F)}(DC, |A_{11}|)P^f + \sum_{g,h} X_{ef,gh}^{(S)}(DC, |A_{11}|)P^{f-h} \cdot A_{gh} + \sum_{g,h} X_{ef,gh}^{(T)}(DC, |A_{11}|)P^{f+h} \cdot A_{gh}^*$$

$$B_{e,f} = X_{ef}^{(F)}(DC, |A_{11}|, |A_{21}|, \theta)P^f + \sum_{g,h} X_{ef,gh}^{(S)}(DC, |A_{11}|, |A_{21}|, \theta)P^{f-h} \cdot A_{gh} + \sum_{g,h} X_{ef,gh}^{(T)}(DC, |A_{11}|, |A_{21}|, \theta)P^{f+h} \cdot A_{gh}^*$$

$$B_{e,f} = X_{ef}^{(F)}(DC, |A_{11}|, \Gamma_2)P^f + \sum_{g,h} X_{ef,gh}^{(S)}(DC, |A_{11}|, \Gamma_2)P^{f-h} \cdot A_{gh} + \sum_{g,h} X_{ef,gh}^{(T)}(DC, |A_{11}|, \Gamma_2)P^{f+h} \cdot A_{gh}^*$$

**“X-parameters unify S-parameters and Load-Pull”**

# NVNA+Load-Pull = Instant Large-Signal Model

- Drag and drop measured X-parameters for immediate ADS simulation “This is a breakthrough for the industry.”

– Gary Simpson Maury Microwave



NVNA +  
Load-Pull



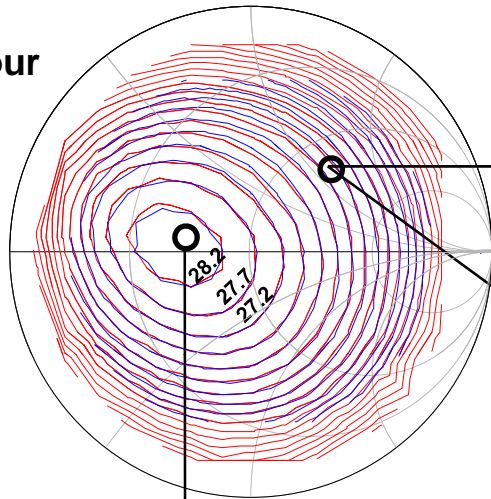
# Load-Dependent X-Parameters of a FET

G. Simpson et al *IEEE ARFTG Conference*, December, 2008

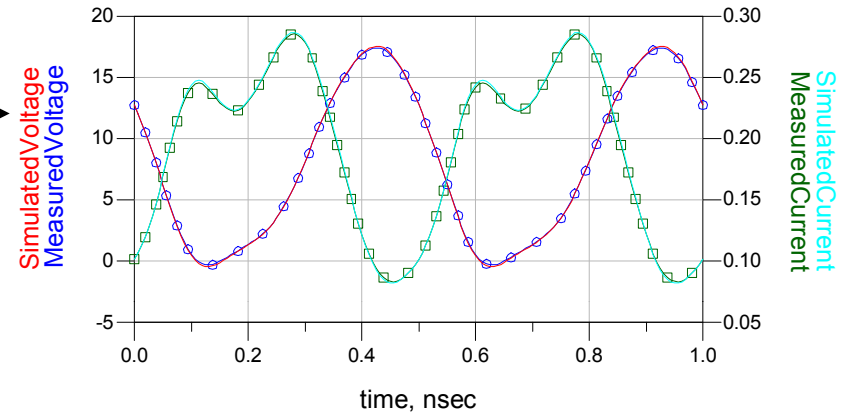
Measurements X-par Simulation

WJ FP2189 1W HFET

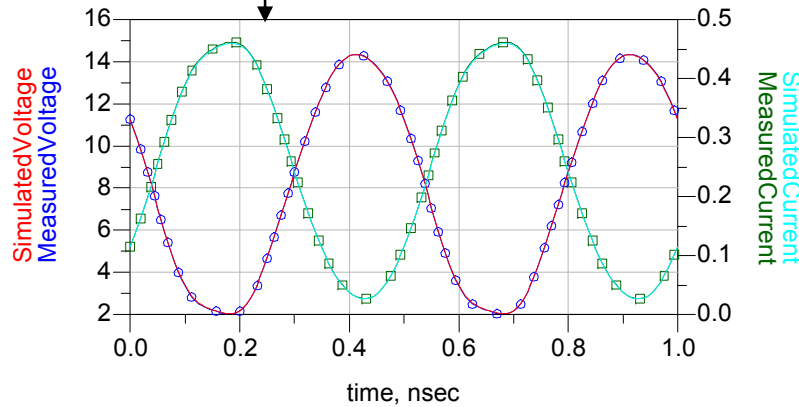
$P_{out}$  Contour (dBm)



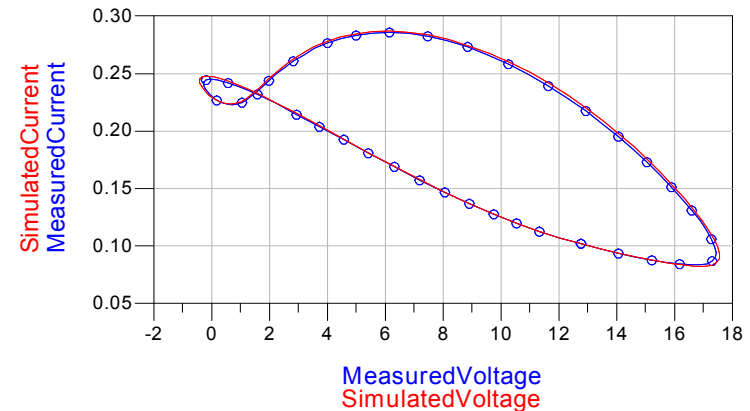
Measured and Simulated Voltage and Current Waveforms



Measured and Simulated Voltage and Current Waveforms



Measured and Simulated Dynamic Load Line



Experimental Harmonic Balance

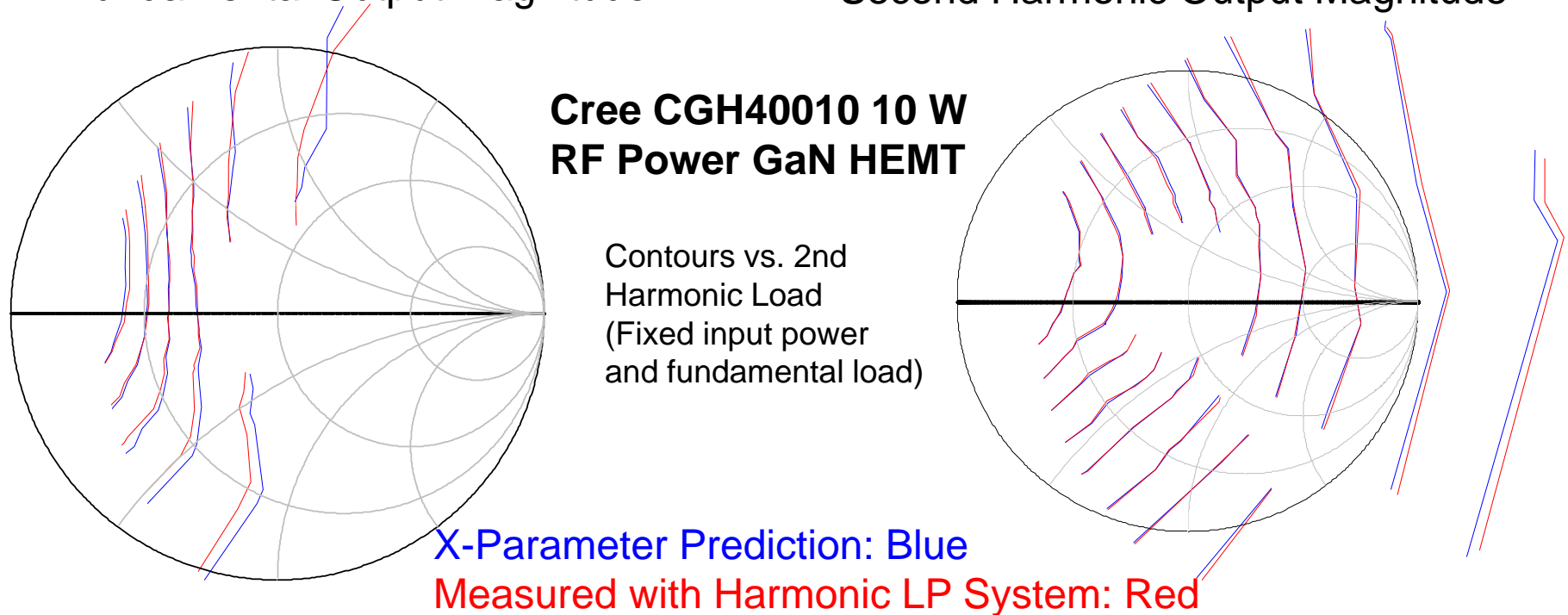
X-parameters unify S-parameters and load-pull

# Harmonic Load-Tuning Predictions from X-parameters

Horn et al, *IEEE Power Amplifier Symposium*, September, 2009

Fundamental Output Magnitude

Second Harmonic Output Magnitude



**Key Agilent IP** calibrates out uncontrolled harmonic impedances presented by tuner & re-grids impedance data for accuracy and interpolation in ADS

*Harmonic load-pull may be unnecessary! Simpler, cheaper, faster alternatives exist*



## Expand Your Agilent PNA-X Into A Nonlinear Load Pull Environment With Maury Automated Tuners

- Simple Setup
- Fast Power Measurements
- Time Domain Waveforms
- X-Parameters
  - Measure vs Impedance
  - Load Directly Into ADS
  - Acts Like A Model
  - Measurement Based Simulation And Design



Maury Microwave Corporation • 2900 Inland Empire Blvd., Ontario, California 91764 USA • Tel: 909-987-1715 • Fax: 909-987-1112  
 Email: maury@maurymw.com  
 Visit Us Online at MAURYMW.COM

Simple Setup  
 Fast, automated measurements  
 Time-domain waveforms

*Load-dependent X-parameters as a measurement-based device model*  
**“The data is the model”**

Useful for:

- High-power device characterization
- X-parameter transistor models
- multi-stage amps w. large mismatch

Control power, frequency, bias and load at fundamental frequency: faster, fewer data, simpler setup than harmonic L-P

- *Get sensitivity to harmonic loads at output and input ports without having to control harmonic impedances*
- *Estimate the effects of source-pull on device performance in ADS without having to control source impedance*

# Load-dependent X-parameters versus harmonic load-pull

Root et al *INMMiC Conference*, April, 2010  
Horn et al *submitted to IEEE CSICS2010*

## Load-dependent X-pars

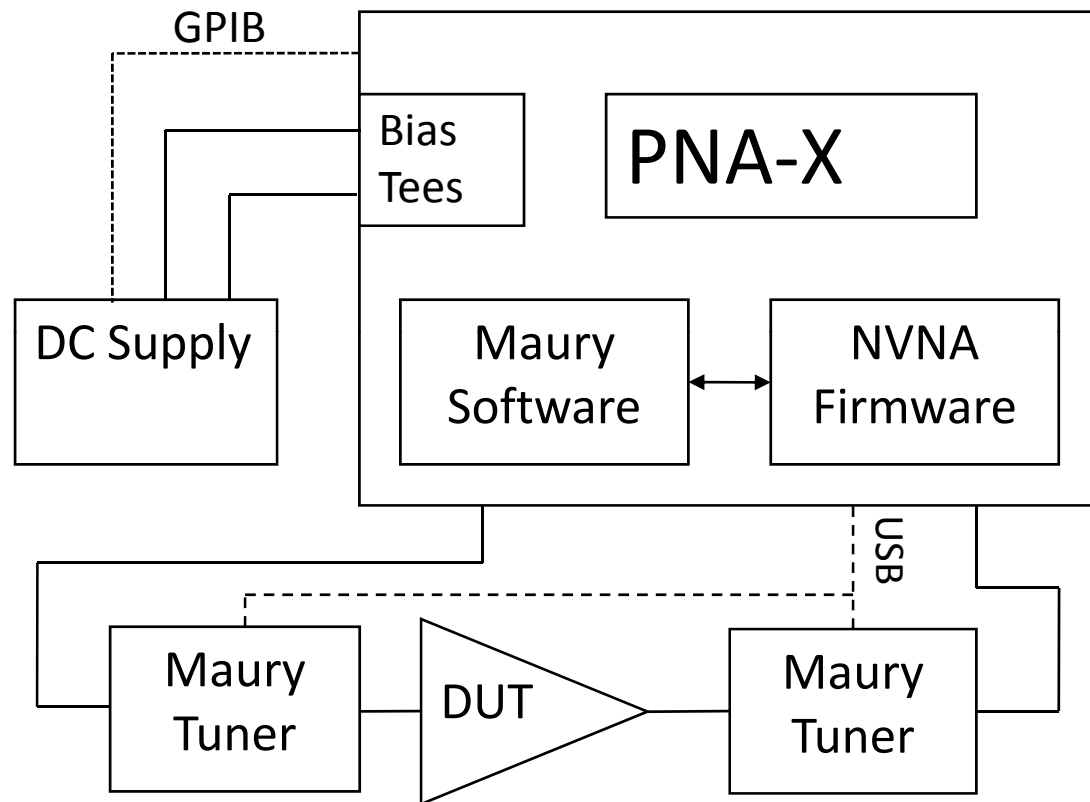
- *One output tuner* to vary load at fundamental frequency. At each load inject small tones at 2<sup>nd</sup> and 3<sup>rd</sup> harmonic freqs  
( $9 \times (1 + 2 \times 2) = 45$  measurements, actually ~99 measurements)
- Measured DC – 4<sup>th</sup> harmonic
- Take into ADS. Present 729 independent loads to model

## Harmonic load-pull validation

- *Three output tuners* to vary loads at fundamental, second, and third harmonics independently  
( $9 \times 9 \times 9 = 729$  measurements)
- Measured DC - 4<sup>th</sup> harmonic

Compare waveforms, PAE, dynamic load-lines, etc.

# Load-dependent X-parameter model for GaN HEMT:



9 load states x 3 x 2

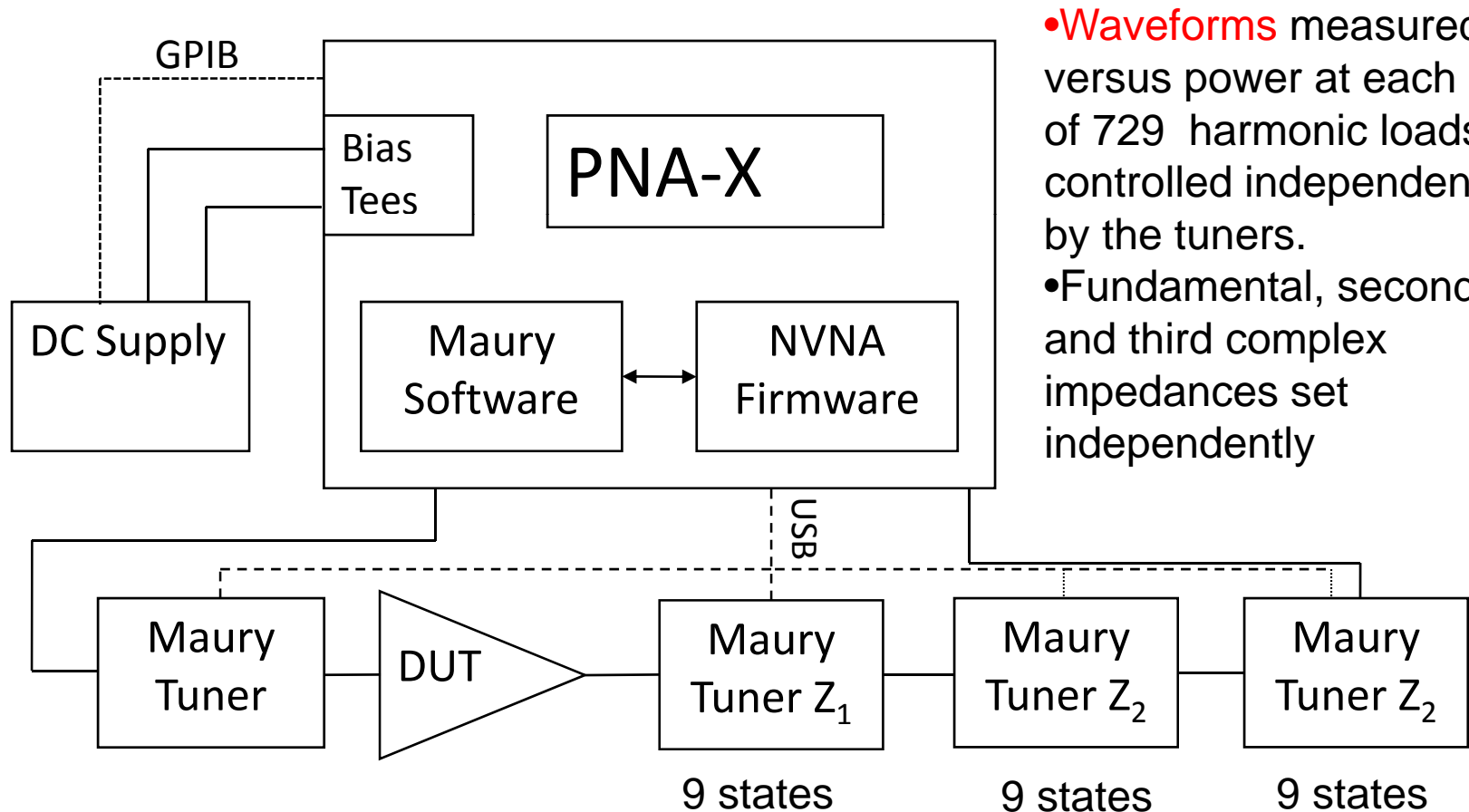
X-parameter file taken into ADS  
for independent validation

Cree  
CGH40010  
**GaN HEMT**  
10 W packaged  
transistor

- 900 MHz
- Measure Load-dependent **X-parameters** vs power at 9 impedances
- 4 harmonics measured
- probe tones at 2<sup>nd</sup> and 3<sup>rd</sup> harmonics
- harmonic impedances uncontrolled

# Harmonic Load-pull Setup: For Validation Only

J. Horn et al *Submitted to CSICS2010*



# Load-dependent X-parameters versus harmonic load-pull

## Load-dependent X-pars

- *One output tuner* to vary load at fundamental frequency. At each load inject small tones at 2<sup>nd</sup> and 3<sup>rd</sup> harmonic freqs (9x(1+2x2) = 45 measurements, actually ~125 measurements)
- Measured DC – 4<sup>th</sup> harmonic
- Take into ADS. Present 729 independent loads to model

## Harmonic load-pull validation

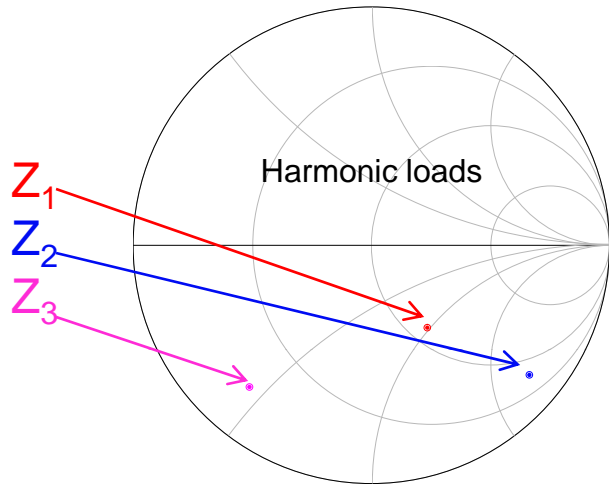
- *Three output tuners* to vary loads at fundamental, second, and third harmonics independently (9x9x9 = 729 measurements)
- Measured DC - 4<sup>th</sup> harmonic

Compare waveforms, PAE, dynamic load-lines, etc.

# Prediction of GaN HEMT *harmonic-load dependence* from fundamental-only load-dependent X-pars

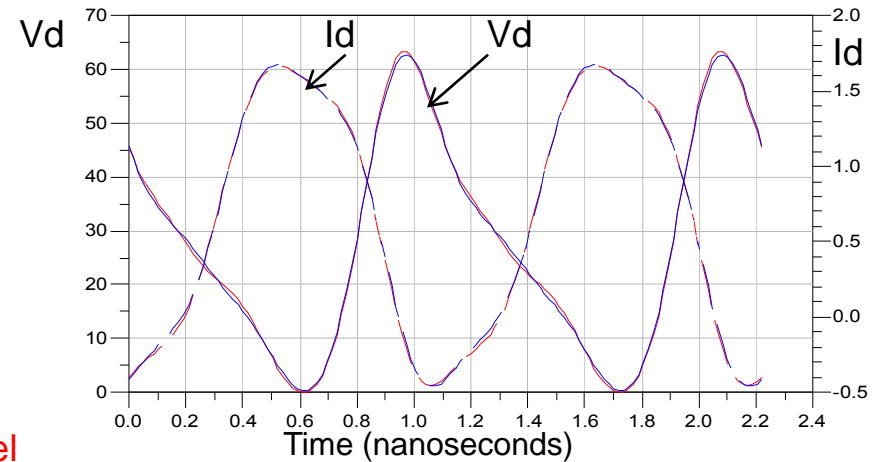
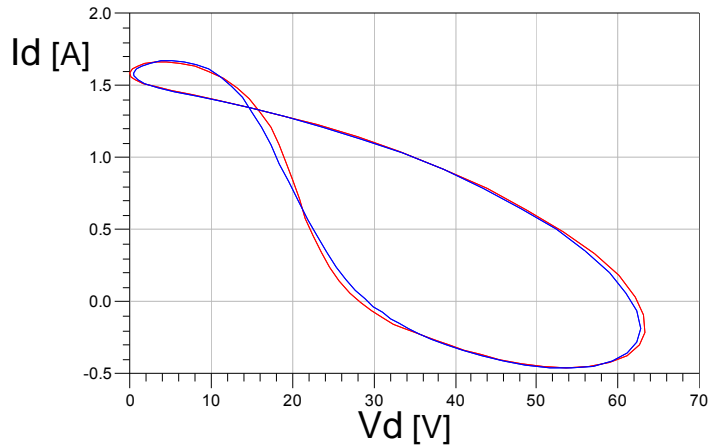
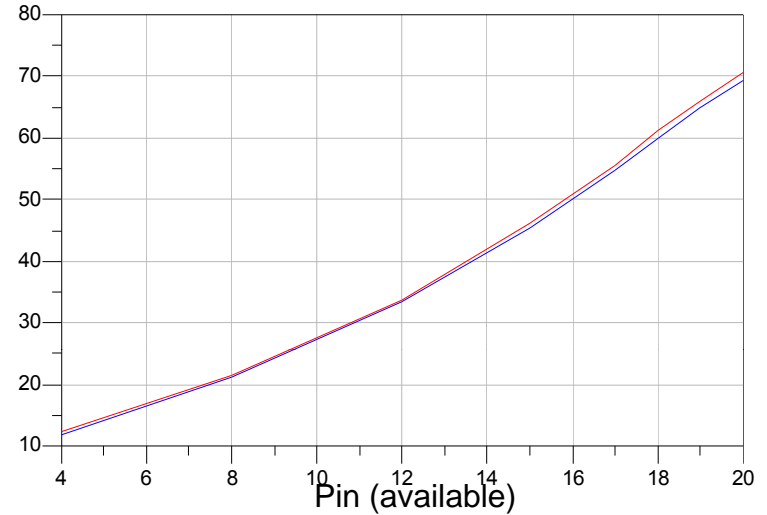
Courtesy of J. Horn

J. Horn et al, *submitted to CSICS2010*



Cree  
CGH40010  
GaN HEMT

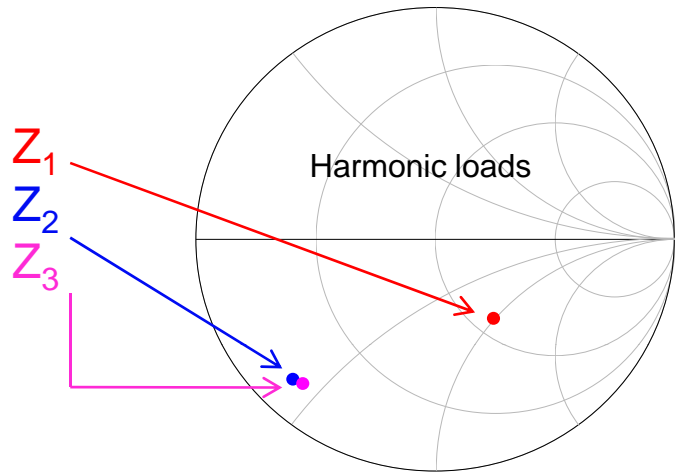
PAE



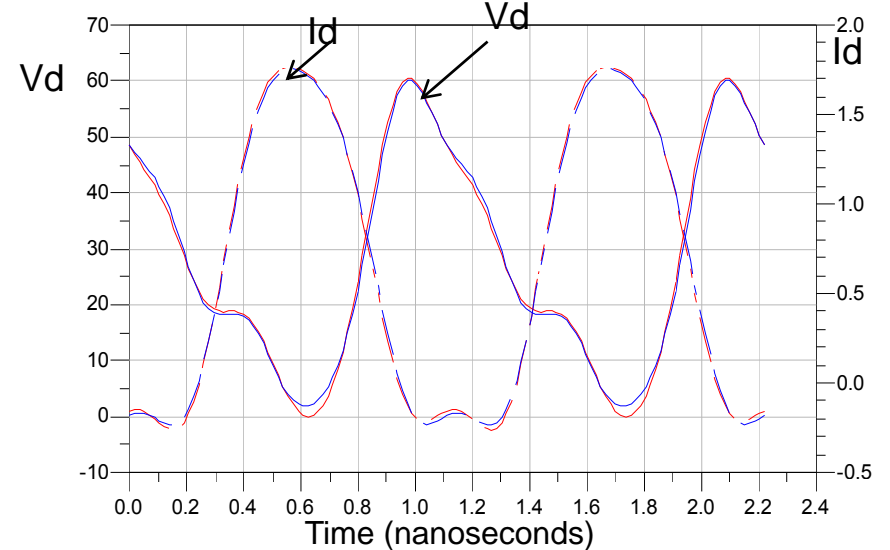
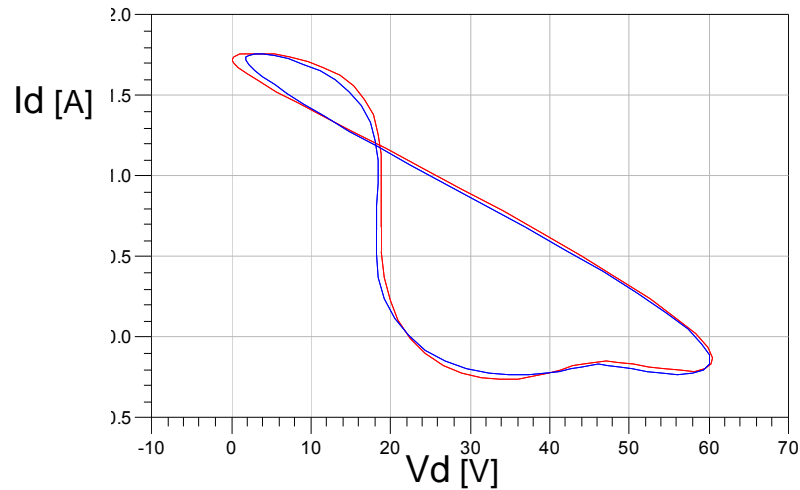
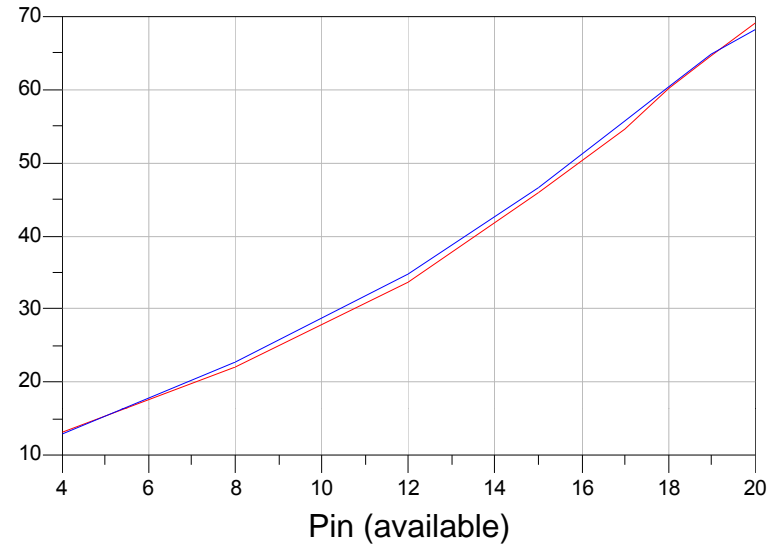
X-parameter model  
Harmonic time-domain load-pull measurements



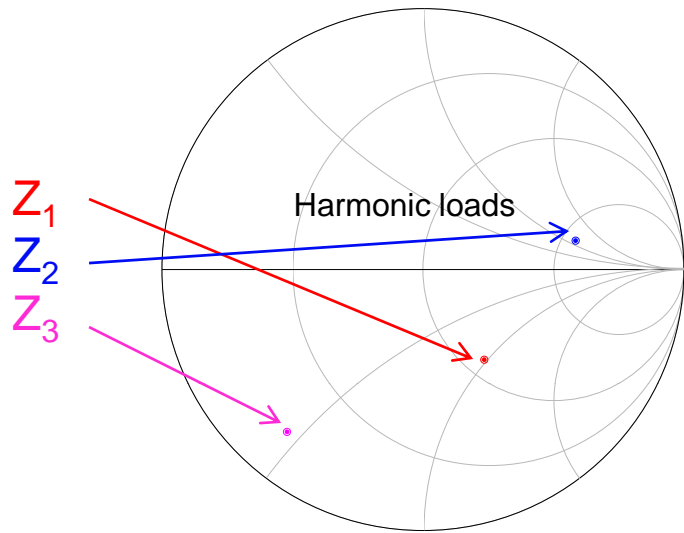
# Prediction of GaN HEMT *harmonic-load dependence* from fundamental-only load-dependent X-pars



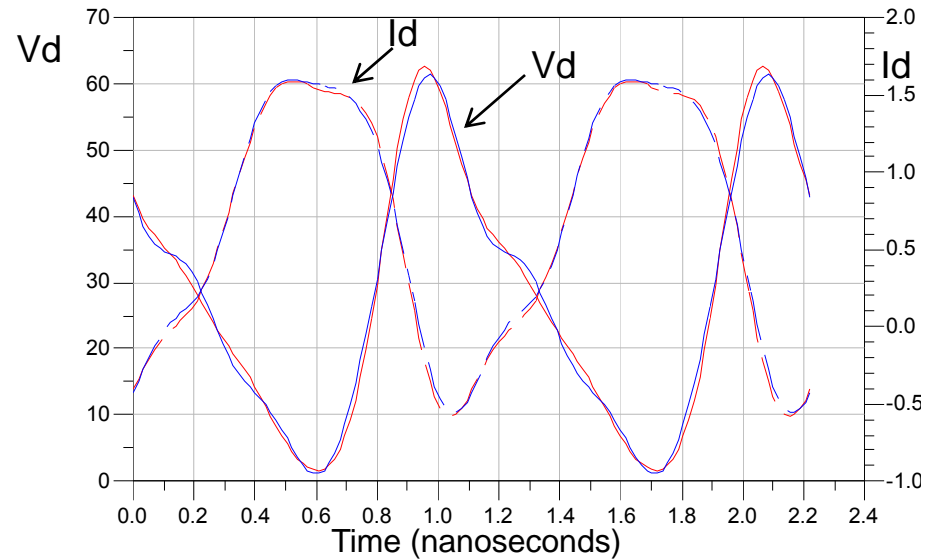
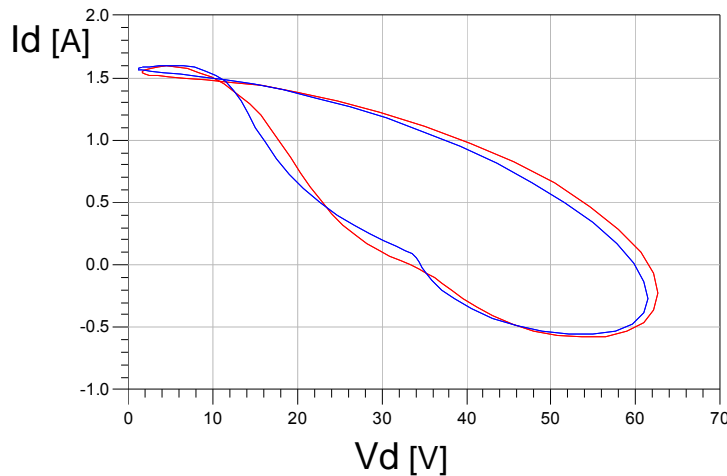
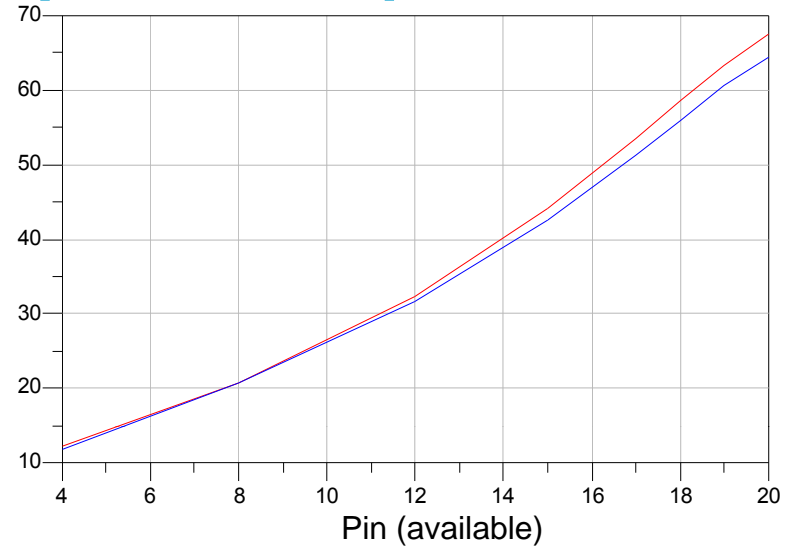
PAE  
Cree  
CGH40010  
GaN HEMT



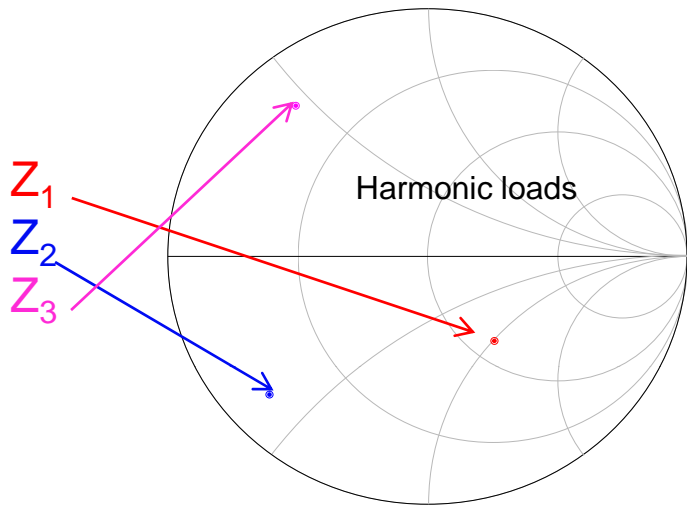
# Prediction of GaN HEMT *harmonic-load dependence* from fundamental-only load-dependent X-pars



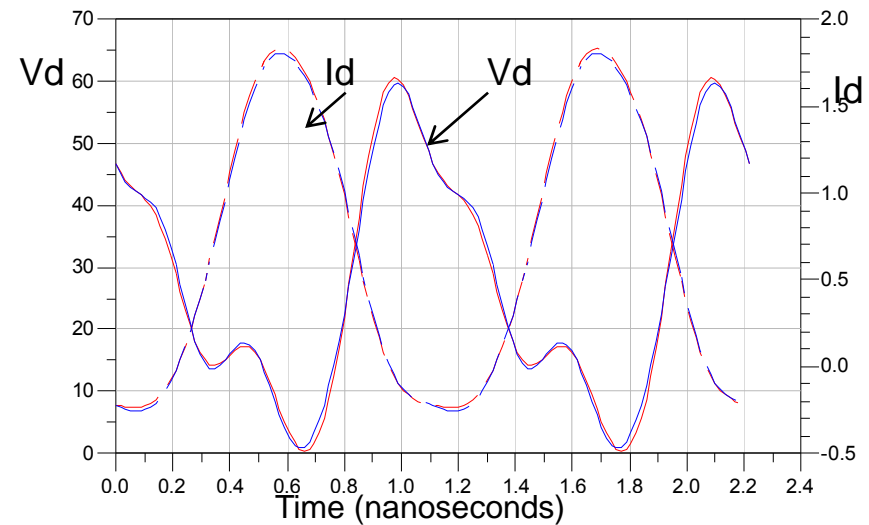
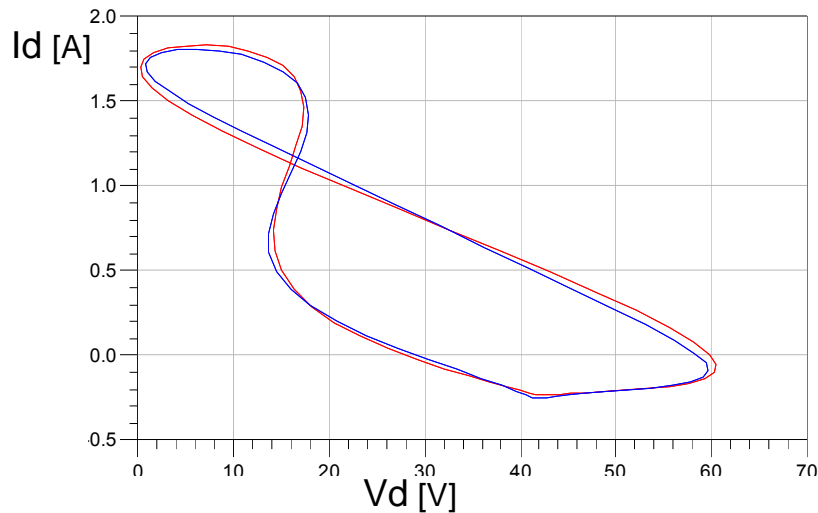
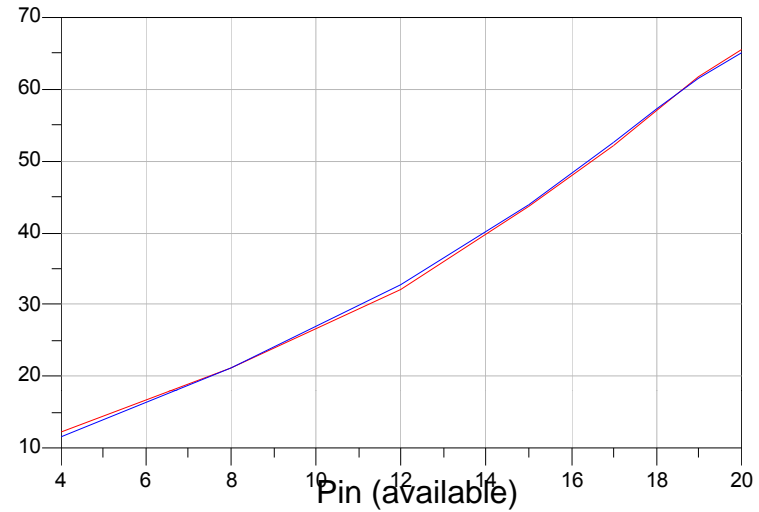
Cree  
CGH40010  
GaN HEMT



# Prediction of GaN HEMT *harmonic-load dependence* from fundamental-only load-dependent X-pars



PAE  
Cree  
CGH40010  
GaN HEMT



## Summary:

# Fundamental-only load-dependent X-parameters

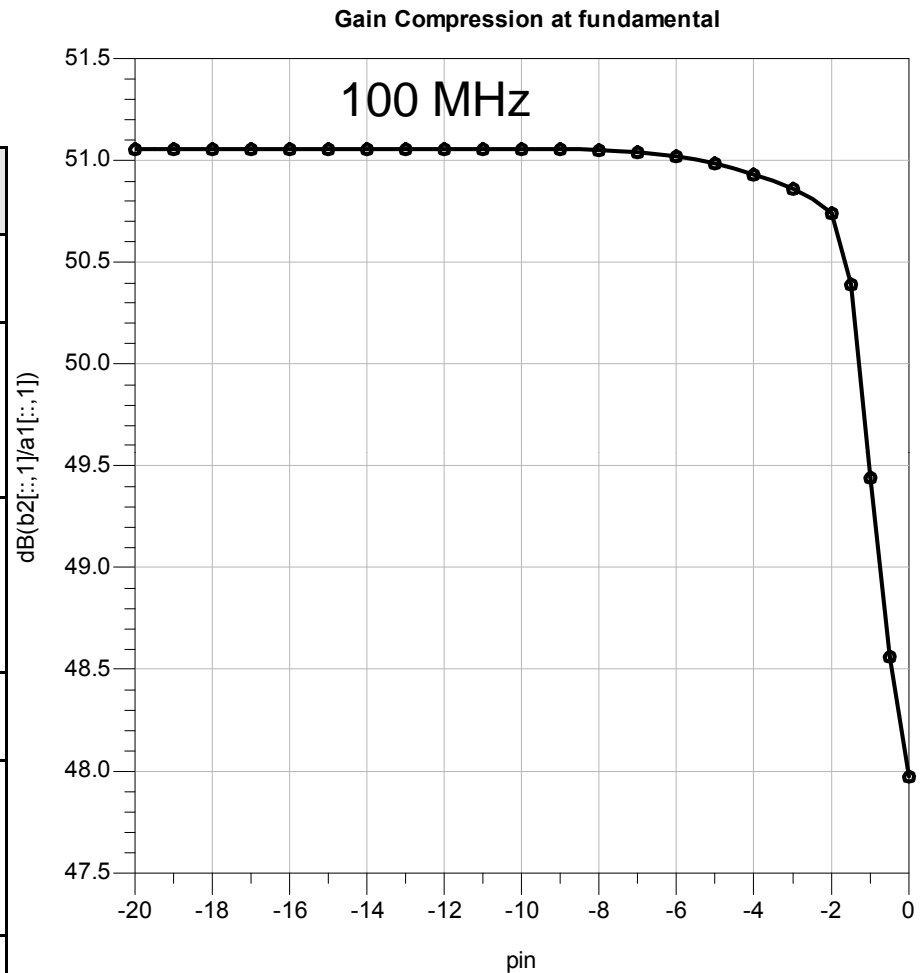
- Full two-port nonlinear functional block model for simulation
  - **Accounts for load-tuning dependence of device performance** without the requirement of independently controlling harmonic loads
  - Use to design matching networks, multi-stage amps, Doherty amps., ...
- Large data / time reduction compared to harmonic load-pull
  - X-parameter model scales linearly in number of loads  $N$
  - Harmonic L-P scales as  $N^H$   $H =$  no. of controlled harmonic loads
- Harmonic load-pull may be unnecessary
  - Validates “principle of harmonic superposition” (Verspecht et al 1997)
  - Source-pull unnecessary (Horn et al *submitted to CSISC 2010*)  
except for power transfer

# X-parameters at 100W

(courtesy K. Anderson)

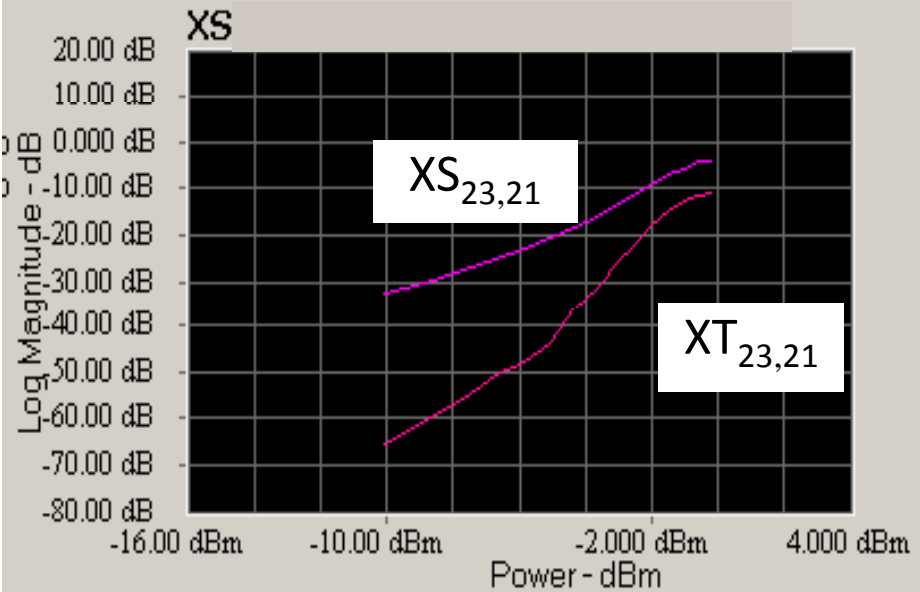
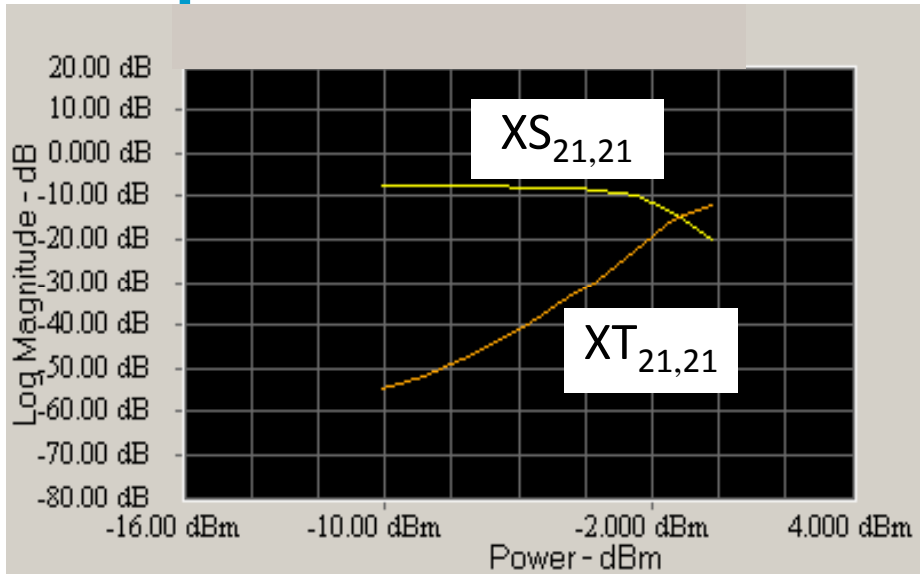
| Parameter                    | Description  |
|------------------------------|--|
| Part Number                  | ZHL-100W-52  |
| Pout max (@ 1dB compression) | 45dBm (min, 50M-500MHz)<br>47dBm (typ, 50M-500MHz)     |
| Pout max (@ 3dB compression) | 46.5dBm (min, 50M-500MHz)<br>48.5dBm (typ, 50M-500MHz) |
| Pin max (no damage)          | +3dBm  |
| Gain                         | 48dB (min)<br>50dB (typ)                               |
| Input VSWR                   | 1.45:1 (typ)   |
| Output VSWR                  | 2.5:1 (typ)  |

## Mini-Circuits ZHL-100W-52

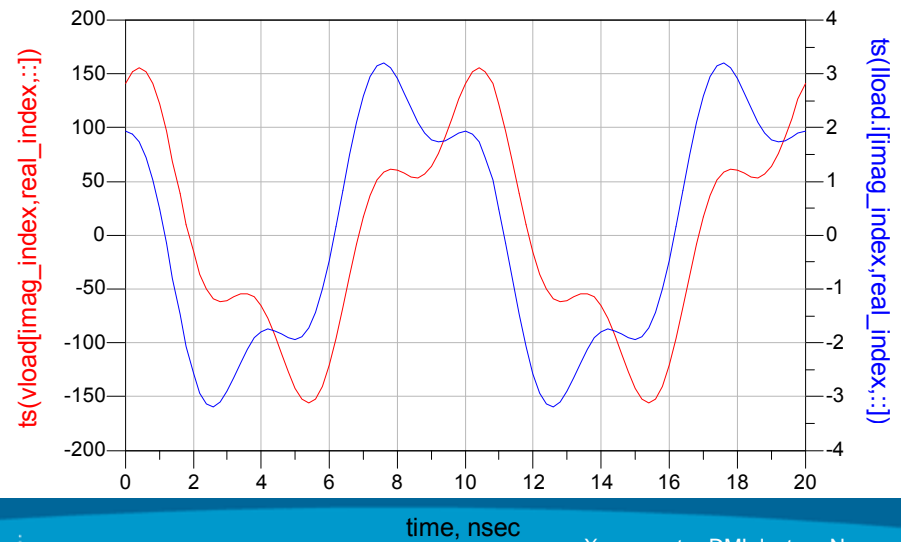


X-parameters have been measured at 250 W

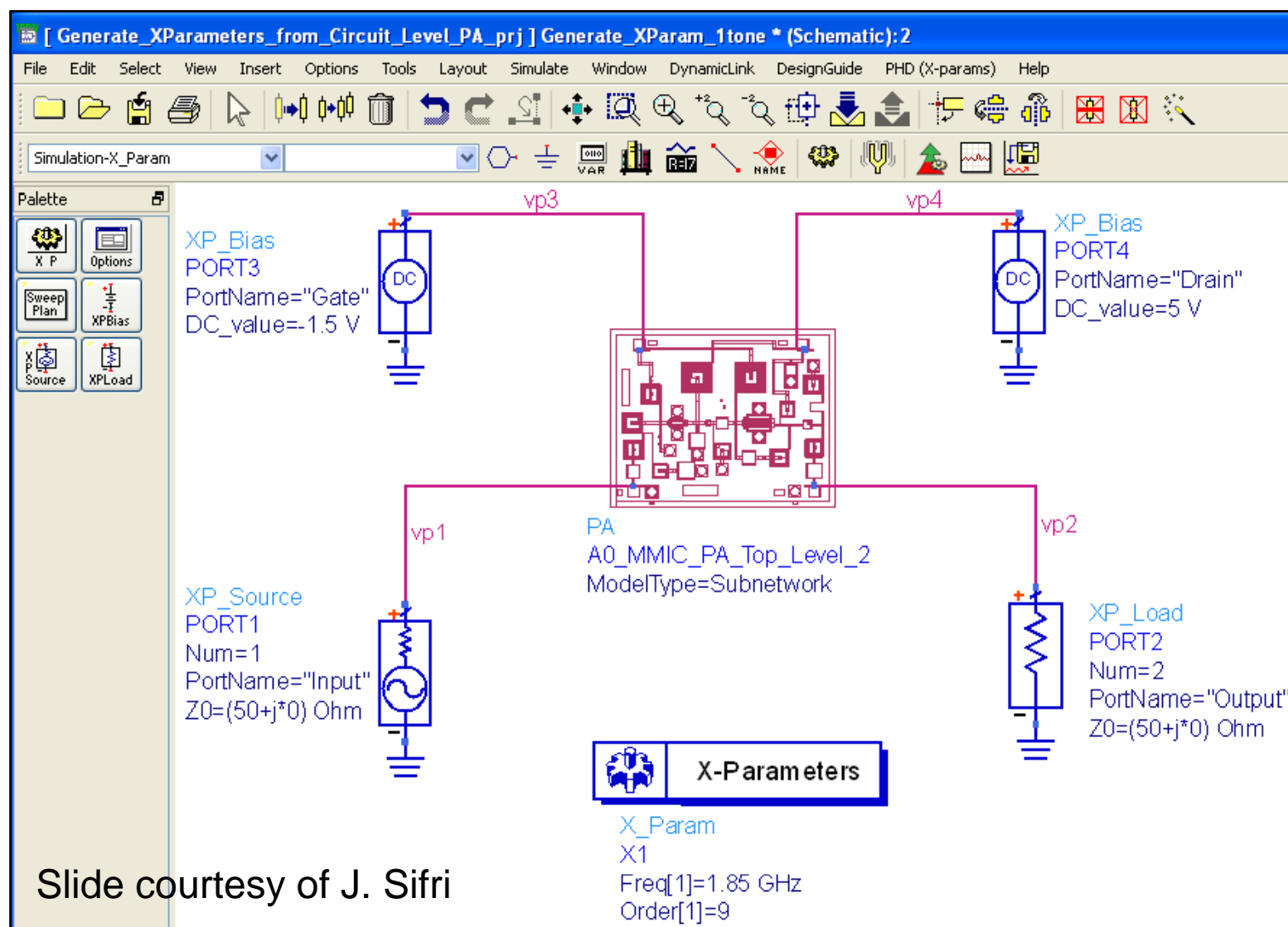
# X-parameters at 100W



5 harmonics, magnitude and phase:  
fund=150 MHz



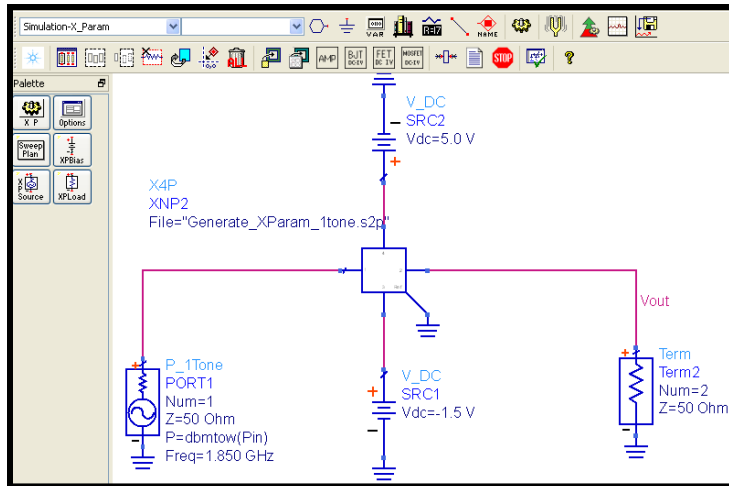
# Generate an IP-Protected X-parameter model



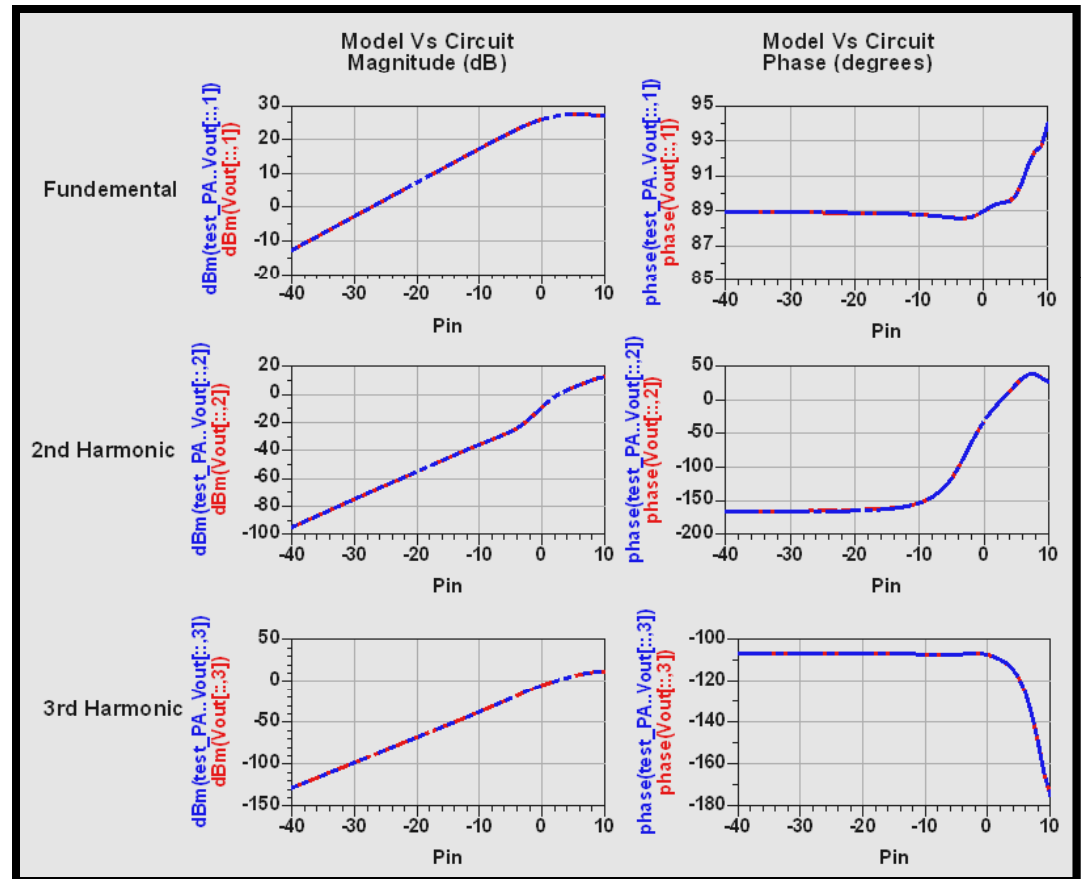
Slide courtesy of J. Sifri

# Single Tone Amp model with 50 ohm load

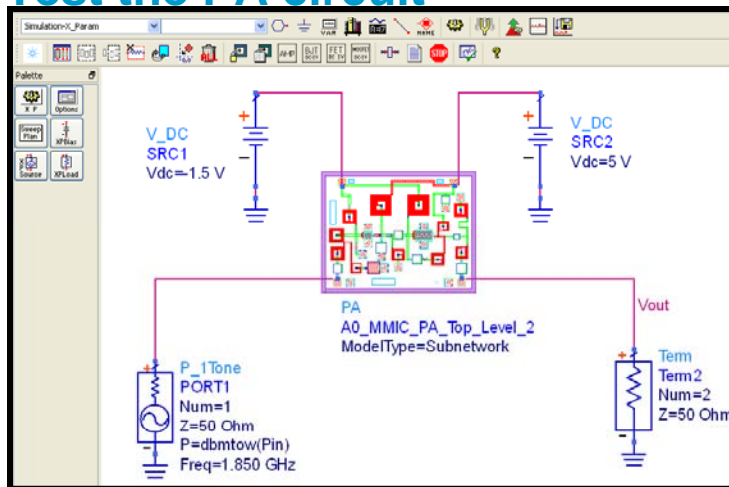
IP-protected model; Fast X-parameter simulation component (20x faster)



## X-pars Vs ckt-level PA Results



## Test the PA circuit





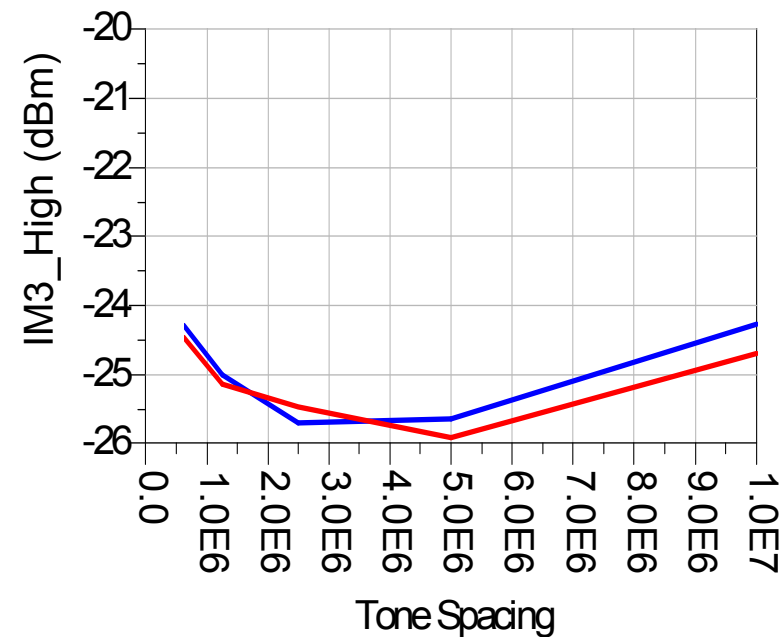
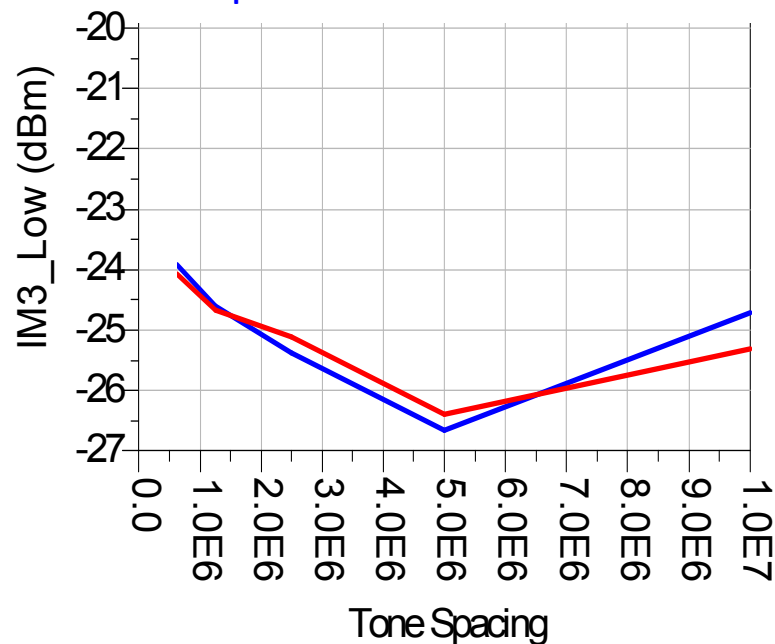
# Soon: Two-tone X-parameter NVNA measurements

- Magnitude *and Phase* of intermod products and sensitivity to mismatch
- Measure and simulate freq-dependence & asymmetry of complex intermods
- Design nonlinear circuits that cancel distortion
- ADS X-parameter generator and XnP component can do this already

Red = 2-Tone X-parameters prediction

Blue = Independent measured data

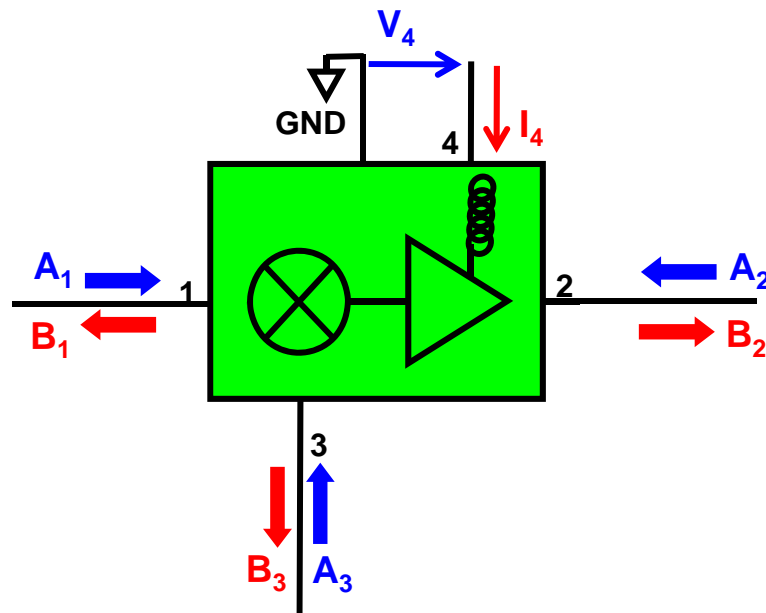
Courtesy J. Horn



# 3-Port X-parameter Measurements

For characterization and measurement-based simulation of three-port components (mixers, converters, switches)

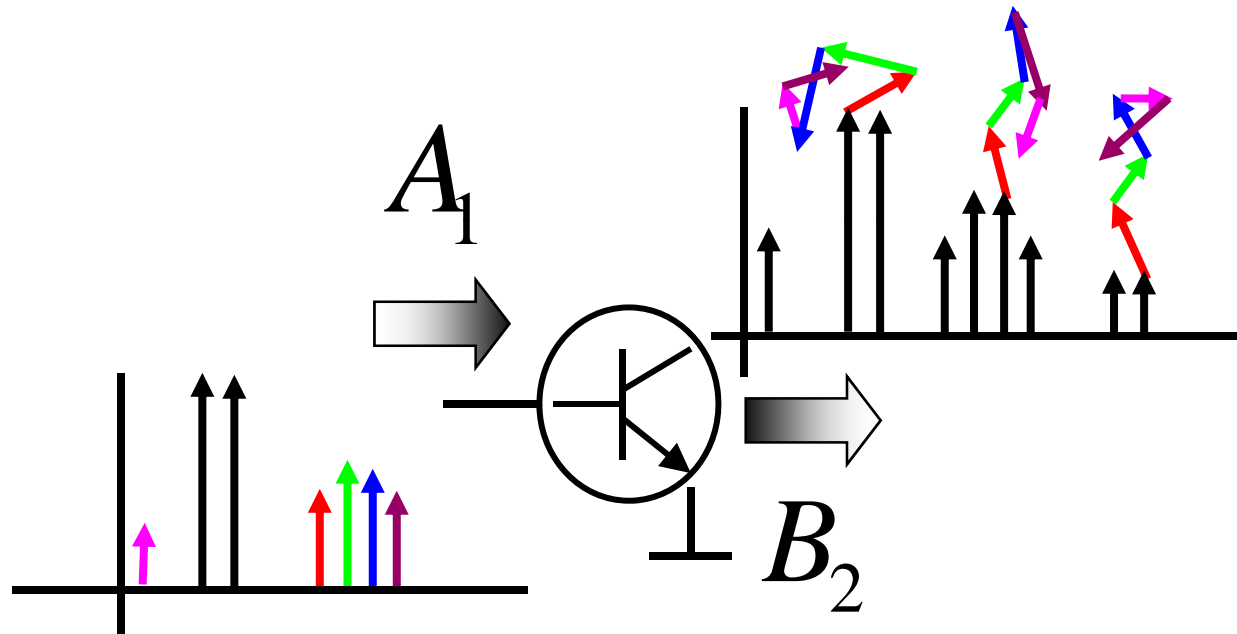
Note: ADS can already generate and simulate with multi-port, multi-tone X-parameters



Here A and B waves include *multiple spectral components*

# Multi-tone, Multi-port X-parameters: Two large signals at different frequencies at different ports

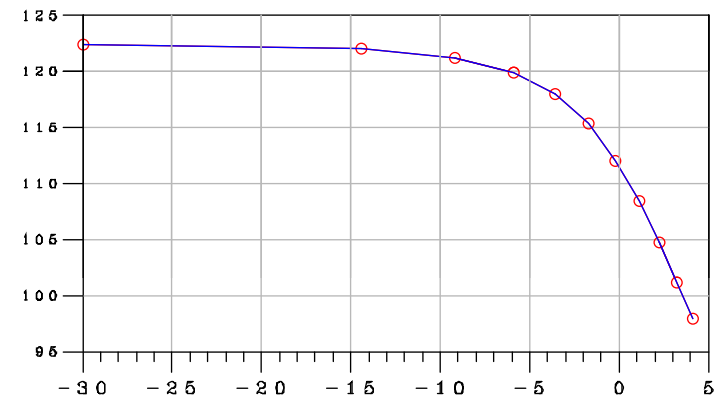
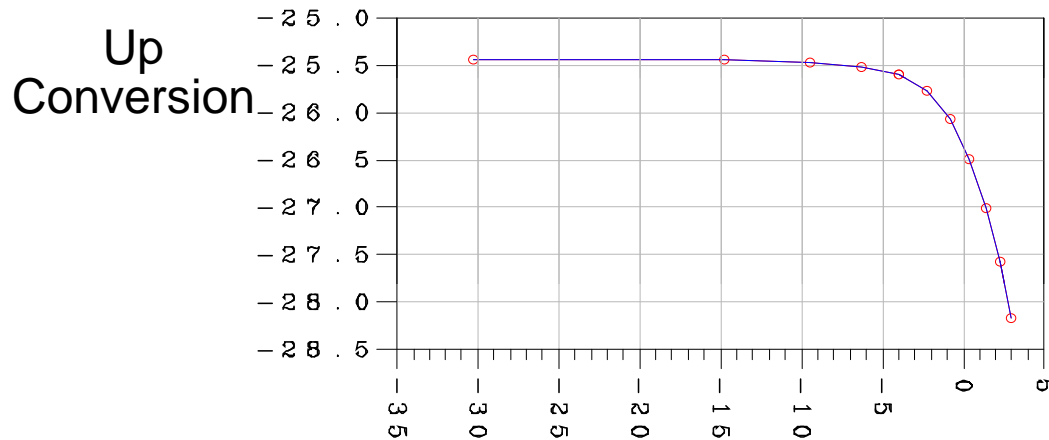
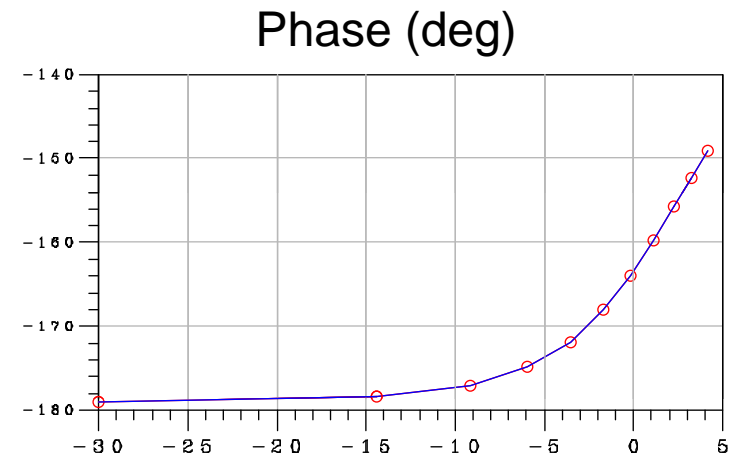
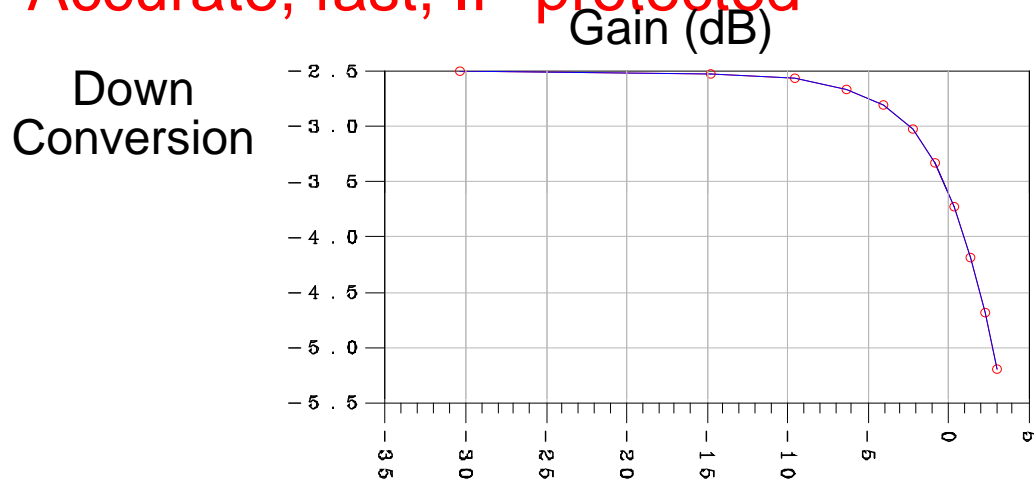
Less restrictive approximation to the general theory:  
 Linearization around the **multi-tone** nonlinear responses



$$B_{i,kl} = X_{i,kl}^{(F)} (A_{1,10}, A_{2,01}, 0, 0, \dots) + \text{Terms } \textit{linear} \text{ in the remaining components}$$

# Mixers: X-parameters extracted from an Agilent DC-50 GHz InP-based Mixer 1GC1-8068: Mismatched (10 Ohms) at IF

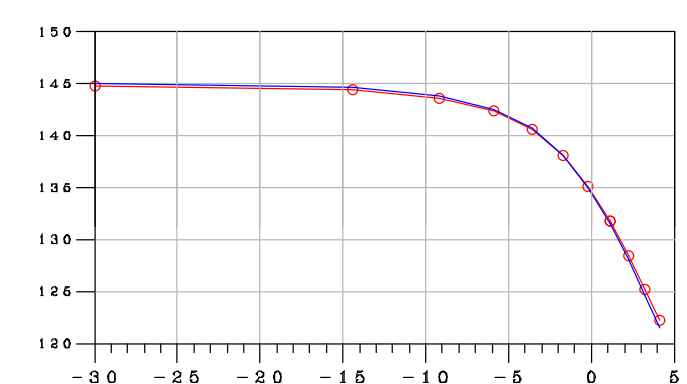
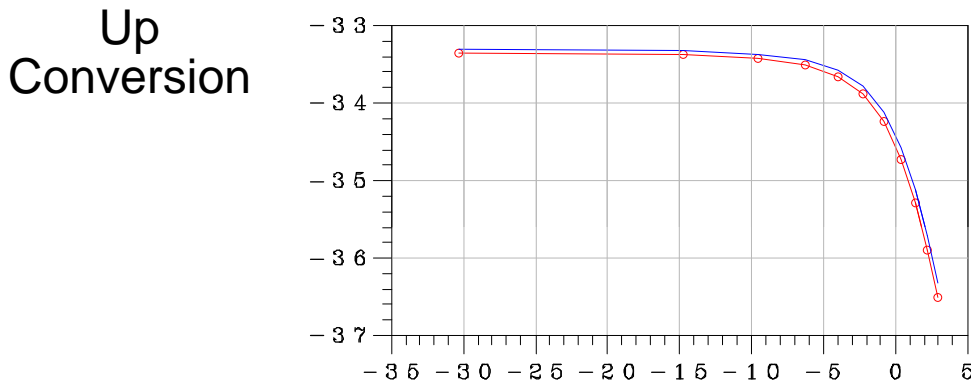
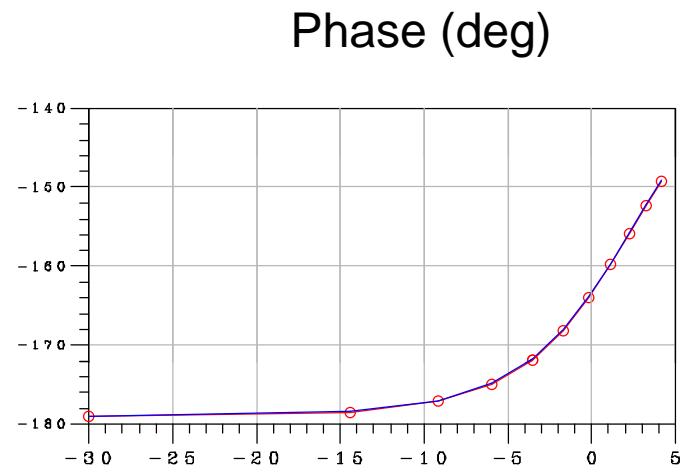
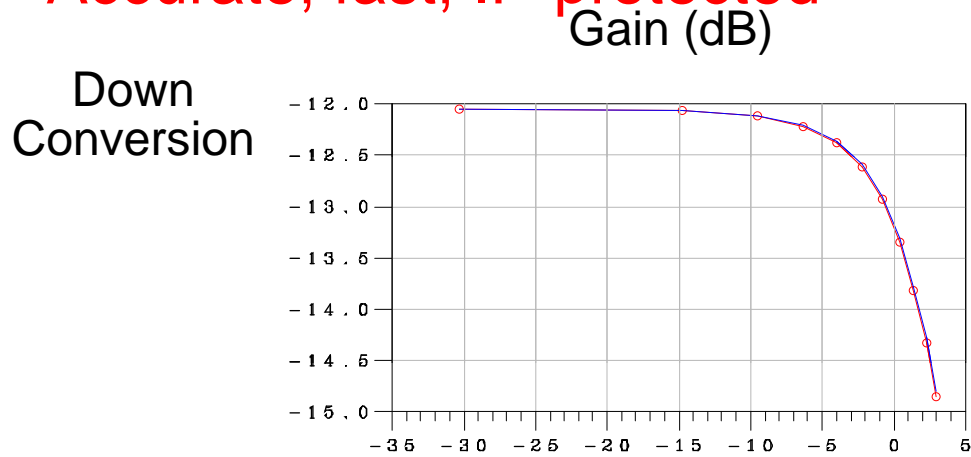
Accurate, fast, IP-protected



Simulation-based LO: 45 GHz RF: 45.1 GHz LO power = 3.5 dBm  
 Circuit Model (solid blue) X-parameter Model (red points)

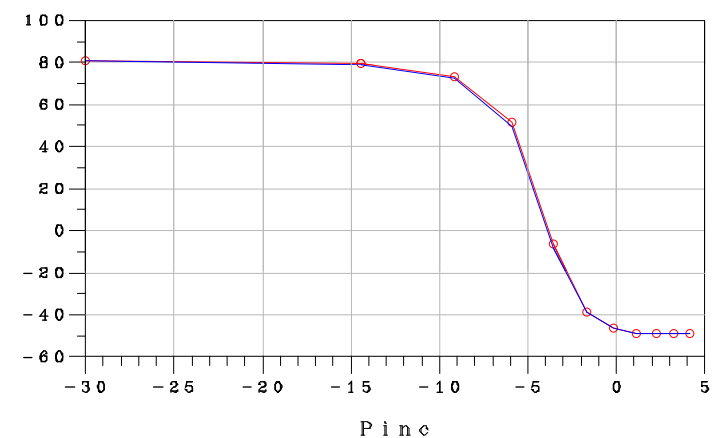
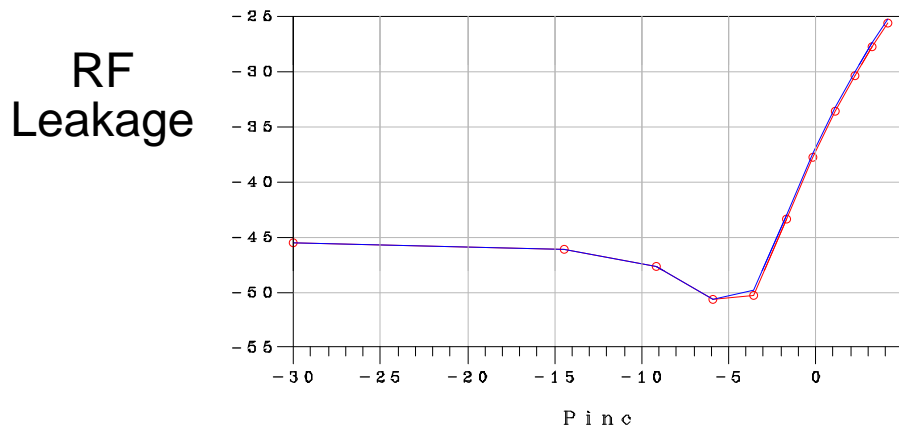
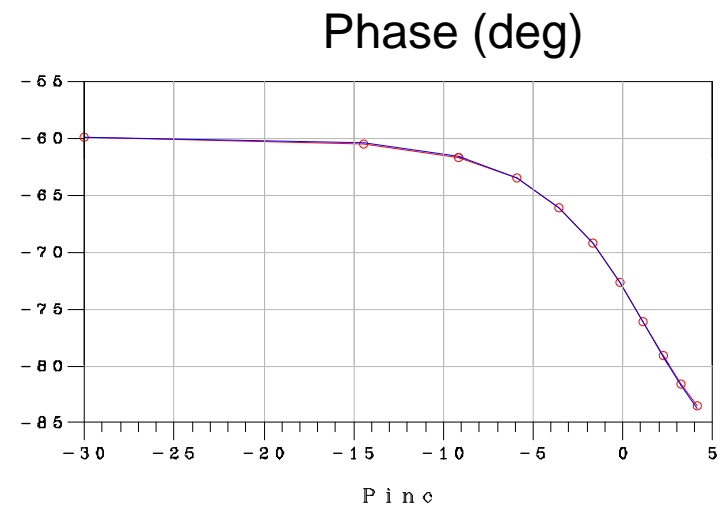
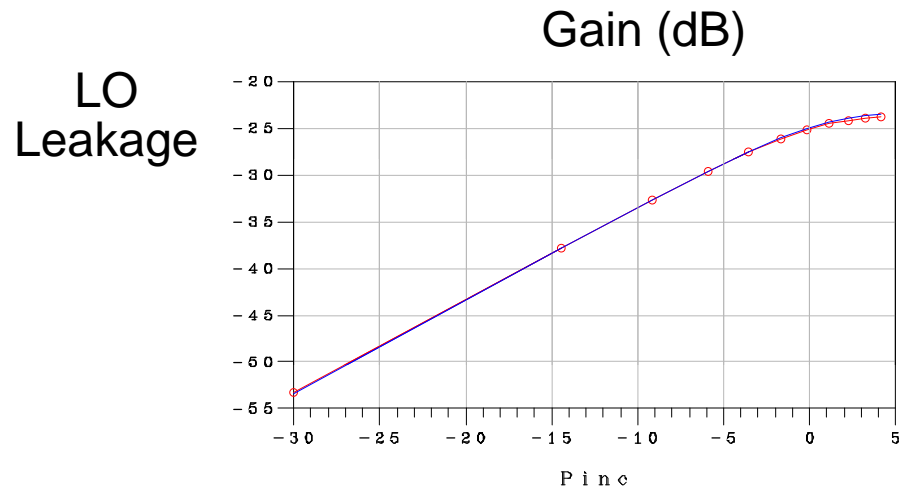
# Mixers: X-parameters extracted from an Agilent DC-50 GHz InP-based Mixer 1GC1-8068: Mismatched (10 Ohms) at IF

Accurate, fast, IP-protected



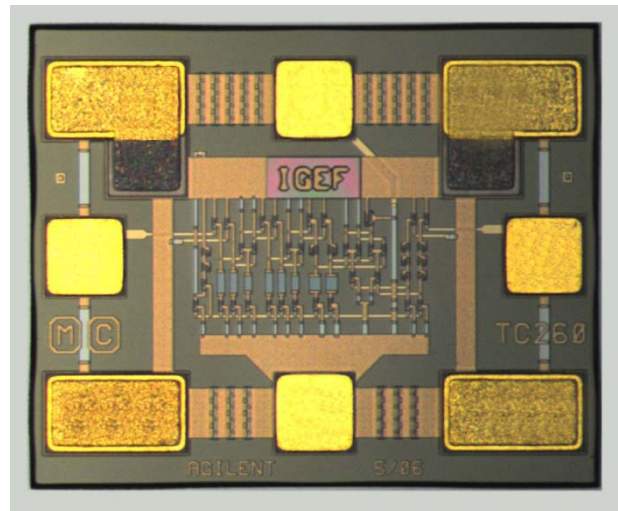
Simulation-based LO: 45 GHz RF: 45.1 GHz LO power = 3.5 dBm  
 Circuit Model (solid blue) X-parameters (red points)

# Two Fundamentals: 50 GHz Integrated Mixer Mismatched load (10 Ohms) at IF

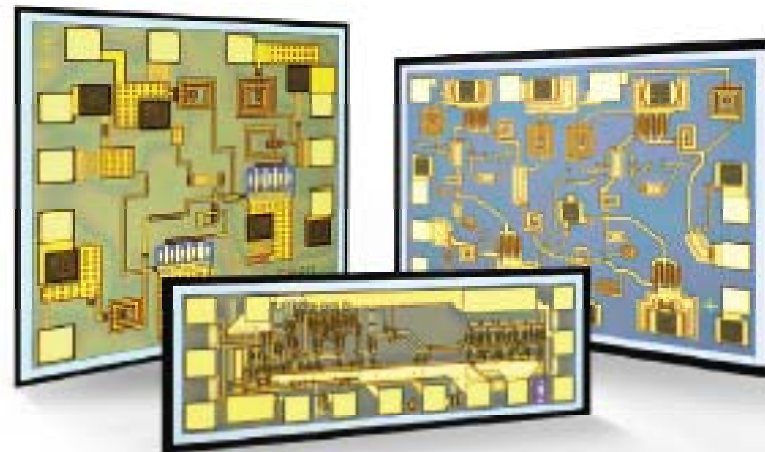


Simulation-based LO: 45 GHz RF: 45.1 GHz LO power = 3.5 dBm  
 Circuit Model (solid blue) X-parameter Model (red points)

# Agilent MMICs: Available for purchase



"I need robust MMICs for my most demanding applications."



**50 GHz InP-based Mixer**  
**Part number: 1GC1-8068**

See: <http://www.agilent.com/find/mmic>

X-parameters available

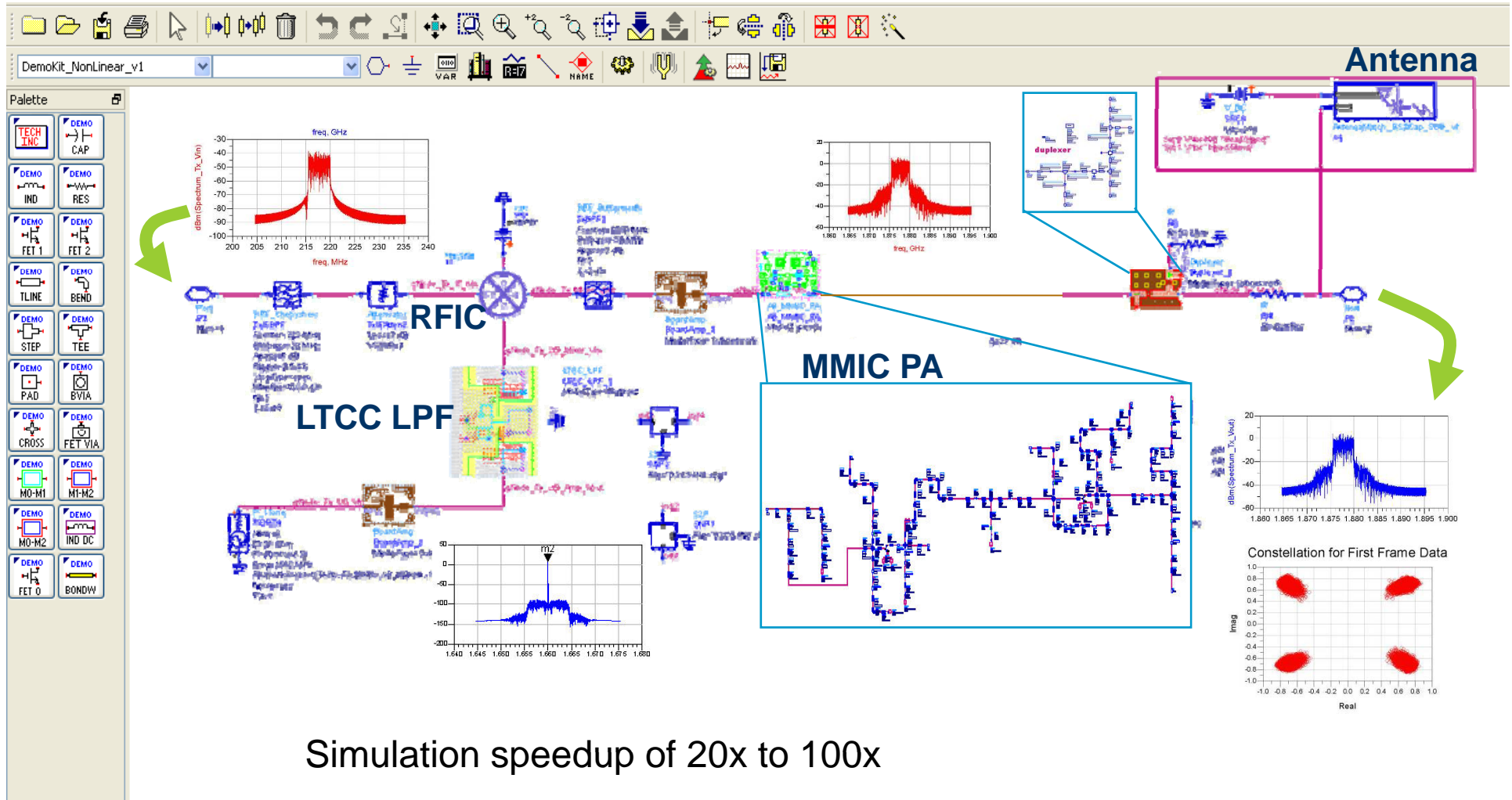
## So do we.

If you're an engineer working in a field requiring robust products that perform to spec in a wide range of real world conditions, we can relate. Agilent requires instrument-grade MMICs to design and build the world's finest measurement equipment. So we manufacture our own MMICs that offer exceptional performance over a broad spectrum of variables. And you can order them now. That's performance. That's Agilent.

|                                     |
|-------------------------------------|
| <b>Agilent MMICs</b>                |
| Highly linear mixers                |
| High power/high fidelity amplifiers |
| High TOI attenuators                |
| Microwave MEMS                      |
| <b>X-parameters available</b>       |

**Request a free catalog**  
[www.agilent.com/find/MMIC-INFO](http://www.agilent.com/find/MMIC-INFO)

# Design Nonlinear RF Systems



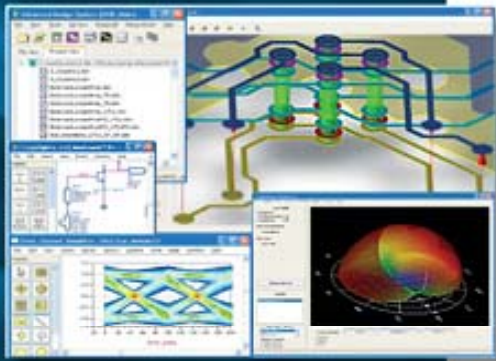
Simulation speedup of 20x to 100x



# X-Parameter technology available in commercial EDA SW

## Advanced Design System (ADS)

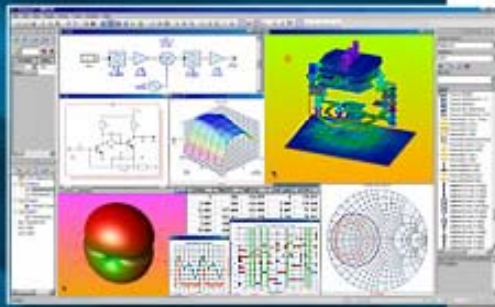
Premier RF & Microwave Design Platform



✓ Available Today

## Genesys

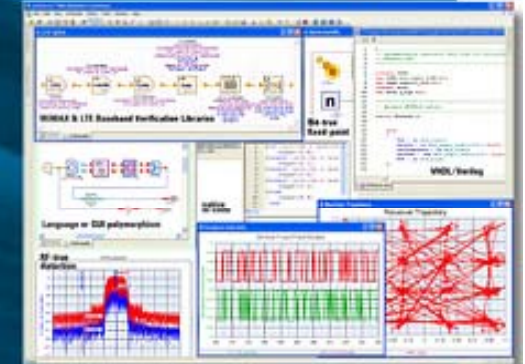
Affordable, High Performance RF/Microwave Board Design Software



✓ Available Soon

## SystemVue

Electronic System-Level Design (ESL) Software



✓ Available Soon

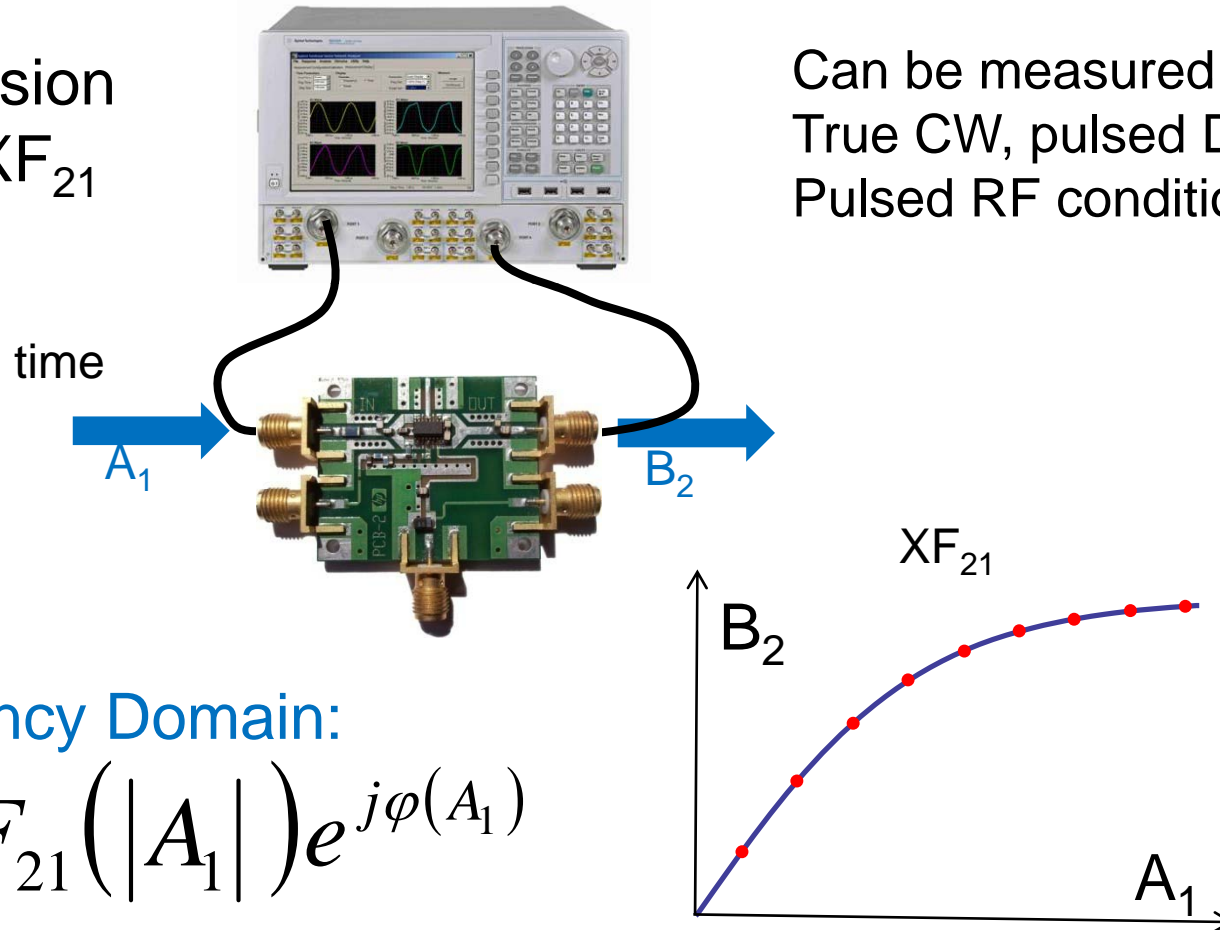
# Extending X-parameters to long-term memory

## Original X-parameters are Static Spectral Mappings

Slides courtesy J. Verspecht NVNA

Static transmission  
X-parameter:  $XF_{21}$

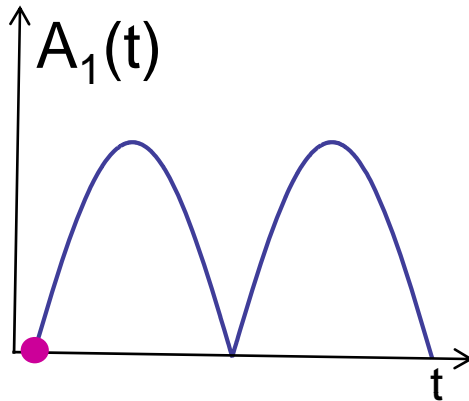
Can be measured under  
True CW, pulsed DC or  
Pulsed RF conditions



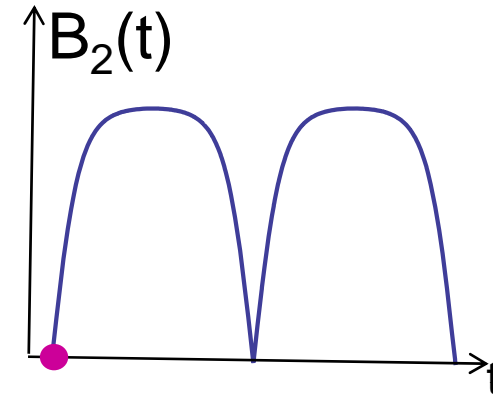
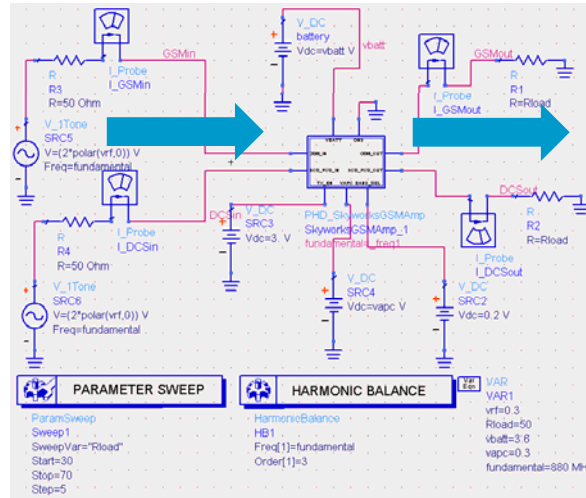
Frequency Domain:

$$B_2 = XF_{21} \left( |A_1| \right) e^{j\varphi(A_1)}$$

# Modulation Simulated in Envelope Domain:



ADS envelope simulator



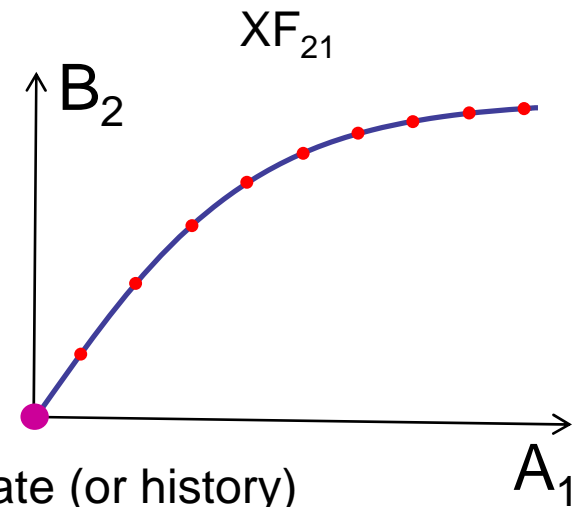
Envelope Domain:

$$B_2(t) = XF_{21}(|A_1(t)|)e^{j\phi(A_1(t))}$$

X-parameters determine Quasi-Static Response

No “BW” effects

Symmetric intermods independent of envelope rate (or history)



# Memory Effects: Beyond Static X-parameters

## Memory Effects:

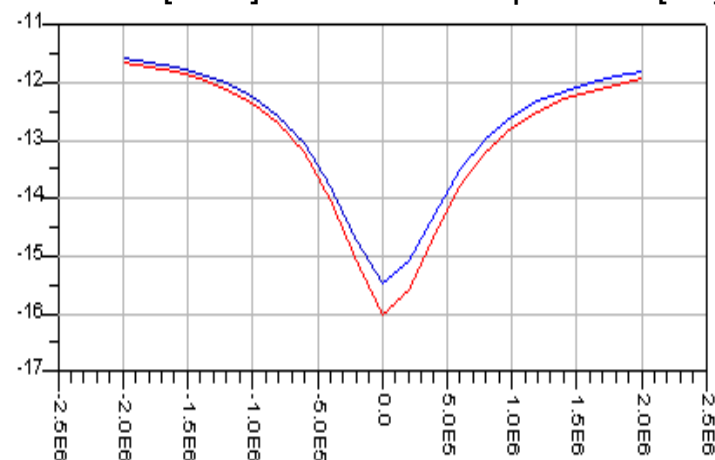
When output depends not only in instantaneous input but also on past input values

- Response to fast input envelope variations may violate quasi-static assumption for use in envelope domain for estimation of response to modulated signals
- Physical causes of memory: Dynamic self-heating, bias-line interaction, trapping effects caused by *additional dynamic variables* – multiple time-scale problem

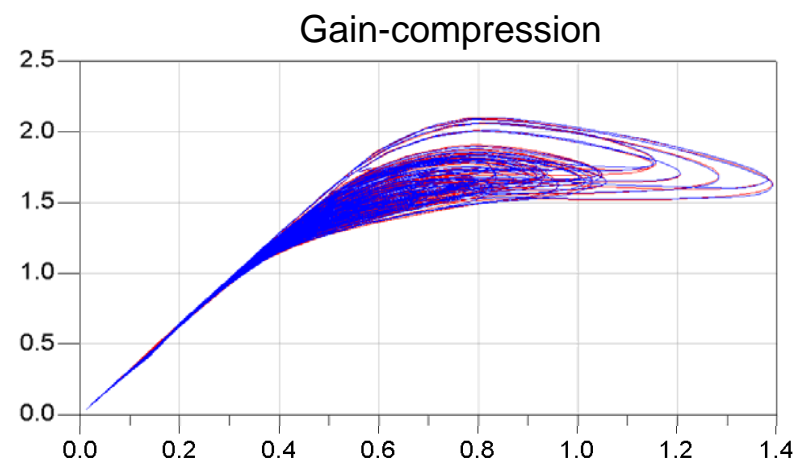
IM3 products asymmetric

Depend on tone spacing

HBT IM3 [dBm] versus tone separation [Hz]



Hysteresis in compression plot

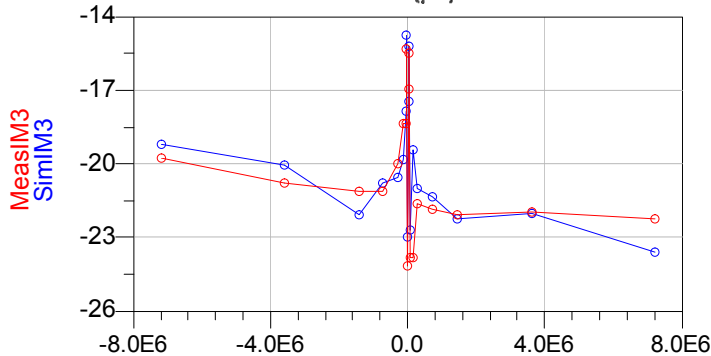
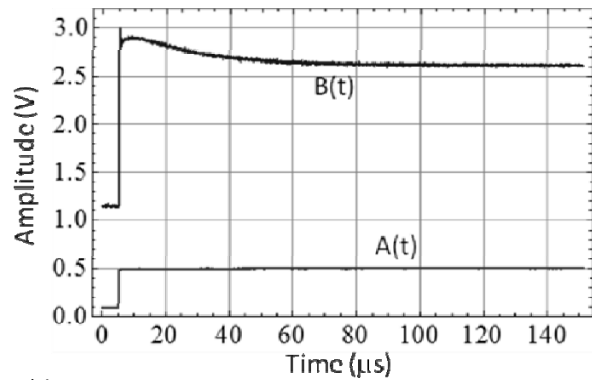


# Dynamic X-parameters: Long-Term Memory

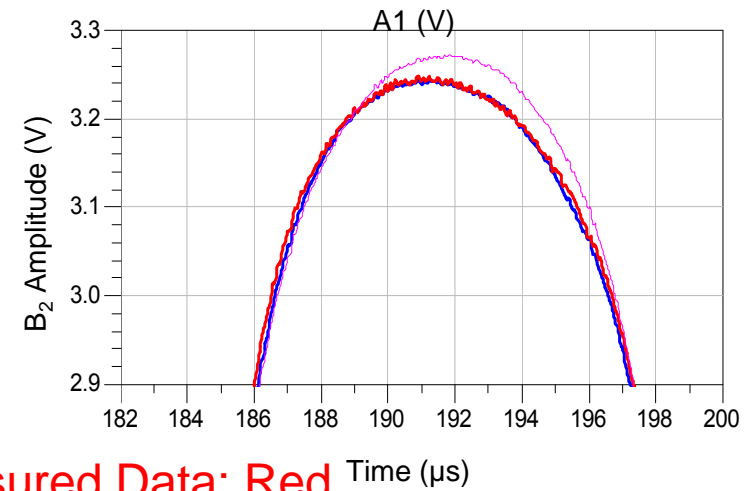
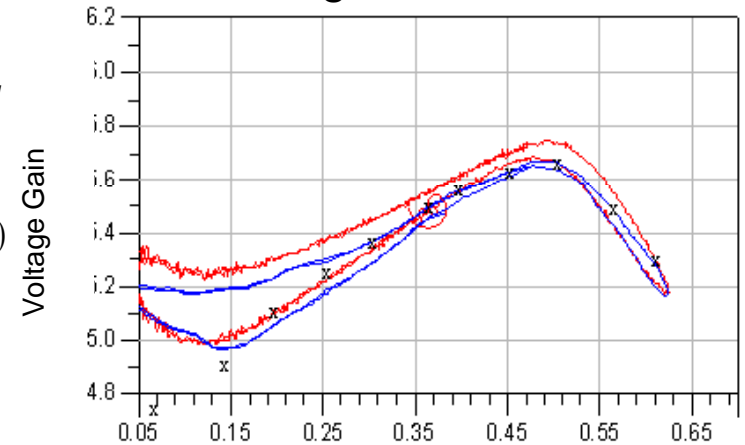
## Fundamental “hidden variable” theory

Verspecht et al “Extension of X-parameters to include long-term dynamic memory effects,” *IEEE MTT-S Int’l Microwave Symposium Digest*, 2009. pp 741-744

$$B(t) = \left\{ XF_{21}(|A(t)|) + \int_0^{\infty} G(|A(t)|, |A(t-u)|, u) du \right\} e^{j\phi(A(t))}$$



Anadigics AWT6282

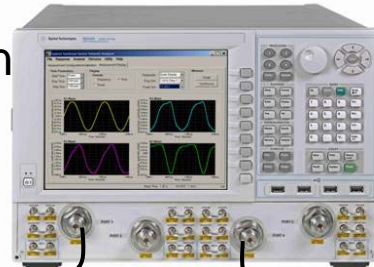


Measured Data: Red  
 Memory model prediction: Blue  
 Static X-parameter prediction: Magenta

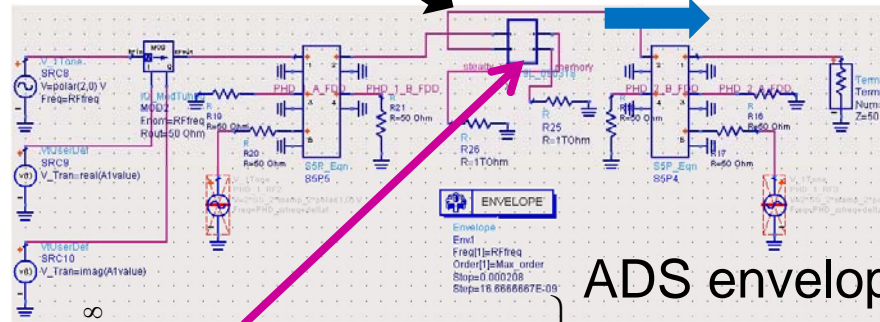
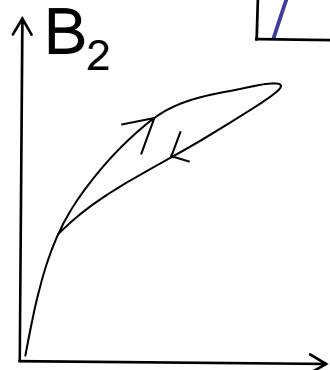
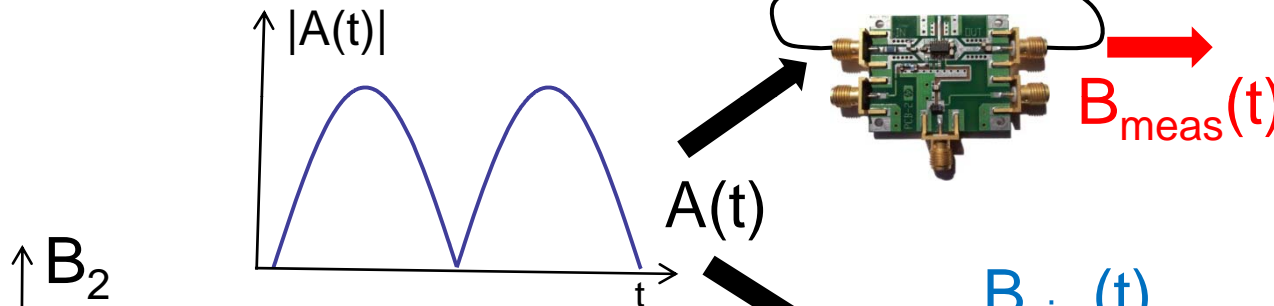
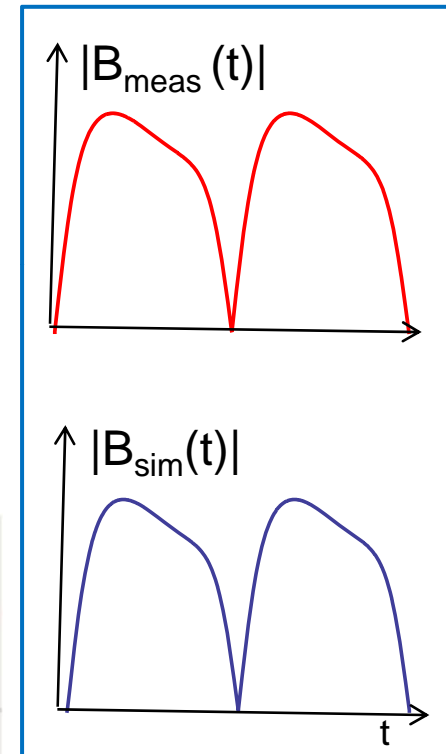


# Dynamic X-parameters Beyond Quasi-Static

- Pulsed Envelope NVNA extraction
- Prototyped in ADS
- Not yet commercialized



comparison

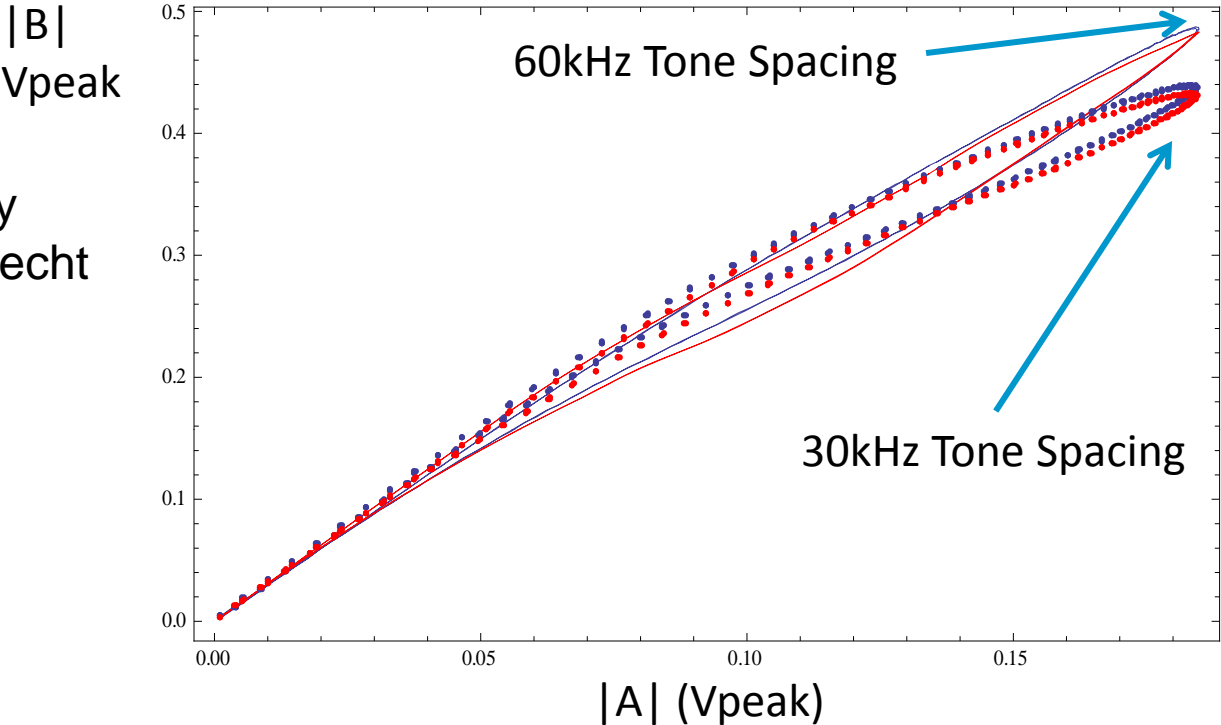


ADS envelope simulator

$$B(t) = \left\{ X F_{21}(|A(t)|) + \int_0^{\infty} G(|A(t)|, |A(t-u)|, u) du \right\} e^{j\varphi(A(t))}$$

# Dynamic X-parameters Predict Memory Effects

Courtesy  
J. Verspecht



ZFL11AD Amp  
F<sub>0</sub>= 1.75GHz

- Measurement 60kHz Tone Spacing
- Model 60kHz Tone Spacing
- Measurement 30kHz Tone Spacing
- Model 30kHz Tone Spacing

See Latest Research Results on Dynamic X-parameters

J. Verspecht, J. Horn, D. E. Root “A Simplified Extension of X-parameters to Describe Memory Effects for Wideband Modulated Signals”

ARFTG Conference Session 2-1 Friday, May 28, 2010 10:20AM (Hilton)

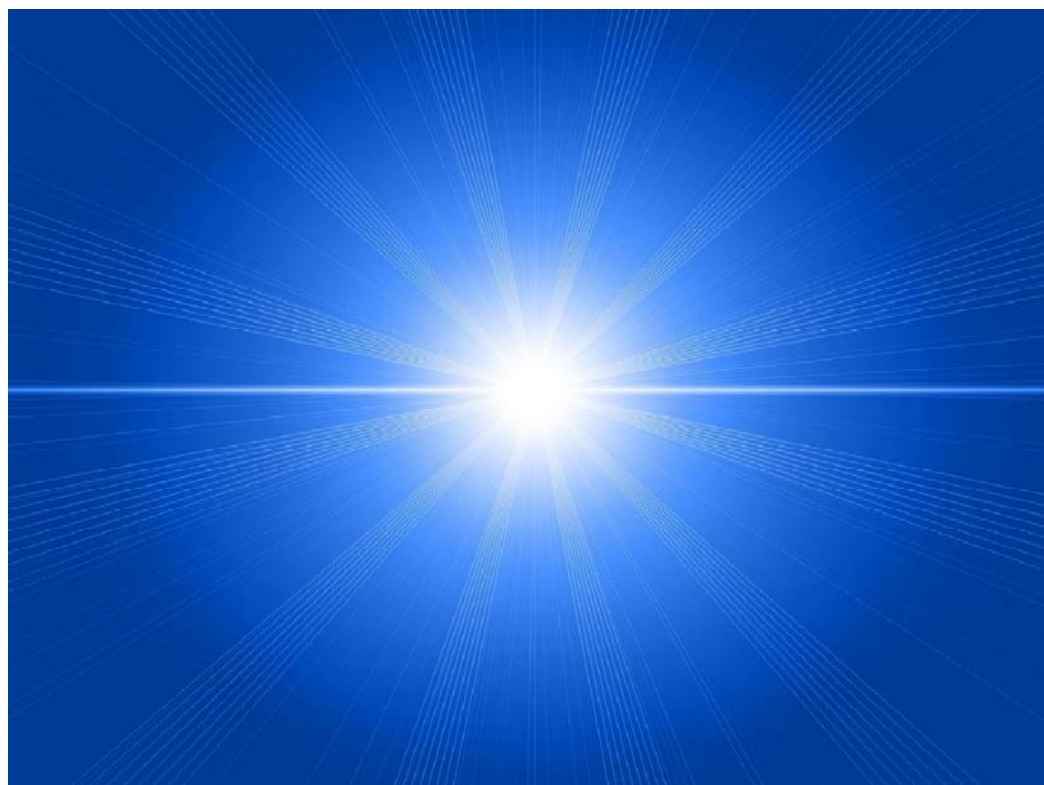
# Summary: X-parameter universe is expanding rapidly

Powerful, practical interoperable solutions for nonlinear characterization, modeling, and design of microwave and RF

**X-parameters: “doing for nonlinear components and systems what S-parameters do for linear components and systems”**

## Applications

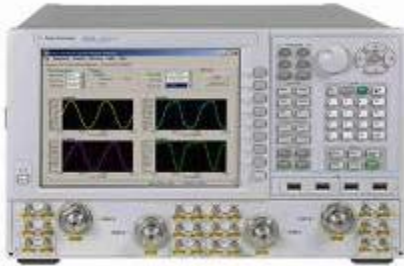
- X-parameters for GSM amp.
- Load-dependent X-parameters
- 50 GHz Agilent NVNA
- High-Power X-parameter meas.
- X-parameter generator in ADS
- XnP component in ADS
- Two-tone measured X-pars
- Three-port measured X-pars
- Memory: Dynamic X-params
- Device modeling
- Education, training, app. notes
- **Industry is adopting paradigm**



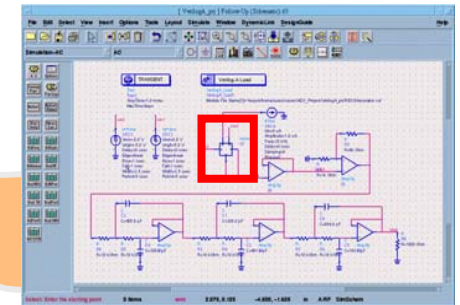


# X-Parameters: Agilest Completes the Nonlinear Puzzle!

Agilent Nonlinear Vector Network Analyzer



Electronic design automation software

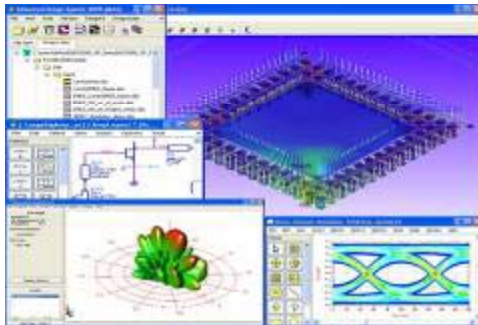


Nonlinear Measurements

Nonlinear Simulation & Design

Nonlinear Modeling

Customer Applications



$$B_{pm} = X_{pm}^F \langle A_{11} \rangle + X_{pm,qn}^S \langle A_{11} \rangle P^{m-n} A_{qn} + X_{pm,qn}^T \langle A_{11} \rangle P^{m+n} A_{qn}^*$$

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4. D. E. Root, J. Verspecht, D. Sharrit, J. Wood, and A. Cognata, "Broad-Band, Poly-Harmonic Distortion (PHD) Behavioral Models from Fast Automated Simulations and Large-Signal Vectorial Network Measurements," *IEEE Transactions on Microwave Theory and Techniques* Vol. 53. No. 11, November, 2005 pp. 3656-3664
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12. J. Verspecht, D. Gunyan, J. Horn, J. Xu, A. Cognata, and D.E. Root, "Multi-tone, Multi-Port, and Dynamic Memory Enhancements to PHD Nonlinear Behavioral Models from Large-Signal Measurements and Simulations," *2007 IEEE MTT-S Int. Microwave Symp. Dig.*, Honolulu, HI, USA, June 2007.
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14. <http://www.agilent.com/find/nvna> for NVNA
15. <http://www.agilent.com/find/mmic> for Agilent MMICs
16. <http://www.agilent.com/find/x-parameters-info> for information about X-parameter open standards