

## Non-reciprocal spin-wave propagation in spin-Hall oscillators: a two-dimensional analytical model

R. Zivieri<sup>1,2</sup>, A. Giordano<sup>2</sup>, R. Verba<sup>3</sup>, M. Carpentieri<sup>4</sup>, A.N. Slavin<sup>5</sup>, G. Finocchio<sup>2</sup>

<sup>1</sup>Department of Physics and Earth Sciences, University of Ferrara, Italy

<sup>2</sup>Department of Mathematical and Computer Sciences, Physical Sciences and Earth Sciences, University of Messina, Italy

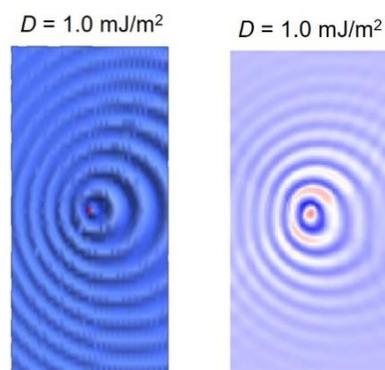
<sup>3</sup>Institute of Magnetism, National Academy of Sciences of Ukraine, Kyiv, Ukraine

<sup>4</sup>Department of Electrical and Information Engineering, Politecnico di Bari, Italy

<sup>5</sup>Department of Physics, Oakland University, Rochester, MI, USA

Non-reciprocity is an important feature of wave propagation in media and is typical of spin-wave propagation in ferromagnetic media [1,2] leading to potentially several physical and technological implications.

We have thus developed a two-dimensional analytical model for describing non-reciprocal spin-wave modes propagation in spin-Hall oscillators with oblique magnetization and in the presence of interfacial Dzialoshinski-Moriya interaction (*i*-DMI). We have found that the wave mode excited by the spin-Hall current is the solution of a generalized confluent Riemann equation and its 2D profile (see Figure 1) exhibits a non-reciprocal propagating behavior depending on the *i*-DMI constant *D*. According to analytical calculations and micromagnetic simulations, we have also shown that the dependence of the threshold current on the external magnetic field is not affected by the *i*-DMI amplitude. Spin-Hall oscillators can be employed as generators of non-reciprocal spin-wave modes for signal processing applications.



**Figure 1.** Left to right: Spatial profile of the excited wave mode according to the analytical model and to micromagnetic simulations.

[1] R. Verba, V. Tiberkevich, and A. Slavin, *Appl. Phys. Lett.* **107**, 112402 (2015).

[2] A. Giordano *et. al.*, *Sci. Rep.* **6**, 36020 (2016).