

Improving dependability of controlled systems: a challenge for automation science and engineering

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with contributions from Jean-Jacques Lesage and other colleagues and PhD students of the Automation Engineering team of LURPA http://www.lurpa.ens-cachan.fr/isa/

Dependable Control of Discrete event Systems

- Dependability
 - Dependability is the trustworthiness of a system which allows reliance to be justifiably placed on the service it delivers
 - Dependability attributes: safety, security, availability, reliability, maintainability
- Objective of our works: to develop methods, models and tools that improve design, implementation and operation of mainly discrete control systems, so as to increase the overall dependability.
- Targets: from basic embedded logic controller to networked automation systems
- Application fields: critical systems (energy, transport, healthcare, complex mechatronic systems)
- Industrial partners: Alstom, Dassault Systems, EDF,











Dependable Control of DES: the quest for the Holy Grail On-line approaches (during operation) • FDI, Diagnosis, Prognosis, ... • Dynamic reconfiguration, ...



Off-line approaches (during specification, design, implementation and validation)

- Fault Prevention (Synthesis, ...)
- Fault Forecasting (Fault Tree Analysis, ...)
- Fault Tolerance (Physically or functionally redundant solutions, ...)
- Fault Removal (Verification, Test, ...)

Some recent PhD works







Guillaume MERLE

Jean-Marc ROUSSEL, Jean-Jacques LESAGE

Fault Tree syntax



Fault Tree Analysis The case of Static Fault Trees (gates: OR, AND, K/among/M)



ALGEBRA

STRUCTURE FUNCTION $TE = A + (A \cdot B) + (A + C) \cdot D$ $= A + (C \cdot D)$

Qualitative analysis (minimal cut sets)

• direct: {A,C.D} (BDDs for complex SFTs)

Quantitative analysis (Pr{TE})

direct: Pr{TE} = Pr{A + (C.D)}

 $= \mathsf{Pr}\{\mathsf{A}\} + \mathsf{Pr}\{\mathsf{C}.\mathsf{D}\}$

 $= Pr{A} + Pr{C} \times Pr{D}$

(evaluation methods for complex SFTs)

Basic fault (event) : occurs with a given probability Pr{A}

The case of Dynamic Fault Tree Analysis (SFT + gates PAND, FDEP and Spare)



Asserts a functional dependency – that the failure of the trigger event causes the immediate and simultaneous failure of the dependent basic events [Dugan et al. 1992]



Output of gate occurs when the principal and all spares components have failed.

2 states for each spare component (active/dormant) associated to 2 failure rates : $\lambda/\alpha\lambda$

3 types of spares: Cold ($\alpha = 0$), Warm (0) $< \alpha < 1$), Hot ($\alpha = 1$)

Dugan et al. 2002]

No algebraic model for Dynamic Gates

Structure Function of DFT undeterminable

Qualitative analysis (minimal cut sequences)

Extracted from Occurrence graph of SPNs



Quantitative analysis

- Continuous Time Markov Chains, Markov **Decision Processes**
- limited to exponential distributions, time consuming

Dynamic Fault Tree Analysis (SFT + gates PAND, FDEP and Spare)



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Dynamic gates expressing a priority:

- Sequential (PAND)
- Preemption-based (FDEP)

Needs: modeling of the order of occurrence of fault events Results: Algebraic structure that allows determination of Structure Function and direct qualit. and quant. analysis

Dynamic gate expressing :

- Explicit duration of event
- Dependence between probabilities

(Pr{Bi} before A occurs < Pr{Bi] after A occurs)



FDEP

Spare

Algebraic model of faults

- Defined on $\mathbf{R}^+ \cup \{+\infty\}$ (faults = functions of time)
- Two values
 - 0: no fault
 - 1: fault
- non-repairable: single change of value

 \Rightarrow date of occurrence d(a)



- Set of non-repairable faults F_{nr}
- Two specific faults \perp and \top

Algebraic model of static gates (example OR gate)

Expected behaviour



Algebraic model

 $Q = A + B \quad \text{with} \quad +: F_{nr} \times F_{nr} \to F_{nr} \\ (a,b) \mapsto a + b \quad a + b = \begin{cases} a \text{ if } d(a) < d(b) \\ a \text{ if } d(a) = d(b) \\ b \text{ if } d(a) > d(b) \end{cases}$

• (F_{nr},+,.,⊥,⊤) is an abelian dioïd, like ({0,1},+,.,0,1)

- \Rightarrow common theorems of Boolean algebra usable
- ⇒ structure function of static fault trees is determinable and simplifiable

Algebraic model of BEFORE operator

Expected behavior:



Algebraic model:

$$\exists : F_{nr} \times F_{nr} \to F_{nr} \\ (a,b) \mapsto a \triangleleft b \qquad a \triangleleft b = \begin{cases} a \text{ if } d(a) < d(b) \\ \bot \text{ if } d(a) \ge d(b) \end{cases}$$

Behavioral & probabilistic model of dynamic gates

Gate symbol	Behavioral model	Probabilistic model
	$Q = (A.B).(A \le B)$ $= B.(A \le B)$	$\Pr\{Q\}(t) = \int_{0}^{t} f_{B}(u) F_{A}(u) du$
	$A_{T} = (A \leq T) + T = A + T$ $B_{T} = (B \leq T) + T = B + T$	$\Pr\{A_{T}\}(t) = F_{A}(t) + F_{T}(t) - F_{A}(t) \times F_{T}(t)$ $\Pr\{B_{T}\}(t) = F_{B}(t) + F_{T}(t) - F_{B}(t) \times F_{T}(t)$
	$\begin{cases} Q = B_a . (A \triangleleft B_a) + A . (B_d \triangleleft A) \\ B_d . B_a = \bot \end{cases}$ B may be active or dormant	$\Pr\{Q\}(t) = \int_{0}^{t} \left(\int_{v}^{t} f_{B_{a}}(u,v) du\right) f_{A}(v) dv$ $+ \int_{0}^{t} F_{B_{d}}(u) f_{A}(u) du$

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Some theorems for development and simplification

Simplification Theorems	Development Theorems
$f + g = g + f \qquad f + (f.g) = f$ $f.g = g.f \qquad f.(f + g) = f$ $f + (g + h) = (f + g) + f \qquad f + \bot = f$ $f.(g.h) = (f.g).f \qquad f.T = f$ $f + f = f \qquad f + T = T$ $f.f = f \qquad f. \bot = \bot$	f + (g.h) = (f + g).(f + h) f.(g + h) = (f.g) + (f.h)

Simplification Theorems	Development Theorems
$f + (f \triangleleft g) = f \qquad f \triangleleft f = \bot$ $g + (f \triangleleft g) = f + g \qquad f \triangleleft \bot = f$ $f \triangleleft f = \bot$ $f \land (f \triangleleft g) = f \triangleleft g \qquad \bot \triangleleft f = \bot$ $f + ((f \triangleleft g) . h) = f \qquad f \triangleleft T = \bot$ $(f \triangleleft g) . (g \triangleleft h) . (f \triangleleft h) = (f \triangleleft g) . (g \triangleleft h)$ $(f \triangleleft g) . (g \triangleleft f) = \bot$	$f \triangleleft (g+h) = (f \triangleleft g).(f \triangleleft h)$ $(f+g) \triangleleft h = (f \triangleleft h) + (g \triangleleft h)$ $f \triangleleft (g.h) = (f \triangleleft g) + (f \triangleleft h)$ $(f.g) \triangleleft h = (f \triangleleft h).(g \triangleleft h)$ $(f \triangleleft g) \triangleleft h = (f \triangleleft g).(f \triangleleft h)$

Another example [Fussel, 1976]



Qualitative analysis

minimal cut sequences: {P,S},{S,P} and {C,P}



Quantitative analysis using our algebraic method (1)

quantitative analysis:

 $TE = (P.S) + P.(C \triangleleft P) \Longrightarrow \Pr\{TE\} = \Pr\{(P.S) + P.(C \triangleleft P)\}$ $= \Pr\{P.S\} + \Pr\{P.(C \triangleleft P)\} - \Pr\{(P.S).(P.(C \triangleleft P))\}$ $= \Pr\{P\} \times \Pr\{S\} + \Pr\{P.(C \triangleleft P)\} - \Pr\{S.(P.(C \triangleleft P))\}$ $= \Pr\{P\} \times \Pr\{S\} + \Pr\{P.(C \triangleleft P)\} - \Pr\{S\} \times \Pr\{P.(C \triangleleft P)\}$ $= \Pr\{P\} \times \Pr\{S\} + \Pr\{S\} + \Pr\{P.(C \triangleleft P)\} - \Pr\{S\} \times \Pr\{P.(C \triangleleft P)\}$

Pr{P} and Pr{S} are known whatever the distribution Pr{P.(C \lhd P)} is known from the distributions of C and P $\forall (A,B), \Pr \{B.(A \lhd B)\} = \int_{0}^{t} f_{B}(u)F_{A}(u)du, F_{A}(t) = \int_{0}^{t} f_{A}(v)dv$

the method does not depend on the distribution



Quantitative analysis (2)

quantitative analysis for an exponential distribution: $\Pr\{P\}(t) = \int_{a}^{t} f_{p}(u) du = \int_{a}^{t} \lambda_{p} e^{-\lambda_{p} u} du = 1 - e^{-\lambda_{p} t}$ $\Pr\{S\}(t) = \int f_s(u) du = \int \lambda_s e^{-\lambda_s u} du = 1 - e^{-\lambda_s t}$ $\Pr\left\{P.(C \triangleleft P)\right\}(t) = \int_{C}^{t} f_{\rho}(u) F_{c}(u) du = \int_{C}^{t} \lambda_{\rho} e^{-\lambda_{\rho} u} \left(1 - e^{-\lambda_{c} u}\right) du$ $=\frac{\lambda_{\rho}}{\lambda_{c}+\lambda_{\rho}}\mathbf{e}^{-(\lambda_{c}+\lambda_{\rho})t}-\mathbf{e}^{-\lambda_{\rho}t}+\frac{\lambda_{c}}{\lambda_{c}+\lambda_{\rho}}$ $\Pr\{TE\}(t) = \Pr\{P\}(t) \times \Pr\{S\}(t) + (1 - \Pr\{S\}(t)) \times \Pr\{P.(C \triangleleft P)\}(t)$ $=\frac{\lambda_{\rho}}{\lambda_{c}+\lambda_{\rho}}e^{-(\lambda_{c}+\lambda_{\rho}+\lambda_{s})t}-e^{-\lambda_{\rho}t}-\frac{\lambda_{\rho}}{\lambda_{c}+\lambda_{r}}e^{-\lambda_{s}t}+1$

More detail: Probabilistic Algebraic Analysis of Fault Trees with Priority Dynamic Gates and Repeated Events, *G. Merle, J.-M. Roussel, J.-J. Lesage*, A. Bobbio, IEEE Trans. on Reliability, 59(1), pp. 250-261, March 2010





Silvain RUEL, Olivier DE SMET, Jean-Marc FAURE

Time performances of networked automation systems



event

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Aim of this study

- Simulation techniques (based on analysis of Petri nets models of the NAS or on specific network simulator):
 - are non-exhaustive
 - then can provide a distribution of a time performance but not the bounds of this distribution.
- Is it possible to obtain these bounds by formal verification of timed models?
 - Exhaustive analysis technique
- Two issues to solve:
 - How to obtain numerical values from results of verification of logic properties?
 - How to avoid (limit) combinatory explosion?

Formal verification of timed models



Five kinds of formal properties with the selected model-checker (UPPAAL)

- E<>p (possibility)
- E[]p (potentially always)
- A<>p (eventually)
- A[]p (invariantly)
- p→q (leads to)

Only logic properties can be checked; it is not possible to obtain a numerical value at the end of the verification

Contribution (1): parametric observer automaton

Parametric observer automaton structure



Three cases

• t_o - t_i < τ

Basic idea

- t_o t_i = τ
- t_o t_i > τ



Associated reachability properties

- P1 : E<> OBS.3
- P2 : E<> OBS.4
- P3 : E<> OBS.5

There exists at least one execution such that the state 3 (resp. 4, 5) is reached.

- τ is the upper bound iff P1 and P2 are verified and P3 is not verified
- τ is the lower bound iff P2 and P3 are verified and P1 is not verified

Contribution (2): Iterative proofs of logic properties







Scalability



Two-stepped abstraction method

U(PA



time properties of networked automation systems. WODES'08, pp. 334-339, Göteborg (Sweden), May 2008

Experimental validation



Results obtained by iterative proofs

• RTmin = 9.49 ms

 ∇c

• RTmax = 23.13 ms



- All the measured values are within the computed bounds.
- Small differences between the computed bounds and the minimum/maximum values of the distribution: 11% for the lower bound, 4% for the upper bound

Other works on networked automation systems

- Formal verification of properties of redundant Ethernet Powerlink
 - Cooperation with Alstom Power (PhD work of Steve Limal)
 - Examples of properties
 - Each message is transmitted even if one medium fails.
 - Each failure must be detected.
 - The redundant extension must not trigger the CSMA/CD mechanism.

Automation cell











Other works on networked automation systems

- Analytic evaluation of the response time using the (max,+) algebra
 - PhD work of Boussad Addad)
 - The system is modeled as a set of Timed Event Graphs (Petri nets where every place has at most one upstream and one downstream transition).
 - The distribution and its bounds can be obtained from the analytic expression.



For details:

Analytic Calculus of Response Time in Networked Automation Systems,

B. Addad, S. Amari, J-J. Lesage, IEEE Trans. on Automation Science and Engineering Vol. 7, Issue. 4, pp. 858-869, 2010.



Conformance test of logic controllers from specifications in Grafcet language



Julien PROVOST, Jean-Marc ROUSSEL, Jean-Marc FAURE

(In the frame of the TESTEC (Test of critical real-time embedded systems) project funded by the French Research Agency)



Aim of conformance test

Check whether an implementation, seen as a black-box with inputs-outputs, behaves correctly with respect to its specification



Conformance test execution

The implementation under test is connected to a test-bench which generates an inputs sequence.

The observed outputs sequence is compared to the expected one.



How to build automatically the test sequence from the specification?



Constraints of this study

- Specification in Grafcet language (IEC 60848 standard)
- Conformance test must be complete: every evolution from every state of the specification must be tested
- Non-invasive test
- Automatic construction of the test sequence
- Only non-timed models are considered



2 scientific issues / 2 scientific contributions

How to obtain a formal model from a Grafcet specification?

- The Grafcet standard provides only textual descriptions of the evolution rules.
- A formal model is mandatory to build a complete test sequence.

How to build a test sequence suitable for controllers with cyclic I/O scanning?

A formal semantics of Grafcet in the form of FSM (Mealy machine)

- Parallel and transient evolutions are taken into account
- Relies on an intermediary model: Stable Location Automaton

Definition of the SICtestability concept

• To prevent from spurious test results

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From Grafcet to FSM

 $t3 + a \cdot \overline{b} \cdot \overline{c}$

OP2 5

t6 + 1

OP3

Grafcet

1

OP1

t1 + a 2



Stable Location Automaton



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Some figures

Grafcet



850 ms

- 9 inputs and 10 outputs
- Several sub-graphs: 16 steps and 15 transitions
- Transition conditions are defined by Boolean expressions

Stable Location Automaton

- Same numbers of inputs and outputs
- State machine: 64 locations and 389
 evolutions
- Evolution conditions are defined by Boolean expressions



FSM

- 2⁹ input alphabet and 2¹⁰ output alphabet elements
- State machine: 64 states and 32,768 transitions
- Every transition is labeled by a couple (input,output)

Provost, J., et al. Translating Grafcet specifications into Mealy machines for conformance test purposes. Control Engineering Practice (2010), doi:10.1016/j.conengprac.2010.10.001

Test sequence construction from the equivalent FSM

The test sequence must be:

- Initializable: the first test step corresponds to a transition that starts from the initial state
- Complete: every transition must be tested at least once

Two optimization criteria

- **Classical approach**: minimization of the length (number of test steps)
 - Transition-Tour method, variant of the Chinese Postman problem
 - For the previous example, this sequence comprises 73,528 test steps and is computed in less than 2 s
 - Erroneous verdicts may occur with logic controllers with cyclic I/O scanning
- Our proposal: minimization of the number of MIC test steps
 - To avoid the previous issue
 - Definition of the concept of SIC-testability

Conformance test execution experiments with minimum-length sequences



First program

Correct program, model-checked

→Test bench may reject the program. False errors are sometimes declared.

Second program

Erroneous program, with intentionally added errors

 \rightarrow Test bench may accept the program. All errors are not always detected.

→Biased results

→Non-valid results

→ Lack of confidence in the conformance test verdicts

Results analysis

All verdict errors occur when several input values are changed simultaneously.

Synchronous events generated by the test-bench are seen as asynchronous by the implementation under test.



Solutions

- Synchronize the test-bench and the controller under test
 - Not always easy and not realistic (a plant is not synchronized with its controller)
- Privilege SIC test sequences





SIC (Single Input Change) test sequence Only one <u>logical input</u> changes at any date t_i

Proposed method to build test sequences

- Is the specification SIC-testable? (an initializable, complete and SIC test sequence can be built from the specification)
 - If the specification is not SIC-testable, determine its SIC-testable part.

Build the test sequence

- For a SIC-testable specification, this sequence is obtained by solving a Traveling Salesman problem on a specific graph whose nodes are couples (state, inputs valuation)
- For a non-SIC-testable specification, this sequence is composed of a SIC sequence to test its SIC-testable part followed by a MIC sequence to test the remaining transitions
- For more details:

Provost, J., et al. SIC-testability of sequential logic controllers. WODES 2010, Berlin, pp. 203-208, August 30 - September 1, 2010

Provost, J., et al. Testing Programmable Logic Controllers from Finite State Machines specification. DCDS'11, pp. 3-8, Saarbrücken, Germany, June 15-17, 2011

Checking SIC-testability of a specification (1)

A SIC relation is defined between two inputs valuations

- v_I and v'_I satisfy a SIC relation: they differ in only one input $dim((v_I \setminus v'_I) \cup (v'_I \setminus v_I)) = 1$
- Notation: $\mathbf{v}'_{\mathbf{I}} \operatorname{R}_{\operatorname{Gray}} \mathbf{v}_{\mathbf{I}}$ $dim((v_{I} \setminus v'_{I}) \cup (v'_{I} \setminus v_{I})) = 1 \Leftrightarrow v'_{I} \operatorname{R}_{\operatorname{Gray}} v_{I}$

• Example

$$a \cdot b \quad R_{Gray} \quad a \cdot \overline{b} \quad ?$$

$$dim((\{a, b\} \setminus \{a\}) \cup (\{a\} \setminus \{a, b\}))$$

$$= dim(\{a\} \cup \emptyset)$$

$$= 1$$

$$a \cdot b \quad R_{Gray} \quad \overline{a} \cdot \overline{b} \quad ?$$

$$dim((\{a, b\} \setminus \emptyset) \cup (\emptyset \setminus \{a, b\}))$$

$$= dim(\{a, b\} \cup \emptyset)$$

$$= 2$$

→ This specification is not SIC-testable



Checking SIC-testability of a specification (2)

SIC-testability checking is based on a fixed point computation, starting from the initial state

The SIC-testable part of the example is shown on the right.

Two transitions of the original model are not SIC-testable (cannot be included into a \overline{a} SIC test sequence): \overline{a}

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(s_1, \overline{a} \cdot \overline{b}) 
(s_3, \overline{a} \cdot b)
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A SIC test sequence can be generated for the SIC-testable part.

Conclusions

 DES modeling and analysis techniques can definitely contribute to improve the dependability attributes (safety, security, availability, ...) of automated systems

• However, be careful with:

- Combinatory explosion when dealing with non-trivial systems
 - Abstraction mechanisms or algebraic approaches may lessen (remove) this issue
- Construction of the formal models
 - A DES model may be mathematically sound but meaningless w.r.t. the real world
- Industrial acceptance of the scientific results and scientific acceptance of the industrial constraints and practices (tailored-made languages, existing engineering environments, well-established know-how)



Thank you !



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